THE FIRST STARS

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Abstract  We review recent theoretical results on the formation of the first stars  
in the universe, and emphasize related open questions. In particular, we discuss  
the initial conditions for Population III star formation, as given by variants of the cold  
dark matter cosmology. Numerical simulations have investigated the collapse and the  
fragmentation of metal-free gas, showing that the first stars were predominantly very  
massive. The exact determination of the stellar masses, and the precise form of the  
primordial initial mass function, is still hampered by our limited understanding of the  
accretion physics and the protostellar feedback effects. We address the importance of  
heavy elements in bringing about the transition from an early star formation mode  
dominated by massive stars to the familiar mode dominated by low-mass stars at later  
times. We show how complementary observations, both at high redshifts and in our  
local cosmic neighborhood, can be utilized to probe the first epoch of star formation.

1. INTRODUCTION

The first stars to form out of unenriched H/He gas marked the crucial transition  
from a homogeneous, simple universe to a highly structured, complex one at  
the end of the cosmic dark ages. Extending the familiar scheme of classifying  
stellar populations in the local universe (Baade 1944) to the extreme case of zero  
metallicity, the first stars constitute the so-called Population III (e.g., Bond 1981;  
Cayrel 1986; Carr 1987, 1994). The quest for Population III stars has fascinated  
astronomers for many decades, back to the first tentative ideas of Schwarzschild  
& Spitzer (1953). Recently, the subject has attracted increased interest, both from  
a theoretical and an observational perspective. New empirical probes of the high-  
redshift universe have become available, and our ability to carry out sophisticated  
numerical simulations has improved dramatically. In this review, we summarize  
the current state of this rapidly evolving field.
The first generation of stars had important effects on subsequent galaxy formation (see Carr et al. 1984 for an early overview). On the one hand, Population III stars produced copious amounts of UV photons to reionize the universe (e.g., Tumlinson & Shull 2000, Bromm et al. 2001b; Schaerer 2002, 2003; Tumlinson et al. 2003; Venkatesan & Truran 2003; Venkatesan et al. 2003). Recently, the Wilkinson Microwave Anisotropy Probe (WMAP) observed the large-angle polarization anisotropy of the cosmic microwave background (CMB), thus constraining the total ionizing photon production from the first stars (e.g., Cen 2003a,b; Ciardi et al. 2003; Haiman & Holder 2003; Holder et al. 2003; Kaplinghat et al. 2003; Kogut et al. 2003; Sokasian et al. 2003a,b; Wyithe & Loeb 2003a,b). The large optical depth to Thomson scattering measured by WMAP has been interpreted as a signature of a substantial early activity of massive star formation at redshifts $z \gtrsim 15$ (see Section 5.1). On the other hand, the supernova (SN) explosions that ended the lives of the first stars were responsible for the initial enrichment of the intergalactic medium (IGM) with heavy elements (e.g., Ostriker & Gnedin 1996, Gnedin & Ostriker 1997, Ferrara et al. 2000, Madau et al. 2001, Mori et al. 2002, Thacker et al. 2002, Bromm et al. 2003, Furlanetto & Loeb 2003, Mackey et al. 2003, Scannapieco et al. 2003, Wada & Venkatesan 2003, Yoshida et al. 2004). An intriguing possibility unique to zero-metallicity massive stars is the complete disruption of the progenitor in a pair-instability supernova (PISN), which is predicted to leave no remnant behind (e.g., Barkat et al. 1967, Ober et al. 1983, Bond et al. 1984, Fryer et al. 2001, Heger & Woosley 2002, Heger et al. 2003). This peculiar explosion mode could have played an important role in quickly seeding the IGM with the first metals (see Section 4.2).

To place the study of the first stars into the appropriate cosmological context, one has to ask (see Section 2), When and how did the cosmic dark ages end? During this time between the emission of the CMB half a million years after the big bang, when the CMB photons shifted into the infrared, and the formation of the first sources of light, the universe would have appeared completely dark to a human observer (see Barkana & Loeb 2001, Loeb & Barkana 2001, Miralda-Escudé 2003 for comprehensive reviews of this cosmic epoch). Historically, the evocative—and now widely used—dark age analogy was first introduced into the literature briefly after the ascent of nonbaryonic, cold dark matter (CDM) scenarios (e.g., Sargent 1986, Rees 1993). In the context of popular CDM models of hierarchical structure formation, the first stars are predicted to have formed in dark matter (DM) halos of mass $\sim 10^8 M_\odot$ that collapsed at redshifts $z \approx 20–30$ (e.g., Tegmark et al. 1997, Yoshida et al. 2003a). The first quasars, however (e.g., Umemura et al. 1993, Loeb & Rasio 1994, Eisenstein & Loeb 1995), are likely to have formed in more massive host systems, at redshifts $z \gtrsim 10$ (Haiman & Loeb 2001, Bromm & Loeb 2003a), and certainly before $z \sim 6.4$, which is the redshift of the most distant quasar known (Fan et al. 2003). Here, we do not discuss quasar formation in depth, and we refer the reader to the references above.

The most fundamental question about the first stars is how massive they typically were (see Section 3). Results from recent numerical simulations of the collapse
and fragmentation of primordial gas clouds suggest that the first stars were predominantly very massive, with typical masses $M_\ast \gtrsim 100 M_\odot$ (Bromm et al. 1999, 2002; Nakamura & Umemura 2001; Abel et al. 2000, 2002). The simulations have taught us that regardless of the detailed initial conditions, the primordial gas attains characteristic values of temperature and density. These, in turn, correspond to a characteristic fragmentation scale, given approximately by the Jeans mass, and they are explained by the microphysics of molecular hydrogen (H$_2$) cooling (see Section 3.2). The minihalos that host the formation of the first stars have virial temperatures of order $\sim 1000$ K, below the threshold for cooling owing to atomic hydrogen lines ($\sim 10^4$ K). Therefore, cooling and fragmentation inside these minihalos are possible only via rotational-vibrational transitions of H$_2$, which can be excited even at these low temperatures (see Section 2 for details).

Despite the progress already made, many important questions remain unanswered. A particularly important one, for example, is: What is the functional form of the primordial initial mass function (IMF)? Constraining the characteristic mass scale still leaves undetermined the overall range of stellar masses and the power-law slope, which is likely to be a function of mass (e.g., Yoshii & Saio 1986; Larson 1998; Nakamura & Umemura 2001, 2002; Omukai & Yoshii 2003). In addition, it is presently not known whether binaries or, more generally, clusters of zero-metallicity stars can form (see Section 3.2). This question has important implications for the star formation process. If Population III star formation typically resulted in a binary or multiple system, much of the progenitor cloud’s angular momentum could go into the orbital motion of the stars in such a system. However, if an isolated formation mode were to predominate, the classical angular momentum barrier could be much harder to breach (see Larson 2003).

How was the epoch of Population III star formation eventually terminated (see Section 4)? Two categories of negative feedback effects are likely to be important, the first being radiative and the second chemical in nature (e.g., Ciardi et al. 2000b, Schneider et al. 2002a, Mackey et al. 2003). The radiative feedback consists in soft UV photons produced by the first stars photodissociating the rather fragile H$_2$ molecules in the surrounding gas, thus suppressing the corresponding H$_2$ cooling (e.g., Haiman et al. 1997, 2000; Omukai & Nishi 1999; Ciardi et al. 2000a; Nishi & Tashiro 2000; Glover & Brand 2001). Massive Population III stars could then no longer form. There is some debate, however, about whether the radiative feedback from the first stars was positive or negative (e.g., Ferrara 1998; Machacek et al. 2001, 2003; Oh 2001; Ricotti et al. 2001; Cen 2003b). The formation of H$_2$ molecules is catalyzed by free electrons, and any process that increased their presence would therefore also boost the abundance of H$_2$. For example, an early background of X-ray photons, either from accretion onto black holes (e.g., Madau et al. 2004) or from the remnants of Population III SNe, could ionize the gas and thus increase the abundance of free electrons (e.g., Haiman et al. 2000, Venkatasekaran et al. 2001, Glover & Brand 2003, Machacek et al. 2003). This debate is ongoing, and it is too early for definitive conclusions (see Section 4.1 for details).
The second feedback effect that is important in terminating the epoch of Population III star formation is chemical—it is due to the enrichment of the primordial gas with the heavy elements dispersed by the first SNe (see Section 4.2). Numerical simulations of the fragmentation process have shown that lower mass stars can only form out of gas that was already preenriched to a level in excess of a critical metallicity estimated to be of order $10^{-4}$–$10^{-3}$ the solar value (Bromm et al. 2001a; see also Schneider et al. 2002a). Depending on the nature of the first SN explosions, and in particular on how efficiently and widespread the metal-enriched ejecta are mixed into the surrounding gas, the cosmic star formation will at some point undergo a fundamental transition from an early, high-mass (Population III) dominated mode to one dominated by lower mass stars (Population II).

We conclude our review with a discussion of observational probes of the nature of the first stars (Section 5). Predicting the properties of the first stars is important for the design of upcoming instruments, such as the *James Webb Space Telescope*¹ (JWST) or the next generation of large (>10 m) ground-based telescopes. The hope is that over the coming decade, it will become possible to confront current theoretical predictions about the properties of the first sources of light with observational data. The increasing volume of data on high-redshift galaxies and quasars from existing ground- and space-based telescopes signals the emergence of this new frontier in cosmology.

## 2. COSMOLOGICAL CONTEXT

The establishment of the current standard ΛCDM model for cosmological structure formation (see Kirshner 2003, Ostriker & Steinhardt 2003 for recent reviews) has provided a firm framework for the study of the first stars. Within variants of the CDM model, where larger structures are assembled hierarchically through successive mergers of smaller building-blocks, the first stars are predicted to form in DM minihalos of typical mass $\sim 10^6 M_\odot$ at redshifts $z \sim 20–30$ (e.g., Couchman & Rees 1986). The virial temperatures in these low-mass halos, $T_{\text{vir}} \propto M^{2/3}(1+z)$ (Barkana & Loeb 2001), are below the threshold, $\sim 10^4$ K, for efficient cooling owing to atomic hydrogen (e.g., Hutchings et al. 2002, Oh & Haiman 2002). It was realized early on that cooling in the low-temperature primordial gas had to rely on molecular hydrogen instead (Saslaw & Zipoy 1967, Peebles & Dicke 1968).

Because the thermodynamic behavior of the primordial gas is primarily controlled by H$_2$ cooling, it is crucial to understand the nonequilibrium chemistry of H$_2$ formation and destruction (e.g., Lepp & Shull 1984, Anninos & Norman 1996, Abel et al. 1997, Galli & Palla 1998, Puy & Signore 1999). Because there are no dust grains to facilitate their formation (e.g., Hirashita & Ferrara 2002), molecules have to form in the gas phase. The most important formation channel

¹See http://ngst.gsfc.nasa.gov.
turns out to be the sequence $H + e^- \rightarrow H^- + \gamma$, followed by $H^- + H \rightarrow H_2 + e^-$. (McDowell 1961). The free electrons act as catalysts, and they are present as a residue from the epoch of recombination (Seager et al. 2000) or result from collisional ionization in accretion shocks during the hierarchical build-up of galaxies (e.g., Mac Low & Shull 1986, Shapiro & Kang 1987). The formation of hydrogen molecules thus ceases when the free electrons have recombined. An alternative formation channel relies on the intermediary $H_2^+$, with free protons as catalysts (e.g., Haiman et al. 1996, Abel et al. 1997). The $H^-$ channel, however, dominates in most circumstances (e.g., Tegmark et al. 1997). Calculations of $H_2$ formation in collapsing top-hat overdensities, idealizing the virialization of DM halos in CDM cosmogonies, have found a simple approximate relationship between the asymptotic $H_2$ abundance and virial temperature in the overdensity (or halo): $f_{H_2} \propto T^{1.5}_{vir}$ (Tegmark et al. 1997).

Applying the familiar criterion (Rees & Ostriker 1977, Silk 1977) for the formation of galaxies that the cooling timescale has to be shorter than the dynamical timescale, $t_{cool} < t_{dyn}$, one can derive the minimum halo mass at a given redshift inside of which the gas is able to cool and eventually form stars (e.g., Tegmark et al. 1997, Santoro & Thomas 2003). The $H_2$ cooling function has been quite uncertain, with rates that differ by an order of magnitude over the relevant temperature regime (Hollenbach & McKee 1979, Lepp & Shull 1984). Recent advances in the quantum-mechanical computation of the collisional excitation process (H atoms colliding with $H_2$ molecules) have provided a much more reliable determination of the $H_2$ cooling function (see Galli & Palla 1998, and references therein).

Combining the CDM prescription for the assembly of virialized DM halos with the $H_2$-driven thermal evolution of the primordial gas, a minimum halo mass of $\sim 10^6 M_\odot$ is required for collapse redshifts $z_{vir} \sim 20–30$. From detailed calculations, one finds that the gas in such a “successful” halo has reached a molecule fraction in excess of $f_{H_2} \sim 10^{-4}$ (e.g., Haiman et al. 1996, Tegmark et al. 1997, Yoshida et al. 2003a). These systems correspond to $3\sigma$–$4\sigma$ peaks in the Gaussian random field of primordial density fluctuations. In principle, DM halos that are sufficiently massive to harbor cold, dense gas clouds could form at higher redshifts, $z_{vir} \gtrsim 40$. Such systems, however, would correspond to extremely rare, high-$\sigma$ peaks in the Gaussian density field (e.g., Miralda-Escudé 2003). To more realistically assess the formation of cold and dense star-forming clouds in the earliest stages of cosmological structure formation, three-dimensional simulations of the combined evolution of the DM and gas are required within a cosmological set-up (Ostriker & Gnedin 1996, Gnedin & Ostriker 1997, Abel et al. 1998). These studies confirmed the important role of $H_2$ cooling in low-mass halos at high $z$. Recently, the problem of forming primordial gas clouds within a fully cosmological context has been revisited with high numerical resolution (Yoshida et al. 2003a,b,c,d). The resulting gas density field is shown in Figure 1 for a standard $\Lambda$CDM cosmology at $z = 17$. The bright knots at the intersections of the filamentary network are the star-forming clouds. They have individual masses (DM and gas) of $\sim 10^6 M_\odot$. As expected from the statistics of the high-$\sigma$ peaks (e.g.,
Figure 2  Condition for successful formation of cold, dense gas clouds. Mass-weighted mean H$_2$ fraction versus virial temperature. (Open circles) DM halos that fail to host cold gas clouds. (Filled circles) DM halos that succeed in harboring star-forming clouds. The critical line corresponds to the condition $t_{\text{cool}} \sim t_{\text{ff}}$. (From Yoshida et al. 2003a.)

Kaiser 1984), the primordial clouds are predominantly clustered, although there are a few cases of more isolated ones.

Whether a given DM halo successfully hosts a cold, dense ($T \lesssim 0.5 T_{\text{vir}}, n_H \gtrsim 5 \times 10^2 \text{ cm}^{-3}$) gas cloud can nicely be understood with the Rees-Ostriker criterion, as shown in Figure 2. Yoshida et al. (2003a) derive a minimum collapse mass of $M_{\text{crit}} \simeq 7 \times 10^5 M_\odot$, with only a weak dependence on collapse redshift (see also Haiman et al. 1996, Fuller & Couchman 2000, Machacek et al. 2001). The dynamical heating accompanying the merging of DM halos has an important effect on the thermal and chemical evolution of the gas. Clouds do not successfully cool if they experience too rapid a growth in mass.

The primordial gas clouds that are found in the cosmological simulations are the sites where the first stars form. It is, therefore, important to learn what properties these clouds have in terms of overall size, shape, and angular momentum contents. The latter is often expressed by the familiar spin-parameter $\lambda = L|E|^{1/2}/(GM^{5/2})$,
where $L$, $E$, and $M$ are the total angular momentum, energy, and mass, respectively. The spin parameter is a measure of the degree of rotational support, such that the ratio of centrifugal to gravitational acceleration is given by $\sim \lambda^2$ at virialization. The spin values measured in pure DM cosmological simulations can be described by a lognormal distribution function with a mean value of $\bar{\lambda} = 0.04$, similar to what is found for larger-scale systems (Jang-Condell & Hernquist 2001). Interestingly, the resulting angular momentum vectors for the gaseous and DM components generally do not align in the simulations of Yoshida et al. (2003a). The overall sizes of the Population III star-forming clouds are close to the virial radius of the host DM halo, with $R_{\text{vir}} \sim 100$ pc, which is not too different from the typical dimensions of present-day giant molecular clouds (e.g., Larson 2003). Depending on the degree of spin, the clouds have shapes with various degrees of flattening (e.g., Bromm et al. 2002, Yoshida et al. 2003a). Owing to the importance of pressure forces, however, overall cloud shapes tend to be rather spherical. To fully elucidate the properties of the star-forming primordial clouds, even higher resolution cosmological simulations will be necessary.

The theoretical predictions for the formation sites of the first stars sensitively depend on the exact nature of the DM component and its fluctuation spectrum. Recently, two models have been discussed that would much reduce the fluctuation power on small mass scales. The first of these, the warm dark matter (WDM) model (e.g., Bode et al. 2001), has been proposed to remedy the well-known problems of standard $\Lambda$CDM on subgalactic scales (e.g., Flores & Primack 1994, Moore et al. 1999). These concern the predicted large abundance of substructure or, equivalently, of satellite systems, and the high (cuspy) densities in the centers of galaxies. Both predictions are in conflict with observations. The second model, the “running” spectral index (RSI) model, is suggested by the combined analysis of the WMAP data, the 2dF galaxy redshift survey, and Lyman-$\alpha$ forest observations (Spergel et al. 2003, Peiris et al. 2003). A series of recent studies have worked out the consequences of these reduced small-scale power models on early star formation (Somerville et al. 2003; Yoshida et al. 2003b,c). Within these models, the star formation rate at $z \gtrsim 15$ is significantly reduced compared to the standard $\Lambda$CDM case. This is due to the absence of low-mass halos and their associated gas clouds, which are cooled by molecular hydrogen. We revisit this issue when we discuss the implications of the WMAP data for early star formation (Section 5.1).

3. FORMATION OF THE FIRST STARS

3.1. Star Formation Then and Now

Currently, we do not have direct observational constraints on how the first stars formed at the end of the cosmic dark ages. It is, therefore, instructive to briefly summarize what we have learned about star formation in the present-day universe, where theoretical reasoning is guided by a wealth of observational data (see Pudritz 2002, Ward-Thompson 2002, Larson 2003 for recent reviews).
Population I stars form out of cold, dense molecular gas that is structured in a complex, highly inhomogeneous way. The molecular clouds are supported against gravity by turbulent velocity fields and pervaded on large scales by magnetic fields. Stars tend to form in clusters ranging from a few hundred up to $\sim 10^6$ stars. It appears likely that the clustered nature of star formation leads to complicated dynamics and tidal interactions that transport angular momentum, thus allowing the collapsing gas to overcome the classical centrifugal barrier (Larson 2002). The IMF of Population I stars is observed to have the approximate Salpeter (1955) form (e.g., Kroupa 2002)

$$\frac{dN}{d \log M} \propto M^{-x},$$

where

$$x \approx \begin{cases} 
1.35 & \text{for } M \gtrsim 0.5 M_\odot \\
0.0 & \text{for } M \lesssim 0.5 M_\odot 
\end{cases}.$$

The IMF is not observationally well determined at the lowest masses, but theory predicts that there should be a lower mass limit of approximately 0.007 $M_\odot$ set by opacity effects. This theoretical limit reflects the minimum fragment mass, set when the rate at which gravitational energy is released during the collapse exceeds the rate at which the gas can cool (e.g., Low & Lynden-Bell 1976, Rees 1976). The most important feature of the observed IMF is that $\sim 1 M_\odot$ is the characteristic mass scale of Population I star formation in the sense that most of the mass goes into stars with masses close to this value. Recent hydrodynamical simulations of the collapse and fragmentation of turbulent molecular cloud cores (e.g., Padoan & Nordlund 2002, Bate et al. 2003) illustrate the highly dynamic and chaotic nature of the star formation process.

The metal-rich chemistry, magnetohydrodynamics, and radiative transfer involved in present-day star formation is complex, and we still lack a comprehensive theoretical framework that predicts the IMF from first principles. Star formation in the high-redshift universe, however, poses a theoretically more tractable problem owing to a number of simplifying features, such as (a) the initial absence of heavy elements and therefore of dust; (b) the absence of dynamically significant magnetic fields in the pristine gas left over from the big bang; and (c) the absence of any effects from previous episodes of star formation, which would completely alter the conditions for subsequent star formation. The cooling of the primordial gas then depends only on hydrogen in its atomic and molecular form. Whereas in the present-day interstellar medium, the initial state of the star-forming cloud is poorly constrained, the corresponding initial conditions for primordial star formation are simple, given by the popular $\Lambda$CDM model of cosmological structure formation. We now turn to a discussion of this theoretically attractive and important problem.

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2See http://www.ukaff.ac.uk/starcluster for an animation.
3.2. Clump Formation: The Characteristic Stellar Mass

How did the first stars form? This subject has a long and venerable history (e.g., Schwarzschild & Spitzer 1953; Matsuda et al. 1969; Yoneyama 1972; Hutchins 1976; Silk 1977, 1983; Yoshii & Sabano 1979; Carlberg 1981; Kashlinsky & Rees 1983; Palla et al. 1983; Yoshii & Saio 1986). In this review, we focus mainly on the more recent work since the renewed interest in high-redshift star formation that began in the mid-1990s (e.g., Haiman et al. 1996, Uehara et al. 1996, Haiman & Loeb 1997, Tegmark et al. 1997, Larson 1998).

The complete answer to this question would entail a theoretical prediction for the Population III IMF, which is rather challenging. A more tractable task is to estimate the characteristic mass scale, \( M_c \), of the first stars; most of the recent numerical work has focused on this simpler problem. The characteristic mass is the mass below which the IMF flattens or begins to decline (see Larson 1998 for examples of possible analytic forms). As mentioned above, this mass scale is observed to be \( \sim 1 \, M_\odot \) in the present-day universe. Because the detailed shape of the primordial IMF is highly uncertain, we focus here on constraining \( M_c \), as this mass scale indicates the typical outcome of the primordial star formation process, or where most of the available mass ends up (e.g., Clarke & Bromm 2003).

To fully explore the dynamical, thermal, and chemical properties of primordial gas, three-dimensional numerical simulations are needed, although more idealized investigations in two, one, or even zero (one-zone models) dimension are important in that they allow researchers to probe a larger parameter space. The proper initial conditions for primordial star formation are given by the underlying model of cosmological structure formation (see Section 2). It is, therefore, necessary to simulate both the DM and gaseous (baryonic) components. To date, two different numerical approaches have been used to simulate the general three-dimensional fragmentation problem in its cosmological context.

The first series of simulations used the adaptive mesh refinement (AMR) technique (Abel et al. 2000, 2002). The AMR algorithm creates a nested hierarchy of ever finer grids in fluid regions where high resolution is needed (see, e.g., Balsara 2001 for a recent review). This method allows one to accurately simulate problems with high dynamic range, i.e., large contrasts in density. Such a situation indeed occurs in primordial star formation, where the proper initial conditions are given by the large-scale (\( \lesssim 10 \, \text{kpc} \)) cosmological environment, and where the collapsing gas has to be followed all the way to protostellar scales (\( \lesssim 10^{-3} \, \text{pc} \)). The second series of simulations used the smoothed particle hydrodynamics (SPH) method (Bromm et al. 1999, 2002). This Lagrangian technique samples the continuous fluid with a finite number of particles whose mass is smoothed out according to a given distribution function (the SPH kernel). It has been applied to a wide range of problems in present-day star formation (see Monaghan 1992 for a standard review).

The SPH approach has the important advantage that it can easily accommodate the creation of sink particles (e.g., Bate et al. 1995). Quite generically, gravitational collapse proceeds very nonuniformly, such that the density in a few subregions
becomes much larger than the average. Numerically, this situation necessitates the adoption of increasingly small timesteps. Although the simulation follows the evolution of the select density peak in detail, the overall system is essentially frozen. To study the collective properties of star formation, i.e., the formation of multiple high-density clumps that interact with each other in a complex fashion (see Bate et al. 2003), the SPH particles are merged into more massive ones, provided they exceed a given density threshold. Recently, the dynamical range of the standard SPH method has been significantly improved by implementing a "particle splitting" technique (Kitsionas & Whitworth 2002, Bromm & Loeb 2003a). When the simulation reaches such high density in a certain region that a sink particle would normally be created, a complementary strategy is now adopted: Every SPH particle in the unrefined, high-density region acts as a parent particle and spawns a given number of child particles, endowing them with its properties. In effect, this is the SPH equivalent of the grid-based AMR technique.

The most important difference between these two studies lies in the way the initial conditions are implemented. The Abel et al. (2000, 2002) simulations start at $z = 100$ with a realistic cosmological set-up, considering a periodic volume of physical size $128/(1 + z)$ kpc. The AMR technique allows Abel et al. (2000, 2002) to bridge the gap from cosmological to protostellar scales. The Bromm et al. (1999, 2002) effort, however, initializes the simulations, also at $z = 100$, by realizing spherical overdensities that correspond to high-$\sigma$ peaks in the Gaussian random field of cosmological density fluctuations (see Katz 1991). The systems considered by Bromm et al. (1999, 2002) comprise halos of total mass $10^5$–$10^7 M_\odot$ that collapse at $z_{\text{vir}} \simeq 20$–30. The virialization (or collapse) redshift, $z_{\text{vir}}$, marks the approximate instant where the DM component settles into virial equilibrium (leading to $-E_{\text{grav}} \sim 2E_{\text{kin}}$). The Bromm et al. (1999, 2002) initial configurations are not simple "top-hat" (i.e., uniform density) clouds, however, as the dynamically dominant DM component is endowed with density fluctuations according to $P(k) \propto k^{-3}$, the asymptotic behavior of the $\Lambda$CDM power spectrum on small mass scales (e.g., Yoshida et al. 2003d). The Bromm et al. (1999, 2002) simulations, therefore, do reflect the basic bottom-up, hierarchical merging of smaller DM halos into larger ones, and the accompanying shock heating of the gas. Because of the isolated nature of their systems, Bromm et al. (1999, 2002) had to treat the initial amount of angular momentum (or spin) as a free parameter, imparting both the DM and gaseous components with solid-body rotation around the center of mass. In the Abel et al. (2000, 2002) simulations, tidal torques from neighboring halos generate the halo spin self-consistently. In summary, the Abel et al. (2000, 2002) investigation is the most realistic treatment of the primordial star formation problem to date, whereas the more idealized Bromm et al. (1999, 2002) simulations, implementing the same physical ingredients as Abel et al. (2000, 2002), have explored a much wider range of initial conditions.

In comparing the simulations of Abel et al. (2000, 2002) and Bromm et al. (1999, 2002), the most important aspect is that both studies, employing very different methods, agree on the existence of a preferred state for the primordial gas, corresponding to characteristic values of temperature and density, $T_c \sim 200$ K and
$n_c \sim 10^4 \, \text{cm}^{-3}$, respectively. These characteristic scales turn out to be rather robust in the sense that they are not very sensitive to variations in the initial conditions. In Figure 3 (panel c), this preferred state in the $T-n$ phase diagram can clearly be discerned. This figure, from the simulations of Bromm et al. (1999, 2002), plots the respective gas properties for each individual SPH particle. The diagram thus contains an additional dimension of information: Where evolutionary timescales are short, only a few particles are plotted, whereas they tend to accumulate where the overall evolution is slow. Such a “loitering” state is reached at $T_c$ and $n_c$.

**Figure 3** Properties of primordial gas. (a) Free electron abundance versus hydrogen number density (in cm$^{-3}$). (b) Hydrogen molecule abundance versus number density. (c) Gas temperature versus number density. At densities below $\sim 1 \, \text{cm}^{-3}$, the gas temperature rises because of adiabatic compression until it reaches the virial value of $T_{vir} \approx 5000 \, \text{K}$. At higher densities, cooling owing to H$_2$ drives the temperature down again until the gas settles into a quasi-hydrostatic state at $T_c \sim 200 \, \text{K}$ and $n_c \sim 10^4 \, \text{cm}^{-3}$. Upon further compression owing to the onset of the gravitational instability, the temperature experiences a modest rise again. (d) Jeans mass (in $M_\odot$) versus number density. The Jeans mass reaches a value of $M_{J} \sim 10^3 M_\odot$ for the quasi-hydrostatic gas in the center of the DM potential well. (From Bromm et al. 2002.)
These characteristic scales can be understood by considering the microphysics of H$_2$, the main coolant in metal-free, star-forming gas (Abel et al. 2002, Bromm et al. 2002). At temperatures $\lesssim 1000$ K, cooling is due to the collisional excitation and subsequent radiative decay of rotational transitions. The two lowest-lying rotational energy levels in H$_2$ have an energy spacing of $E / k_B \simeq 512$ K. Collisions with particles (mostly H atoms) that populate the high-energy tail of the Maxwell-Boltzmann velocity distribution can lead to somewhat lower temperatures, but H$_2$ cooling cannot proceed to $T \lesssim 100$ K. This explains the characteristic temperature. The characteristic density, in turn, is given by the critical density above which collisional deexcitations, which do not cool the gas, compete with radiative decays, which lead to cooling. This saturation of the H$_2$ cooling marks the transition from non-local thermodynamic equilibrium (non-LTE) rotational level populations to thermal (LTE) ones. At densities below $n_c$, the cooling rate is proportional to the density squared, whereas at higher densities, the dependence is only linear.

Once the characteristic state is reached, the evolution toward higher density is temporarily halted owing to the now inefficient cooling, and the gas undergoes a phase of quasi-hydrostatic, slow contraction. To move away from this loitering regime, enough mass has to accumulate to trigger a gravitational runaway collapse. This condition is simply $M \gtrsim M_J$, where the Jeans mass or, almost equivalently, the Bonnor-Ebert mass$^3$ can be written as (e.g., Clarke & Bromm 2003)

$$M_J \simeq 700 M_\odot \left( \frac{T}{200 \, \text{K}} \right)^{3/2} \left( \frac{n}{10^4 \, \text{cm}^{-3}} \right)^{-1/2}. \quad (3)$$

Primordial star formation, where magnetic fields and turbulence are expected to initially play no important dynamical role, may be the best case for the application of the classical Jeans criterion, which is describing the balance between gravity and the opposing thermal pressure (Jeans 1902).

A prestellar clump of mass $M \gtrsim M_J$ is the immediate progenitor of a single star or, in the case of further subfragmentation, a binary or small multiple system. In galactic star-forming regions, like $\rho$ Ophiuchi, such clumps with masses close to stellar values have been observed as gravitationally bound clouds that lack the emission from embedded stellar sources (e.g., Motte et al. 1998). The high-density clumps are clearly not stars yet. To probe the further fate of a clump, one first has to follow the collapse to higher densities up to the formation of an optically thick hydrostatic core (see Section 3.3), and subsequently the accretion from the diffuse envelope onto the central core (see Section 3.4). The parent clump mass, however, already sets an upper limit for the final stellar mass whose precise value is determined by the accretion process.

Although Abel et al. (2000, 2002) and Bromm et al. (1999, 2002) agree on the magnitude of the characteristic fragmentation scale, Abel et al. (2000, 2002)

$^3$An equilibrium isothermal sphere of finite size with a fixed temperature and boundary pressure is unstable to collapse if its mass exceeds the critical Bonnor-Ebert value (see Larson 2003).
have argued that only one star forms per halo, whereas Bromm et al. (1999, 2002) have simulated cases where multiple clumps form, such that the number of stars in a minihalo is \( N_* \sim 1–5 \). Among the cases studied by Bromm et al. (1999, 2002) favoring \( N_* > 1 \) are high-spin runs that lead to disk-like configurations, which subsequently fragment into a number of clumps or more massive halos (with total mass \( M \lesssim 10^7 M_\odot \)). Notice that the case simulated by Abel et al. (2000, 2002) corresponds to a gas mass of \( \sim 3 \times 10^4 M_\odot \). Such a low-mass halo is only marginally able to cool, and when Bromm et al. (1999, 2002) simulated a system with this mass, they also found that only a single star forms inside the halo. Further work is required to elucidate whether the multiple-clump formation in Bromm et al. (1999, 2002) also occurs in simulations with realistic cosmological initial conditions.

Whether primordial clusters of metal-free stars are able to form in the first galaxies is an important open question. The answer will determine the proper interpretation of the primordial IMF. If Population III star formation were generally clustered, as is the case in the present-day universe, the IMF would simply describe the actual distribution of stellar masses in a given cluster. However, if the first stars formed predominantly in isolation, the IMF would have the meaning of a probability distribution in a random process that results in only one stellar mass per “draw.” The present-day IMF, however, appears to be shaped largely by the chaotic interactions between many accreting protostars in a common reservoir of gas (e.g., Bate et al. 2003). If there were no cluster to begin with, how would the IMF be built up? Would there still be a self-similar extension at masses \( M > M_c \)?

Progress has to rely on improved simulations in future work, and it is difficult to guess the outcome.

A possible clustered nature of forming Population III stars would also have important consequences for the transport of angular momentum. In fact, a crucial question is how the primordial gas can so efficiently shed its angular momentum on the way to forming massive clumps. In the case of a clustered formation process, angular momentum could be efficiently transported outward by gravitational (tidal) torques. Tidal torques can then transfer much of the angular momentum from the gas around each forming clump to the orbital motion of the system, similar to the case of present-day star formation in a clustered environment (e.g., Larson 2002, Bate et al. 2003). In the isolated formation process of Abel et al. (2000, 2002), however, such a mechanism is not available. Alternatively, Abel et al. (2000, 2002) have suggested the efficient transport of angular momentum via hydrodynamic shocks during turbulent collapse. Again, more work is required to convincingly sort out the angular momentum transport issue. It may be possible that magnetic fields in an accretion disk around the primordial protostar could be sufficiently amplified by dynamo action from the suspected very weak primordial values (e.g. Kulsrud et al. 1997). The dynamo activity could occur as a consequence of turbulence that is driven by gravitational instabilities in the disk (Tan & Blackman 2004), and magnetic stresses could then facilitate angular momentum transport in the accretion disk.

As pointed out above, important contributions have also been made by more idealized, two- to zero-dimensional studies. These investigations typically ignore
the DM component, thus implicitly assuming that the gas has already dissipatively collapsed to the point where the DM ceases to be dynamically dominant. Much attention has been paid to the collapse of filamentary clouds (Nakamura & Umemura 1999, 2001, 2002). Results from one- and two-dimensional simulations that otherwise include all the relevant processes for the primordial chemistry and cooling have estimated fragmentation scales $M_c \sim 1 M_\odot$ and $M_c \sim 100 M_\odot$, depending on the (central) initial density. When the initial density is larger than $\sim 10^5 \text{ cm}^{-3}$, fragmentation leads to the lower mass value. This bifurcation has led to the prediction of a bimodal IMF for the first stars (Nakamura & Umemura 2001). It is, however, not obvious how such a high initial density can be reached in a realistic situation where the collapse starts from densities that are typically much smaller than the bifurcation value.

Recently, the question of whether low-mass metal-free stars can form has received considerable interest in connection with the discovery of extremely metal-poor (or more precisely iron-poor) galactic halo stars (see Section 5.2). Is it possible to place a firm lower limit on the mass of the first stars? Such a minimum mass may be given by the so-called opacity limit for fragmentation (e.g., Low & Lynden-Bell 1976, Rees 1976). The opacity limit, estimated to be $M_F \sim 0.007 M_\odot$ in present-day star formation, is the mass of a cloud that is no longer able to radiate away its gravitational binding energy in a free-fall time. For the case of metal-free stars, one-dimensional, spherically symmetric calculations have indicated a value that is rather similar to the present-day opacity limit (Omukai & Nishi 1998; see also Section 3.3). Whereas Omukai & Nishi (1998) have included all relevant sources of opacity in metal-free gas, a somewhat more idealized study by Uehara et al. (1996) has estimated that a cloud of $\sim 1 M_\odot$ may become opaque to H$_2$-line radiation. It is currently not clear how relevant the latter value is in a realistic collapse calculation.

We conclude this section with three other recent suggestions of how to produce lower-mass stars out of zero-metallicity gas. The first one is a modified version of the double-peaked (bimodal) IMF and it relies on the presence of deuterium hydride (HD) (Uehara & Inutsuka 2000, Nakamura & Umemura 2002). In principle, HD is a much more efficient coolant than H$_2$. It possesses a permanent electric dipole moment with Einstein $A$ coefficients that are larger by a factor of $10^3$ compared to the quadrupole transition probability for H$_2$. It can cool the gas to temperatures below $\sim 100 \text{ K}$ because its rotational level spacings are smaller than those of H$_2$ (e.g., Puy & Signore 1996, Flower et al. 2000). Bromm et al. (2002) included HD cooling in their simulations and found that it does not change the thermal evolution of the gas. It may, however, be possible to reach a regime where HD cooling becomes important when the gas cools down from temperatures above 10,000 K, e.g., in photoionization heated gas or in shock-heated material in dwarf-galaxy-size DM halos (masses $\gtrsim 10^8 M_\odot$).

The second idea postulates that the fragmentation scale (in effect the Jeans mass) will be reduced in gas that is bathed in soft UV radiation below the high masses predicted for the first stars (Omukai & Yoshii 2003). It is argued that the
strong UV radiation in the vicinity of a massive Population III star will destroy H₂, thus preventing the gas from reaching the characteristic loitering state. The gas may then be able to collapse, albeit at higher temperatures, to increasingly large densities (see also Omukai 2001). The three-dimensional simulations of Bromm & Loeb (2003a), although treating a very similar case, have failed to show the postulated fragmentation to small masses.

The final idea proposed the formation of lower-mass stars in zero-metal, shock-compressed gas (Mackey et al. 2003). The required compression could, for example, be induced by the first energetic SN explosions. Assuming that the shock is radiative and isobaric (e.g., Shapiro & Kang 1987) one can derive the expression

\[
M_J \simeq 10 M_\odot \left( \frac{n_0}{10^2 \text{ cm}^{-3}} \right)^{-1/2} \left( \frac{\mu_{sh}}{200 \text{ km s}^{-1}} \right)^{-1},
\]

where \(n_0\) denotes the preshock density and \(\mu_{sh}\) the velocity of the shock. Indeed, because a metal-free population of stars with a characteristic mass intermediate between the “classical” Population II and Population III cases would be quite distinct, Mackey et al. (2003) have suggested naming these hypothetical stars Population II.5. Numerical simulations of SN explosions at high redshifts have so far failed to bear out this prediction (Bromm et al. 2003), but it may be possible that Population II.5 stars can only form in more massive systems (see Salvaterra et al. 2003).

We conclude this section by pointing out that all the realistic three-dimensional simulations of the first star formation problem to date have consistently shown that the primordial gas fragments into massive clumps. Conversely, none of the suggestions for making low-mass stars out of zero-metallicity gas have yet been realized in a three-dimensional simulation. The tentative conclusion, therefore, is that the typical outcome of primordial star formation consists in massive clumps, and that low-mass clumps may need very special conditions to form.

### 3.3. Protostellar Collapse

What is the further fate of the clumps discussed above? In particular, one would like to test the notion that such a Jeans-unstable clump is the immediate progenitor of a single star that forms in its center. This evidently will only be correct if the clump does not undergo further subfragmentation upon collapsing to higher densities. It has long been suspected that such subfragmentation could occur at densities in excess of \(\sim 10^6 \text{ cm}^{-3}\), at which point three-body reactions become very efficient in converting the atomic gas (with only a trace amount of H₂ molecules from the H⁻ channel) into fully molecular form: \(3\text{H} \rightarrow \text{H}_2 + \text{H}\) (Palla et al. 1983). The H₂ coolant suddenly gets more abundant by a factor of \(\sim 10^3\). The corresponding boost in cooling could trigger a thermal instability, thus breaking up the clump into smaller pieces (Silk 1983). Both Abel et al. (2000, 2002) and Bromm et al. (1999, 2002) have included the three-body reactions in their chemical reaction networks and they have followed their simulations to higher densities to test whether or not
subfragmentation occurs [for the Bromm et al. (1999, 2002) model, this calculation is described in Bromm 2000 and Bromm & Loeb 2004]. Both groups report that no further subfragmentation is seen. With hindsight, this may not be too surprising. The reason is that any small density fluctuations that are present earlier on and that could serve as seeds for later fragmentation will have been erased by pressure forces during the slow, quasi-hydrostatic loitering phase at $n \sim n_c$. In addition, inefficient cooling may also play a role in suppressing high-density fragmentation. Despite the increase in the cooling rate throughout the fully molecular gas, cooling never leads to a significant drop in temperature owing to the counteracting effect of compressional heating and H$_2$ formation heating.

Extending the analogous calculation for the collapse of a present-day protostar (Larson 1969) to the primordial case, Omukai & Nishi (1998) have carried out one-dimensional hydrodynamical simulations in spherical symmetry. They also consider the full set of chemical reactions and implement an algorithm to solve for the radiative transfer in the H$_2$ lines as well as in the continuum. The most important result is that the mass of the initial hydrostatic core, formed in the center of the collapsing cloud when the density is high enough ($n \sim 10^{22}$ cm$^{-3}$) for the gas to become optically thick to continuum radiation, is almost the same as in present-day star formation: $M_{\text{core}} \sim 5 \times 10^{-3} M_\odot$. In Figure 4, the radial profiles of density, temperature, velocity, and H$_2$ abundance are shown (reproduced from Omukai & Nishi 1998). The profiles of density and velocity before the time of core formation (corresponding to the curves with label 6) are well described by the Larson-Penston (LP) similarity solution (Larson 1969, Penston 1969). The LP solution approximately describes the growth of the central density peak and is valid asymptotically in the limit of high central densities and small radii where the initial and boundary conditions have been “forgotten.” Once the core has formed, the self-similarity is broken. Similar results have been found by Ripamonti et al. (2002) who have in addition worked out the spectrum of the radiation that escapes from the collapsing clump (mostly in the IR as continuum and line photons). This type of approximately self-similar behavior seems to be a very generic result of collapse with a simple equation of state, even when rotation and magnetic fields are included (see Larson 2003). The apparent robustness of the LP solution thus supports the results found for the Population III case.

The small value of the initial core does not mean that this will be the final mass of a Population III star. This instead will be determined by how efficient the accretion process will be in incorporating the clump mass into the growing protostar. Before we discuss the accretion process in the following section, we briefly mention that fragments with masses close to the opacity limit could survive if the accretion process were somehow prematurely curtailed. This mechanism has been found in the simulation of a collapsing present-day, turbulent molecular cloud (Bate et al. 2003). A fraction of the accreting cores is ejected, by slingshot interactions with neighboring ones, from the natal cloud before they could grow to stellar masses, and thus end up as brown dwarfs (Bate et al. 2002). Again, such a mechanism would only work in a clustered environment, and as discussed above, this might not be valid for primordial star formation. An alternative suggestion to produce primordial
brown dwarfs invokes cooling owing to HD, which, as pointed out above, could lead to lower temperatures and higher densities (Uehara & Inutsuka 2000).

3.4. Accretion Physics

How massive were the first stars? Star formation typically proceeds from the inside-out through the accretion of gas onto a central hydrostatic core. Whereas the initial mass of the hydrostatic core is very similar for primordial and present-day
star formation (see above), the accretion process—ultimately responsible for setting the final stellar mass—is expected to be rather different. On dimensional grounds, the accretion rate is simply related to the sound speed cubed over Newton’s constant (or equivalently given by the ratio of the Jeans mass and the free-fall time): 

\[ \dot{M}_{\text{acc}} \sim \frac{c^3}{G} \propto T^{3/2}. \]

A simple comparison of the temperatures in present-day star-forming regions \((T \sim 10\text{ K})\) with those in primordial ones \((T \sim 200–300\text{ K})\) already indicates a difference in the accretion rate of more than two orders of magnitude.

Extending earlier work by Stahler et al. (1986), Omukai & Palla (2001, 2003) have investigated the accretion problem in considerable detail, going beyond the simple dimensional argument given above. Their computational technique approximates the time evolution by considering a sequence of steady-state accretion flows onto a growing hydrostatic core. Somewhat counterintuitively, these authors identify a critical accretion rate, \(\dot{M}_{\text{crit}} \sim 4 \times 10^{-3} M_\odot \text{ yr}^{-1}\), such that for accretion rates higher than this, the protostar cannot grow to masses much in excess of a few tens of solar masses. For smaller rates, however, the accretion is predicted to proceed all the way up to \(\sim 600 M_\odot\), i.e., on the order of the host clump.

The physical basis for the critical accretion rate is that for ongoing accretion onto the core, the luminosity must not exceed the Eddington value, \(L_{\text{EDD}}\). In the early stages of accretion, before the onset of hydrogen burning, the luminosity is approximately given by \(L_{\text{tot}} \sim L_{\text{acc}} \simeq GM_\ast \dot{M}_{\text{acc}} / R_\ast\). By demanding \(L_{\text{acc}} \simeq L_{\text{EDD}}\) it follows

\[ \dot{M}_{\text{crit}} \simeq \frac{L_{\text{EDD}} R_\ast}{GM_\ast} \sim 5 \times 10^{-3} M_\odot \text{ year}^{-1}, \tag{5} \]

where \(R_\ast \sim 5 R_\odot\), a typical value for a Population III main-sequence star (e.g., Bromm et al. 2001b). In Figure 5 (from Omukai & Palla 2003), the mass-radius relation is shown for various values of the accretion rate. The dramatic swelling in radius effectively shuts off accretion at \(M_\ast \lesssim 100 M_\odot\), when the accretion rate exceeds \(\dot{M}_{\text{crit}}\).

Realistic accretion flows are expected to have a time-dependent rate, and the outcome will thus depend on whether the accretion rate will decline rapidly enough to avoid exceeding the Eddington luminosity at some stage during the evolution. The biggest caveat concerning the Omukai & Palla (2003) results seems to be the issue of geometry. A three-dimensional accretion flow of gas with some residual degree of angular momentum will deviate from spherical symmetry and instead form a disk. It is then conceivable that most of the photons can escape along the axes, whereas mass can flow in unimpeded through the accretion disk (see Tan & McKee 2004).

Recently, Bromm & Loeb (2003b, 2004) have used the SPH particle-splitting technique to study the three-dimensional accretion flow around a primordial protostar. Whereas Bromm et al. (1999, 2002) created sink particles already at \(n \simeq 10^8 \text{ cm}^{-3}\), briefly before three-body reactions would convert the gas into
Figure 5  Evolution of accreting metal-free protostar. Shown is the radius-mass relation for different values of the accretion rate (increasing from bottom to top). Accretion is effectively shut off for the cases with $\dot{M} \gtrsim \dot{M}_{\text{crit}}$ because of the dramatic increase in radius. (From Omukai & Palla 2003.)

fully molecular form, the gas is now allowed to reach densities of $10^{12}$ cm$^{-3}$ before being incorporated into a central sink particle. Bromm & Loeb (2004) studied how the molecular core grows in mass over the first $\sim 10^4$ years after its formation. The accretion rate is initially very high, $\dot{M}_{\text{acc}} \sim 0.1 M_\odot$ year$^{-1}$, and subsequently declines in time in a complex fashion. Expressed in terms of the sound speed in Population III prestellar cores, this initial rate is $\dot{M}_{\text{acc}} \sim 25c_s^3/G$. Therefore, as initial accretion rates of a few tens times $c_s^3/G$ are commonly encountered in
simulations of present-day star formation, the Population III case might again be an example of a very generic type of behavior for collapse and accretion (see Larson 2003).

The mass of the molecular core, taken as an estimator of the protostellar mass, grows approximately as $M_\ast \sim \int \dot{M}_{\text{accd}} \, dt \propto t^{0.75}$, for $t < 10^3$ years, and as $M_\ast \propto t^{0.4}$ afterward. The early time accretion behavior is similar to the power-law scalings found in one-dimensional, spherically symmetric simulations (Omukai & Nishi 1998, Ripamonti et al. 2002). The complex accretion history encountered in the simulation of Bromm & Loeb (2004), however, cannot be accommodated with a single power-law. Such a multiple power-law behavior has also been inferred in other studies (Abel et al. 2002, Omukai & Palla 2003). This earlier inference, however, was indirect in that it did not follow the actual accretion flow but instead estimated the accretion rate from the instantaneous density and velocity profiles at the termination of the three-dimensional simulation of Abel et al. (2002). In the simulation of Bromm & Loeb (2004), the accretion rate quickly drops, after only $\sim 3000$ years, below $\dot{M}_{\text{crit}}$, at which point the stellar mass is $M_\ast \approx 30 M_\odot$. The accretion rate thus becomes subcritical early on, at which time the protostar still undergoes Kelvin-Helmholtz contraction (the descending portion of the curves in Figure 5). The dramatic expansion in radius, which according to Omukai & Palla (2003) would shut off further accretion, could therefore be avoided. A conservative upper limit for the final mass of the star is then $M_\ast (t = 3 \times 10^6$ years) $\sim 500 M_\odot$. This upper bound has been derived by assuming that accretion cannot go on for longer than the total lifetime of a very massive star (VMS), which is almost independent of stellar mass (e.g., Bond et al. 1984).

Can a Population III star ever reach this asymptotic mass limit? The answer to this question is not yet known with any certainty, and it depends on whether the accretion from the dust-free envelope is eventually terminated by feedback from the star (e.g., Omukai & Palla 2001, 2003; Ripamonti et al. 2002; Omukai & Inutsuka 2002; Tan & McKee 2004). The standard mechanism by which accretion may be terminated in metal-rich gas, namely radiation pressure on dust grains (Wolfire & Cassinelli 1987), is evidently not effective for gas with a primordial composition. Recently, it has been speculated that accretion could instead be turned off through the formation of an H II region (Omukai & Inutsuka 2002) or through the radiation pressure exerted by trapped Ly$\alpha$ photons (Tan & McKee 2004). The termination of the accretion process defines the current unsolved frontier in studies of Population III star formation.

3.5. The Second Generation of Stars: Critical Metallicity

How and when did the transition take place from the early formation of massive stars to that of low-mass stars at later times? The very first stars, marking the cosmic Renaissance of structure formation, formed under conditions that were much simpler than the highly complex environment in present-day molecular clouds. Subsequently, however, the situation rapidly became more complicated, again due
to the feedback from the first stars on the IGM, owing to the production of photons and of heavy elements (see Section 4).

In contrast to the formation mode of massive stars (Population III) at high redshifts, fragmentation is observed to favor stars below a solar mass (Population I and II) in the present-day universe. The transition between these fundamental modes is mainly expected to be driven by the progressive enrichment of the cosmic gas with heavy elements (see Section 4.2). This enables the gas to cool to lower temperatures. The concept of a critical metallicity, $Z_{\text{crit}}$, has been used to characterize the transition between Population III and Population II formation modes, where $Z$ denotes the mass fraction contributed by all heavy elements (Omukai 2000; Bromm et al. 2001a; Schneider et al. 2002a, 2003a; Mackey et al. 2003). Published studies have only constrained this important parameter to within a few orders of magnitude, $Z_{\text{crit}} \sim 10^{-6}$–$10^{-3} Z_\odot$, under the implicit assumption of solar relative abundances of metals. This assumption is likely to be violated by the metal yields of the first SNe at high redshifts, for which strong deviations from solar abundance ratios are predicted (e.g., Heger & Woosley 2002; Qian & Wasserburg 2002; Qian et al. 2002; Umeda & Nomoto 2002, 2003; Sneden & Cowan 2003).

The cooling rate of the metals depends on their ionization state, which is controlled by the ionizing backgrounds (UV and X-ray photons or cosmic rays) and which is still not well known (see Section 4.1).

Recently, Bromm & Loeb (2003c) have shown that the transition between the above star formation modes is driven primarily by fine-structure line cooling of singly ionized carbon or neutral atomic oxygen. Earlier estimates of $Z_{\text{crit}}$, which did not explicitly distinguish between different coolants, are refined by introducing separate critical abundances for carbon and oxygen, $[\text{C/H}]_{\text{crit}}$ and $[\text{O/H}]_{\text{crit}}$, respectively, where $[A/H] = \log_{10}(N_A/N_H) - \log_{10}(N_A/N_H)_\odot$, and a subscript $\odot$ denotes solar values. Because C and O are also the most important coolants throughout most of the cool atomic interstellar medium (ISM) in present-day galaxies, it is not implausible that these species might be responsible for the global shift in the star formation mode. Indeed, under the temperature and density conditions that characterize Population III star formation, the most important coolants are O I and C II, whose fine-structure lines dominate over all other metal transitions (Hollenbach & McKee 1989). Cooling owing to molecules becomes important only at lower temperatures, and cooling owing to dust grains only at higher densities (e.g., Omukai 2000, Schneider et al. 2003a). The presence of dust is likely to modify the equation of state at these high densities in important ways (Schneider et al. 2003a), and it will be interesting to explore its role in future collapse calculations. The physical nature of the dust, however, that is produced by the first SNe is currently still rather uncertain (e.g., Loeb & Haiman 1997, Todini & Ferrara 2001, Nozawa et al. 2003, Schneider et al. 2003b).

A strong UV flux just below the Lyman limit ($h\nu < 13.6$ eV) is predicted to be emitted by the same stars that are responsible for the reionization of the IGM (see Section 4.1). This soft UV radiation can penetrate the neutral IGM and ionize any trace amount of neutral carbon owing to its low first-ionization potential of...
11.26 eV. Because the abundance of carbon is so low, the UV background can ionize carbon throughout the universe well before hydrogen reionization. Oxygen, however, will predominantly be neutral prior to reionization because its ionization potential is 13.62 eV. Cooling is mediated by excitations owing to collisions of the respective metal with free electrons or hydrogen atoms. At the low fractional abundances of electrons, $x_e \lesssim 10^{-4}$, expected in the neutral (rapidly recombining) gas at $z \sim 15$, collisions with hydrogen atoms dominate. This renders the analysis independent of the very uncertain hydrogen-ionizing backgrounds at high redshifts (cosmic rays or soft X-rays).

To derive the critical C and O abundances, Bromm & Loeb (2003c) start with the characteristic state reached in primordial gas that cools only through molecular hydrogen (Section 3.2). For the gas to fragment further, additional cooling owing to C II or O I is required. Fragmentation requires that the radiative cooling rate be higher than the free-fall compressional heating rate. The critical metal abundances can thus be found by equating the two rates: $\Lambda_\text{CII,OI}(n, T) \simeq 1.5nk_B T/t_H$, where $k_B$ is Boltzmann’s constant. The critical C and O abundances are found by setting $n \sim n_c$ and $T \sim T_c$, resulting in $[\text{C}/\text{H}]_\text{crit} \simeq -3.5 \pm 0.1$ and $[\text{O}/\text{H}]_\text{crit} \simeq -3.05 \pm 0.2$. Strictly speaking, these threshold levels are the required abundances in the gas phase.

Even if sufficient C or O atoms are present to further cool the gas, there will be a minimum attainable temperature that is set by the interaction of the atoms with the thermal CMB: $T_{\text{CMB}} = 2.7 \, \text{K}(1 + z)$ (e.g., Larson 1998, Clarke & Bromm 2003). At $z \sim 15$, this results in a characteristic stellar mass of $M_* \sim 20 \, M_\odot/(n_f/10^4 \, \text{cm}^{-3})^{-1/2}$, where $n_f > 10^4 \, \text{cm}^{-3}$ is the density at which opacity prevents further fragmentation (e.g., Rees 1976). It is possible that the transition from the high-mass to the low-mass star formation mode was modulated by the CMB temperature and was therefore gradual, involving intermediate-mass (Population II.5) stars at intermediate redshifts (Mackey et al. 2003). This transitional population could give rise to the faint SNe that have been proposed to explain the observed abundance patterns in metal-poor stars (Umeda & Nomoto 2002, 2003).

When and how uniformly the transition in the cosmic star formation mode took place was governed by the detailed enrichment history of the IGM. This, in turn, was determined by the hydrodynamical transport and mixing of metals from the first SN explosions. We discuss the SN-driven dispersal of heavy elements in Section 4.2.

4. FEEDBACK EFFECTS ON THE IGM

4.1. Radiative Feedback: The Suicidal Nature of the First Stars

The radiation produced by Population III star formation will influence the subsequent thermal history of the IGM and will modify the properties of star-forming gas. This radiative feedback may occur in a variety of ways that depend on the
energy range of the stellar photons. Molecular hydrogen is the main coolant in low-
temperature, metal-free gas. It enables the formation of the first stars at $z \simeq 20$–30. We therefore first focus on the radiative effects that are able to influence the H$_2$ chemistry. This feedback could either be negative, if it is due to soft UV photons, or positive, if it is due to X-rays.

We begin by discussing negative feedback. Molecular hydrogen is fragile and can readily be destroyed by photons in the Lyman-Werner (LW) bands, within the energy range $11.2$–$13.6$ eV, via the two-step Solomon process (Stecher & Williams 1967)

$$H_2 + \gamma \rightarrow H^*_2 \rightarrow 2H.$$ (6)

The intermediate stage involves an excited electronic state, H$_2^*$, from which a fraction of the subsequent decays end in the vibrational continuum of the ground state, resulting in the dissociation of the molecule (e.g., Glover & Brand 2001). The question arises whether H$_2$ cooling can be suppressed in halos that virialize after the first stars have formed and built up a background of LW photons (e.g., Haiman et al. 1997). These photons have energies just below the Lyman limit and so can easily penetrate a still-neutral IGM prior to reionization. These second-generation halos are typically more massive compared to the $\sim 10^5$–$10^6$ M$_\odot$ systems that host the formation of the first stars at $z \gtrsim 20$. The gas might then be able to self-shield against the photo-dissociating LW background (e.g., Glover & Brand 2001, Kitayama et al. 2001, Machacek et al. 2001). The effect of self-shielding is often taken into account, both in simulations and in analytical work, by writing the H$_2$ photodissociation rate as $k_{\text{diss}} \propto J_{21} f_{\text{shield}}$, with a proportionality constant that depends on the spectrum of the background radiation. Here, $J_{21}$ measures the flux at the Lyman limit in the customary units of $10^{-21}$ ergs s$^{-1}$ cm$^{-2}$ Hz$^{-1}$ sr$^{-1}$. For the shielding factor, the following approximate expression is usually used:

$$f_{\text{shield}} \simeq \min[1, (N_{H_2}/10^{14} \text{ cm}^{-2})^{-0.75}]$$ (Draine & Bertoldi 1996). This formula is accurate only for a static medium, and it will grossly overestimate the H$_2$ line opacity in the presence of large-scale velocity gradients. In cases with strong bulk flows, the effect of self-shielding is conservatively overestimated.

The overall normalization of the LW background and its evolution with redshift are still rather uncertain. Close to the epoch of reionization, however, a significant flux in the LW bands ($h
u < 13.6$ eV) is expected (e.g., Bromm & Loeb 2003a). The flux in the LW bands just below the Lyman limit, $J_{21}^+$, could be much larger than that just above, $J_{21}^-$. Assuming that only a fraction, $f_{\text{esc}}$, of the ionizing photons can escape from the star-forming halos, one has $J_{21}^+ \simeq J_{21}^- / f_{\text{esc}}$. This could be quite large because $f_{\text{esc}}$ is expected to be low at high redshifts (Wood & Loeb 2000, and references therein). Alternatively, a strong background of photo-dissociating photons could also arise internally from star formation in an early dwarf galaxy itself (e.g., Omukai & Nishi 1999, Oh & Haiman 2002).

The strong UV background flux estimated above makes it possible for H$_2$ formation to be effectively suppressed close to the redshift of reionization. In the absence of molecular hydrogen, however, cooling can still proceed via atomic
transitions in halos of mass (see Barkana & Loeb 2001)

\[ M \gtrsim 10^8 M_\odot \left( \frac{1 + z}{10} \right)^{-3/2}. \]  

(7)

The virial temperature, \( T_{\text{vir}} \sim 10^4 \text{ K} \), in these more massive halos allows for the very efficient cooling of the gas via lines of atomic hydrogen (e.g., Madau et al. 2001, Bromm & Clarke 2002). In cases where the gas temperature is close to the virial temperature, the gas cloud as a whole can undergo collapse but it will not be able to fragment until high-enough densities are reached so that the Jeans mass has declined sufficiently (Oh & Haiman 2002, Bromm & Loeb 2003a). Recent numerical simulations of the collapse of a dwarf galaxy at \( z \approx 10 \), massive enough for atomic H cooling to operate but where cooling owing to \( \text{H}_2 \) is effectively suppressed by a strong LW background, have shown that very massive (\( \sim 10^6 M_\odot \)), compact (radii \( \lesssim 1 \text{ pc} \)) gas clouds form in the center of the DM potential well (Bromm & Loeb 2003a). These clouds may be the immediate progenitors of supermassive black holes that could seed high-redshift quasar activity.

In contrast to this negative feedback on \( \text{H}_2 \), opposing positive feedbacks have been proposed. As discussed in Section 2, \( \text{H}_2 \) formation is primarily facilitated by free electrons. Any process that temporarily enhances their abundance, therefore, will also tend to increase the \( \text{H}_2 \) fraction. Various mechanisms have been suggested. First, X-ray photons from SN remnants (e.g., Oh 2001, Cen 2003a) or the accretion onto black holes could ionize hydrogen in dense regions, enabling the reformation of \( \text{H}_2 \) (Glover & Brand 2003, Machacek et al. 2003). Second, the free electrons in relic H II regions (Oh & Haiman 2003), or inside the outer boundary of a still-active one (Ricotti et al. 2001, 2002a,b), may accomplish the same. Finally, the collisional ionization in shock waves, and the subsequent nonequilibrium cooling and molecule reformation has been discussed (e.g., Mac Low & Shull 1986, Shapiro & Kang 1987, Ferrara 1998, Bromm et al. 2003). The last mechanism evidently is not strictly radiative in nature, but it seems appropriate to include it here. In summary, conclusions on the overall sign of the radiative feedback on the \( \text{H}_2 \) chemistry are still very uncertain. To reach more robust results, sophisticated cosmological simulations are required, treating the build-up of the radiation backgrounds and their influence on the overall star formation rate in a self-consistent manner. Such challenging simulations are currently still beyond our capabilities.

A qualitatively different feedback is photoheating owing to radiation with energies high enough to ionize hydrogen atoms (see Barkana & Loeb 2001 for a comprehensive discussion). Because photoionization-heating raises the gas temperature to \( \sim 10^4 \text{ K} \), this gas is then evaporated out of the high-redshift potential wells with virial temperatures \( T_{\text{vir}} < 10^4 \text{ K} \). Star formation is thus temporarily shut off. This photoevaporation feedback could be due to sources in the halo itself (e.g., Bromm et al. 2003, Oh & Haiman 2003, Whalen et al. 2003) or to an external ionizing background (e.g., Barkana & Loeb 1999, Susa & Umemura 2000, Kitayama et al. 2001, Dijkstra et al. 2004, Shapiro et al. 2004, Tassis et al. 2003). External feedback is likely to become important only at \( z \sim 6 \), where the universe is close
to complete reionization; in contrast, internal feedback could operate already at much higher redshifts.

4.2. Chemical Feedback: First Supernovae and Early Metal Enrichment

The crucial transition from a smooth, homogeneous universe to an increasingly complex and structured one is marked by the death of the first stars. The SN explosions at the end of the initial burst of Population III star formation disperse the first elements into the hitherto pristine IGM. How did this initial metal enrichment proceed? To account for the widespread presence of metals in the Ly\(\alpha\) forest at \(z \sim 4-5\) (e.g., Songaila 2001, Schaye et al. 2003), star formation in low-mass systems at \(z \gtrsim 10\) has been proposed (e.g., Madau et al. 2001, Mori et al. 2002, Wada & Venkatesan 2003). The metals produced in these low-mass halos can more easily escape from their shallow potential wells than those at lower redshift (e.g., Aguirre et al. 2001a,b). In addition, the enriched gas has to travel much shorter distances between neighboring halos at these early times, and it might therefore have been easier to establish a uniform metal distribution in the IGM.

The important question arises: How did the first stars die? The answer to this question sensitively depends on the precise mass of a Population III star. In particular, if the star has a mass in the narrow interval \(140 M_\odot \lesssim M_* \lesssim 260 M_\odot\), it will explode as a PISN, leading to the complete disruption of the progenitor (e.g., Fryer et al. 2001, Heger et al. 2003). Population III stars with masses below or above the PISN range are predicted to form black holes. This latter fate is not accompanied by a significant dispersal of heavy elements into the IGM because most of the newly synthesized metals will be locked up in the black hole. The PISN, however, will contribute all its heavy element production to the surrounding gas.

As we have discussed in Section 3.5, the IGM metal enrichment history is crucial for understanding the detailed transition in the star formation mode from high-mass to low-mass dominated. If this enrichment is very uniform, the transition would occur rather suddenly. If, on the other hand, enrichment is very patchy, with islands of high-metallicity gas embedded in mostly still pristine material, then the transition would occur in a nonsynchronized way, probably occupying a considerable time interval (e.g., Scannapieco et al. 2003).

Recently, Bromm et al. (2003) have presented numerical simulations of the first SN explosions at high redshifts (\(z \sim 20\)). In contrast to earlier work, both analytical (e.g., Larson 1974, Dekel & Silk 1986, Scannapieco et al. 2002, Furlanetto & Loeb 2003) and numerical (e.g., Mori et al. 2002, Thacker et al. 2002, Wada & Venkatesan 2003), their focus is on the minihalos that are the sites for the formation of the very first stars. These halos, with masses of \(M \sim 10^5-10^6 M_\odot\) and collapse redshifts of \(z \gtrsim 20\) are the sites for the formation of the truly first stars. It is not obvious, however, whether star formation in more massive systems would not already be significantly altered by the activity of previous generations of stars. In particular, PISN explosions may only have occurred in the minihalos mentioned above.
Bromm et al. (2003) assume that there is one single Population III star in the center of the minihalo and that this star is massive enough to explode as a PISN. To span the plausible energy range, explosion energies of $E_{SN} = 10^{51}$ and $10^{53}$ ergs are considered, corresponding to stars with masses $M_\ast \simeq 140$ and 260 $M_\odot$, respectively (Fryer et al. 2001). The latter case marks the upper mass limit of the PISN regime. The explosion energy is inserted as thermal energy, such that the explosion is initialized with conditions appropriate for the adiabatic Sedov-Taylor (ST) phase. Because the PISN is completely disrupted without leaving a remnant behind, it is possible to trace the subsequent fate of the metals by using the SPH particles that represent the stellar ejecta as markers.

Initially, the blast wave evolves into a roughly uniform medium at radii $r \lesssim R_{\text{core}} \sim 20$ pc, resulting in the usual ST scaling: $R_{sh} \propto t^{0.4}$. Once the blast wave reaches beyond the core, however, it encounters an isothermal density profile in the remainder of the halo, leading to the scaling (e.g., Ostriker & McKee 1988): $R_{sh} \simeq 30$ pc$(E_{SN}/10^{53}$ ergs)$^{1/3}$(t/10$^5$ year)$^{2/3}$. A few million years after the explosion, radiative (inverse Compton) losses become important, and the SN remnant enters its final, snowplow phase. The significance of inverse Compton cooling distinguishes very-high-$z$ SN explosions from those occurring in the present-day universe.

After approximately $10^5$ years, when $t_{\text{cool}} \lesssim R_{sh}/u_{sh}$, a dense shell begins to form at a radius $\sim 50$ pc. The thermodynamic properties of the dense shell, the interior bubble, and the surrounding medium are summarized in Figure 6. The shocked, swept-up gas exhibits three distinct thermal phases, as can clearly be seen in Figure 6. One phase is at $T \gtrsim 10^5$ K, the second is at $T \sim 10^4$ K, and the third is at $T \lesssim 10^3$ K. The latter two phases correspond to the dense shell. The cooling from very high temperatures to $\sim 10^5$ K and subsequently to $10^2$ K proceeds in nonequilibrium, such that a fraction of free electrons persists below $\sim 8000$ K, allowing the reformation of H$_2$ (e.g., Mac Low & Shull 1986, Shapiro & Kang 1987, Oh & Haiman 2002). The molecular fraction in the densest regions asymptotically assumes a plateau value of $f_{H_2} \sim 3 \times 10^{-3}$. Inside the expanding SN remnant lies a hot pressurized bubble (the grey symbols in Figure 6) that corresponds to the original stellar ejecta. This bubble drives the outward motion, and its gas is slowly cooled by adiabatic expansion and inverse Compton losses.

In Figure 7, the projected gas density is shown $\sim 10^6$ years after the explosion for explosion energy $E_{SN} = 10^{53}$ ergs. The blast wave has succeeded in completely disrupting the minihalo, dispersing most of the halo gas into the IGM. Comparing $E_{SN}$ with the binding energy of the minihalo, $E_{\text{grav}} \sim 10^{51}$ ergs, such an outcome is clearly expected. It depends, however, on the inefficient radiative processes that cool the hot bubble gas in the initial stages of expansion.

The second prominent feature in Figure 7 is the vigorous fragmentation of the dense shell into a large number of small cloudlets. The emergence of these cloudlets, corresponding to gas at $T \lesssim 10^3$ K, is not driven by gravity (e.g., Elmegreen 1994, and references therein), but is instead owing to a thermal instability triggered by the onset of atomic cooling. The explosions simulated by Bromm et al. (2003) do not result in the formation of lower-mass stars, or Population II.5
Figure 6  Thermodynamic properties of the shocked gas $\sim 10^5$ years after the explosion of a PISN. Gas temperature (in K) versus log $n$ (in cm$^{-3}$). **Dashed line:** The virial temperature of the minihalo. It is evident that $T_{\text{vir}} \sim 3000$ K is much lower than the gas temperature in the minihalo. Most of the gas will therefore be expelled from the halo on a dynamical timescale. **Dotted line:** Adiabatic behavior. The gas in the outer reaches of the minihalo, as well as in the general IGM, approximately follows this scaling. **Grey symbols:** Location of the gas that makes up the original stellar ejecta. This gas is hot and diffuse, can consequently cool only slowly, and therefore provides the pressure source that drives the expansion of the bubble. Notice that a fraction of the gas has been able to cool to $\sim 200$ K due to the action of molecular hydrogen. (From Bromm et al. 2003.)

stars in the terminology of Mackey et al. (2003). This is consistent with the prediction in Mackey et al. (2003) that Population II.5 stars can only form in DM halos massive enough to be able to cool via atomic hydrogen (see also Salvaterra et al. 2003). To further test the possibility of SN-triggered star formation in the high-redshift universe, it will be necessary to explore a range of cosmological environments corresponding to different halo masses and collapse redshifts.

What is the fate of the metals that are produced in the PISN progenitor? PISNe are predicted to have substantial metal yields, on the order of $y = M_Z/M_\star \sim$...
0.5, and for the largest stellar masses in the PISN range, most of $M_Z$ is made up of iron (Heger & Woosley 2002). Bromm et al. (2003) find that for $E_{SN} = 10^{53}$ ergs, $\sim 90\%$ of the metals have escaped from the DM minihalo $4 \times 10^8$ years after the explosion. The metals have filled most of the interior hot bubble (see inset of Figure 7), and there has not yet been sufficient time for them to significantly mix into the dense surrounding shell. A rough estimate of the resulting metallicity in the surrounding contaminated IGM can be obtained as follows: $Z = M_Z / M_{gas} \sim 100 M_\odot / 10^5 M_\odot \gtrsim 10^{-2} Z_\odot$. This value is well above the critical metallicity threshold, $Z_{crit} \sim 10^{-3} Z_\odot$, for enabling the formation of lower-mass stars (see Section 3.5). The conclusion is that Population III stars can continue to form in the pristine gas within the neighboring halos, as the metals that are dispersed in the explosion do not reach them.

Whereas a single SN explosion might be able to evacuate most of the gas from a minihalo, the situation could be quite different for multiple SN explosions in early dwarf galaxies of mass $\sim 10^8 M_\odot$ (Mori et al. 2002, Wada & Venkatesan 2003). In this case, the simulations indicate that off-nuclear SN explosions drive inward-propagating blast waves that act to assemble gas in the central regions of the host galaxy. The gas in these galaxies may thus be able to survive multiple SN explosions, and star formation would not be significantly suppressed owing to the mechanical SN feedback. In summary, it appears that the effect of SN events on star formation in early galaxies and on the chemical and thermal evolution of the IGM depends sensitively on the specific environment.

For the PISN explosion studied by Bromm et al. (2003), the extent of the metal-enriched region with a physical size of $\sim 1$ kpc is comparable to the radius of the relic H II region around the minihalo. In a related paper (Yoshida et al. 2004), it is argued that if Population III stars have led to an early partial reionization of the universe, as may be required by the recent WMAP results (see Section 5.1), this will have resulted in a nearly uniform enrichment of the universe to a level $Z_{min} \gtrsim 10^{-4} Z_\odot$ already at $z \gtrsim 15$. It would indeed be a remarkable feature of the universe if the first stars had endowed the IGM with such a widespread, near-universal level of early enrichment (see also Oh et al. 2001). An interesting implication could be the observability of unsaturated metal absorption lines at $z \gtrsim 6$, which would probe the neutral fraction of the IGM during the epoch of reionization (Oh 2002).

We end this section by emphasizing that we are only beginning to understand the complex processes that distributed the first heavy elements into the IGM, and more sophisticated numerical simulations are required for further progress.

5. OBSERVATIONAL SIGNATURE

An increasing variety of observational probes of the first stars has been suggested (e.g., Haiman & Loeb 1997, Oh et al. 2003, Stiavelli et al. 2004). Below, we focus on three of them, and here only briefly mention some of the others (see Barkana
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& Loeb 2001 for a comprehensive discussion). Intriguing possibilities would arise if the Population III IMF were sufficiently top-heavy to enable the formation of massive black holes (e.g., Madau & Rees 2001, Islam et al. 2003, Volonteri et al. 2003). Possible consequences might include backgrounds of gravitational waves (Schneider et al. 2000, de Araujo et al. 2002) and diffuse neutrinos (Schneider et al. 2002b). In the latter case, the high-energy (TeV) neutrinos might originate in the relativistic jets that are associated with gamma-ray bursts (GRBs), which are believed to accompany the birth of a black hole (see Section 5.3).

The integrated light emitted during the lifetime of Population III stars is predicted (Bond et al. 1986, Santos et al. 2002, Salvaterra & Ferrara 2003) to contribute significantly to the locally observed cosmic near-infrared background (e.g., Hauser & Dwek 2001). A related signature is the Population III contribution to the background anisotropy (Magliocchetti et al. 2003, Cooray et al. 2004). Finally, 21-cm radiation from neutral hydrogen, both in emission and absorption, could provide a unique probe of the conditions in the early minihalos, thus testing our assumptions on the initial conditions for Population III star formation (e.g., Madau et al. 1997; Tozzi et al. 2000; Carilli et al. 2002; Furlanetto & Loeb 2002; Iliev et al. 2002, 2003; Ciardi & Madau 2003). However, in practice, these observations may be extremely challenging owing to the strong foreground contamination (Di Matteo et al. 2002).

In the following section, we discuss three empirical probes of the first stars in somewhat greater detail, as they have already provided us with constraints on the nature of the first stars, or promise soon to do so.

5.1. Reionization Signature from the First Stars

The WMAP satellite has recently measured, from the CMB polarization anisotropies (Kaplinghat et al. 2003), the total optical depth to Thomson scattering: \(\tau_e = 0.17 \pm 0.04\) (Kogut et al. 2003, Spergel et al. 2003). Such a high value is surprising. We know that the IGM was completely ionized again at redshifts \(z \lesssim 6\) from the absence of Gunn-Peterson troughs in high-redshift Sloan Digital Sky Survey (SDSS) quasars (e.g., Fan et al. 2003). Scattering from free electrons between \(z \sim 0–6\) only contributes \(\tau_e \simeq 0.05\). The observed excess must have arisen from the scattering of CMB photons off free electrons ionized by star formation at higher redshifts. Normal stellar populations (characterized by a standard IMF, or at most a modestly top-heavy one with characteristic mass \(M_\star \sim 5 \, M_\odot\)) could have successfully reproduced the measured high optical depth if reionization had occurred already at \(z \sim 15\) (Ciardi et al. 2003).

Such a solution, however, runs into difficulties when two other empirical constraints are taken into account. The first one considers the thermal history of the postreionization IGM (e.g., Theuns et al. 2002, Hui & Haiman 2003). After reionization is completed, the IGM continues to be heated by photoionization. This heating, however, cannot compete with the cooling owing to adiabatic Hubble expansion. In consequence, the earlier reionization occurred, the lower the IGM
temperature at a given fixed redshift. Observations at $z \sim 3$ indicate that the last complete overlap of ionizing bubbles (i.e., the last time the IGM was completely ionized) could not have occurred before a redshift $z \sim 9$. The second constraint, which is difficult to accommodate within the model of Ciardi et al. (2003), is the detection of select SDSS quasars at $z \gtrsim 6$ with Gunn-Peterson absorption in their vicinity. It is not easy to see how islands of neutral gas could have persisted down to $z \sim 6$ if the IGM had already been completely reionized at $z \sim 15$.

To simultaneously account for all the available observational constraints thus poses a nontrivial challenge to theory. It has been suggested that an early generation of very massive Population III stars, as predicted by numerical simulations (see Section 3), could naturally allow for a solution (Cen 2003a,b; Haiman & Holder 2003; Somerville & Livio 2003; Wyithe & Loeb 2003a,b). The high efficiency of producing ionizing photons per stellar baryon for very massive Population III stars (e.g., Tumlinson & Shull 2000; Bromm et al. 2001b; Schaerer 2002, 2003) can lead to an early first episode of at least partial reionization at $z \sim 15$, thus ensuring a sufficiently large optical depth to Thomson scattering. As we discussed in Section 4, Population III star formation was self-limiting owing to the effect of radiation and the dispersal of heavy elements. After the era of Population III star formation at $z \gtrsim 15$, the IGM was able to recombine again owing to the temporary lull in the production of ionizing photons. Eventually, normal (Population II) stars form in more massive (dwarf-sized) systems, and lead to the final, complete reionization of the universe at $z \sim 7$. In this case, there is no conflict with the empirical constraints outlined above. In Figure 8, a sample reionization history is shown that is representative for the double-reionization models (from Wyithe & Loeb 2003b). At present, the error bars in the WMAP determination of $\tau_\nu$ are still too large to firmly establish the need for very massive Population III stars to have formed in the high-redshift universe. By the end of its mission, however, the error on $\tau_\nu$ is estimated to have gone down to $\pm 0.01$. If the high current value were to persist, the evidence for a top-heavy IMF in primordial star formation would have been considerably strengthened.

Cosmological models with reduced small-scale power (see Section 2) cannot easily be reconciled with a high value of $\tau_\nu$ (Somerville et al. 2003; Yoshida et al. 2003b,c). To compensate for the missing contribution from minihalos, one would have to invoke an extremely high ionizing photon production rate in galaxies at $z \gtrsim 6$. This could, in principle, be achieved by maintaining a top-heavy IMF over a long period, $6 \lesssim z \lesssim 20$. The problem with such a scenario is the severe overproduction of metals. These would have to be hidden to an improbable degree so that the formation of massive Population III stars were not terminated too early (Yoshida et al. 2004). The study of the first stars thus has the exciting potential to provide astrophysical constraints on the properties of DM particles because these properties are reflected in the nature of the density fluctuations at small spatial scales.
Figure 8  Sample history of reionization. Shown are the volume filling factors (Q) of ionized regions as a function of redshift. For hydrogen (solid line), a complex evolution is evident, with an early (partial) reionization at $z \sim 15$ owing to massive Population III stars. This mode of star formation is self-terminating, such that the second (complete) reionization at $z \sim 9$ is due to normal Population II stars. Also shown is the hypothetical case where He ionization is ignored (light lines), as well as the predicted histories for He$^+$ and He$^{++}$ reionization. (Adapted from Wyithe & Loeb 2003b.)

5.2. Stellar Archaeology: Relics from the End of the Dark Ages

It has long been realized that the most metal-poor stars found in our cosmic neighborhood would encode the signature from the first stars within their elemental abundance pattern (e.g., Bond 1981, Beers et al. 1992). For many decades, however, the observational search has failed to discover a truly first-generation star with zero metallicity. Indeed, there seemed to have been an observational lower limit of $[\text{Fe/H}] \sim -4$ (e.g., Carr 1987, Oey 2003). In view of the recent theoretical prediction that most Population III stars were very massive, with associated lifetimes of $\sim 10^6$ years, the failure to find any living Population III star in the Galaxy is not surprising, as they all would have died a long time ago (e.g., Hernandez & Ferrara 2001). Furthermore, theory has predicted that star formation out of extremely low-metallicity gas, with $Z \lesssim Z_{\text{crit}} \sim 10^{-3.5} Z_{\odot}$ (see Section 3.5), would be essentially equivalent to that out of truly primordial gas. Again, this theoretical prediction was in accordance with the apparent observed lower-metallicity cutoff.

Recently, however, this simple picture has been challenged by the discovery of the star HE0107-5240 with a mass of $0.8 M_{\odot}$ and an iron abundance of $[\text{Fe/H}] = -5.3$ (Christlieb et al. 2002). This finding indicates that at least some low mass stars could have formed out of extremely low-metallicity gas. Does the existence of this star invalidate the theory of a metallicity threshold for enabling low-mass star formation? As pointed out by Umeda & Nomoto (2003), a possible explanation
Figure 9  Observed abundances in low-metallicity galactic halo stars. For carbon (upper panel) and oxygen (lower panel), filled circles correspond to samples of dwarf and subgiant stars (from Akerman et al. 2003), and open squares correspond to a sample of giant stars (from Cayrel et al. 2004). The dashed lines indicate the predicted critical carbon and oxygen abundances (see Section 3.5). The cross is the location of the extremely iron-poor giant star HE0107-5240. (Adapted from Bromm & Loeb 2003c.)

could lie in the unusually high abundances of carbon and oxygen in HE0107-5240. As discussed in Section 3.5, Bromm & Loeb (2003c) have demonstrated that indeed carbon and oxygen may have been the main drivers for the Population III to II transition.

In Figure 9, we compare the theoretical thresholds derived by Bromm & Loeb (2003c) to the observed carbon and oxygen abundances in metal-poor dwarf (Akerman et al. 2003) and giant (Cayrel et al. 2004) stars in the halo of our Galaxy. All data points lie above the critical oxygen abundance, but a few cases lie below the critical carbon threshold. All these low-mass stars are consistent with the model because the corresponding oxygen abundances lie above the predicted threshold. The subcritical [C/H] abundances could have originated either in the
progenitor cloud or from the mixing of CNO-processed material (with carbon converted into nitrogen) into the stellar atmosphere during the red giant phase. To guard against this a posteriori processing of carbon (and to a lesser degree of oxygen), dwarf stars should be used, as they provide a more reliable record of the primordial abundance pattern that was present at birth. The current data on dwarf stars (filled symbols in Figure 9) does not yet reach carbon and oxygen abundances that are sufficiently low to probe the theoretical cooling thresholds. Note also that the extremely iron-poor star HE0107-5240 has carbon and oxygen abundances that lie above the respective critical levels. The formation of this low-mass star (∼0.8 $M_\odot$) is therefore consistent with the theoretical framework considered by Bromm & Loeb (2003c).

The lessons from stellar archaeology on the nature of the first stars are likely to increase in importance because greatly improved, large surveys of metal-poor galactic halo stars are under way or are currently being planned.

5.3. Gamma-Ray Bursts as Probes of the First Stars

GRBs are the brightest electromagnetic explosions in the universe, and they should be detectable out to very high redshifts (e.g., Wijers et al. 1998, Blain & Natarajan 2000, Ciardi & Loeb 2000, Lamb & Reichart 2000, Bromm & Loeb 2002, Choudhury & Srianand 2002). Although the nature of the central engine that powers the relativistic jets is still debated, recent evidence indicates that GRBs trace the formation of massive stars (e.g., Bloom et al. 2002, and references therein). Because the first stars are predicted to be predominantly very massive, their death might possibly give rise to GRBs at very high redshifts (e.g., Schneider et al. 2002b). A detection of the highest-redshift GRBs would probe the earliest epochs of star formation, one massive star at a time (e.g., Barkana & Loeb 2004, Mészáros & Rees 2003). The Swift satellite,4 planned for launch in 2004, is expected to detect approximately one hundred GRBs per year. The redshifts of high-z GRBs can be easily measured through infrared photometry on the basis of the Gunn-Peterson trough in their spectra owing to Ly$\alpha$ absorption by neutral intergalactic hydrogen along the line of sight. What fraction of the detected bursts will originate at redshifts $z \gtrsim 5$?

To assess the utility of GRBs as probes of the first stars, one has to calculate the expected redshift distribution of GRBs (e.g., Bromm & Loeb 2002, Choudhury & Srianand 2002). Under the assumption that the GRB rate is simply proportional to the star formation rate, Bromm & Loeb (2002) find that approximately a quarter of all GRBs detected by Swift will originate from a redshift $z \gtrsim 5$ (see Figure 10). This estimate takes into account the detector sensitivity, but it is still very uncertain because of the poorly determined GRB luminosity function. The rate of high-redshift GRBs may, however, be significantly suppressed if the early massive stars

4See http://swift.gsfc.nasa.gov.
Figure 10  Redshift distribution of all GRBs in comparison with measurements in flux-limited surveys. (a) Fraction of bursts that originate at a redshift higher than $z$ versus $z$. The data points reflect $\sim 20$ observed redshifts to date. (b) Fraction of bursts per logarithmic interval of $(1+z)$ versus $z$. (Solid lines) All GRBs for star formation in halos massive enough to allow cooling via lines of atomic hydrogen. The calculation assumes that the GRB rate is proportional (with a constant factor) to the star formation rate at all redshifts. (Dot-dashed lines) Expected distribution for Swift. (Long-dashed lines) Expected distribution for BATSE. The curves for the two flux-limited surveys are rather uncertain because of the poorly determined GRB luminosity function. (From Bromm & Loeb 2002.)

fail to launch a relativistic outflow. This is conceivable, as metal-free stars may experience negligible mass loss before exploding as a SN (Baraffe et al. 2001). They would then retain their massive hydrogen envelope, and any relativistic jet might be quenched before escaping from the star (Heger et al. 2003).

If high-redshift GRBs exist, the launch of Swift will open up an exciting new window into the cosmic dark ages (e.g., Gou et al. 2004). Different from quasars or galaxies that fade with increasing redshift, GRB afterglows maintain a roughly constant observed flux at different redshifts for a fixed observed time lag after the gamma-ray trigger (Ciardi & Loeb 2000). The increase in the luminosity distance at higher redshifts is compensated by the fact that a fixed observed time lag corresponds to an intrinsic time shorter by a factor of $(1 + z)$ in the source rest-frame, during which the GRB afterglow emission is brighter. This quality makes GRB afterglows the best probes of the metallicity and ionization state of the intervening IGM during the epoch of reionization. In contrast to quasars, the UV emission from
GRBs has a negligible effect on the surrounding IGM (because $\sim 10^{51}$ ergs can only ionize $\sim 4 \times 10^4 M_\odot$ of hydrogen). Moreover, the host galaxies of GRBs induce a much weaker perturbation to the Hubble flow in the surrounding IGM, compared to the massive hosts of the brightest quasars (Barkana & Loeb 2004). Hence, GRB afterglows offer the ideal probe (much better than quasars or bright galaxies) of the damping wing of the Gunn-Peterson trough (Miralda-Escudé 1998) that signals the neutral fraction of the IGM as a function of redshift during the epoch of reionization.

6. EPILOGUE: THE ROAD AHEAD

One of the fascinating aspects of the recent research on the first stars has been the confluence of many hitherto unrelated subfields. To fully explore its rich potential, we have to utilize high-redshift studies and near-field cosmological data (Freeman & Bland-Hawthorn 2002). The latter approach refers to the stellar archaeology of observing the chemical abundance patterns in extremely metal-poor galactic halo stars (see Section 5.2). Furthermore, the study of the first stars lies at the intersection of star-formation theory with cosmological structure formation, where the scales for the phenomena overlap. Similarly, there is also an overlap between star and galaxy formation because at this early time, the scale of galaxies and the scale of star-forming clouds had not yet become clearly separated. Therefore, we can investigate all these phenomena in their most elementary form, before their scales had become widely separated and before the universe had evolved into the vastly more complicated structure that we observe today, where there is a huge range of scales at play.

Most of the work so far has been theoretical, but the field is driven by the prospect of upcoming observational probes that will soon test the theoretical predictions. The WMAP satellite has already provided important clues, and Swift will soon do so as well. Most importantly, NASA’s planned successor mission to the Hubble Space Telescope, the JWST, to be launched around 2011, is a prime driver behind current cosmological research. The JWST is designed to image the first stars, SNe, and quasars. In thinking ahead, pondering about the first glimpses that we have gained into the cosmic dark ages, one wonders what exciting discoveries are awaiting us.

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Figure 1  Emergence of primordial star-forming regions within a standard ΛCDM cosmology. Shown is the projected gas density at $z = 17$ within a simulation box of physical size $\sim 50$ kpc. The bright knots at the intersections of the filamentary network are the sites where the first stars form. (From Yoshida et al. 2003a.)
Figure 7  Situation ~10^6 years after the explosion for the case with $E_{SN} = 10^{53}$ ergs. Shown is the projected gas density within a box of linear physical size 1 kpc. The SN bubble has expanded to a radius of ~200 pc, having evacuated most of the gas in the minihalo (with a virial radius of ~150 pc). The dense shell has fragmented into numerous cloudlets. Inset: Metal distribution after 3 Myr. The stellar ejecta (red dots) trace the metals, and are embedded in pristine, un-enriched gas (blue dots). More than 90% of the heavy elements have escaped the minihalo and have filled a significant fraction of the hot bubble. (From Bromm et al. 2003.)