

The Effect of Large-Scale Structure on the Magnification of High- z Sources by Cluster-Lenses*

Anson D'Aloisio

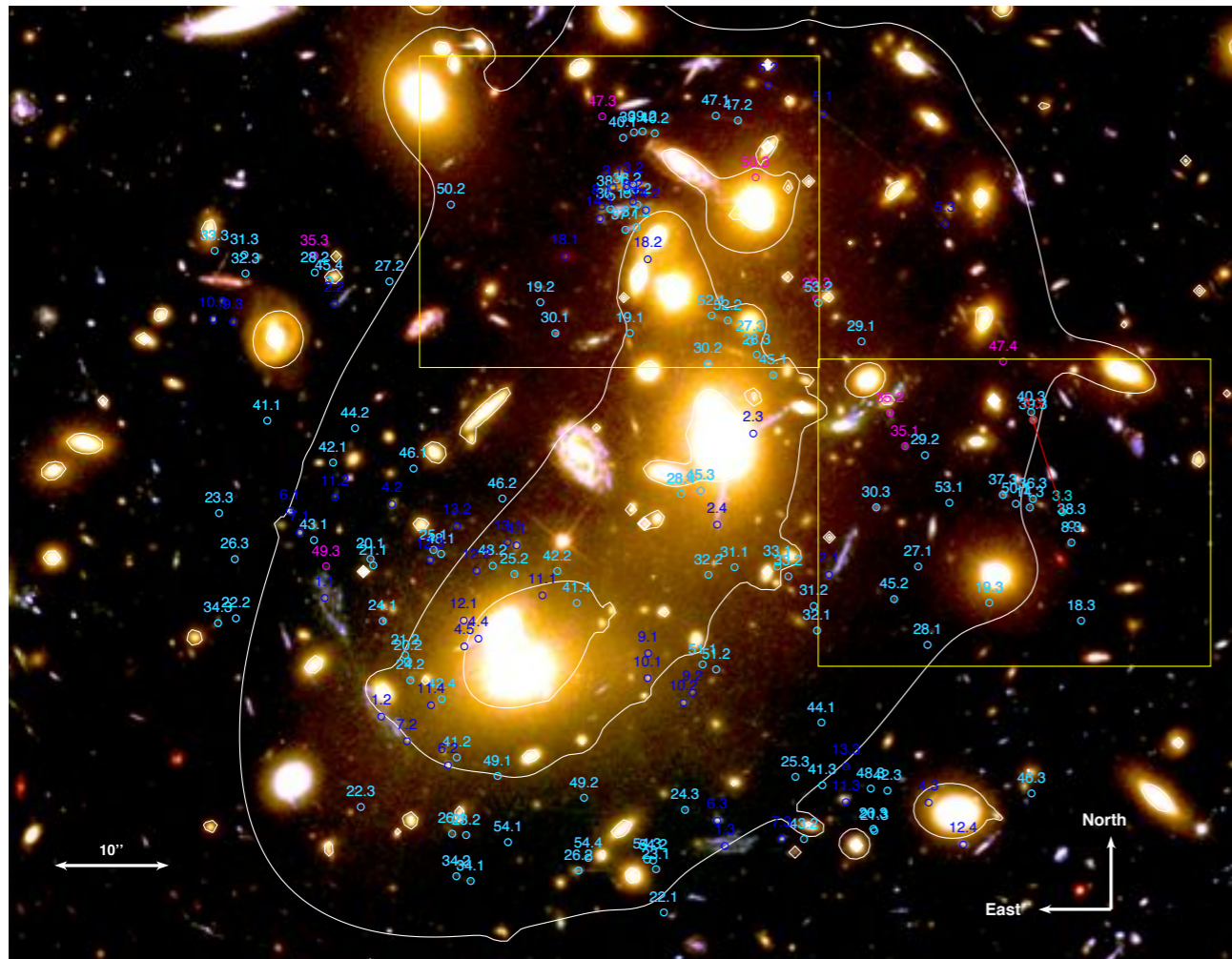
University of Washington, Seattle

University of Texas at Austin

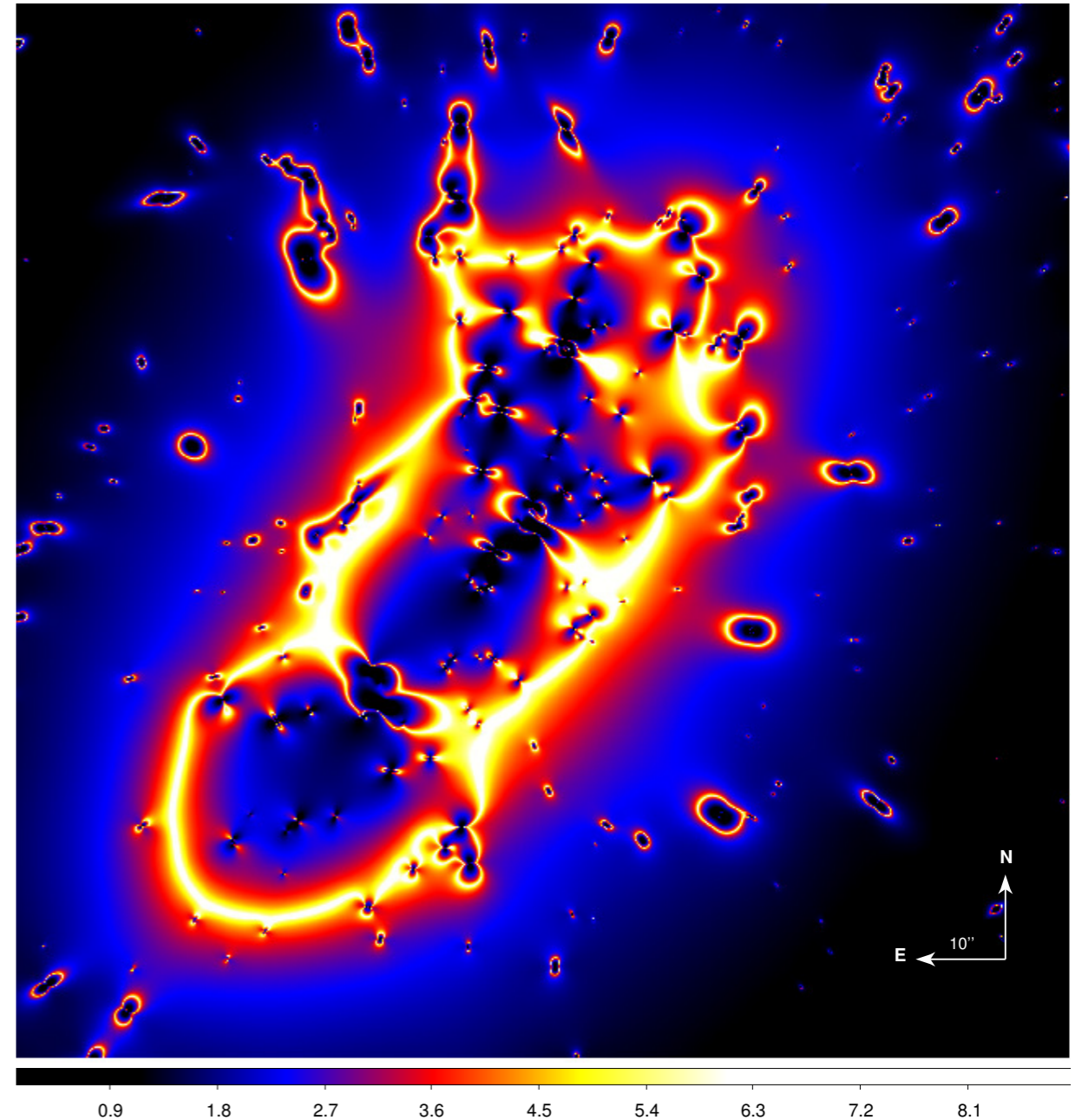
Collaborators: Priyamvada Natarajan & Paul R. Shapiro

*MNRAS, 445, 3581 (arXiv:1311.1614)

HFF Precision Magnification Maps



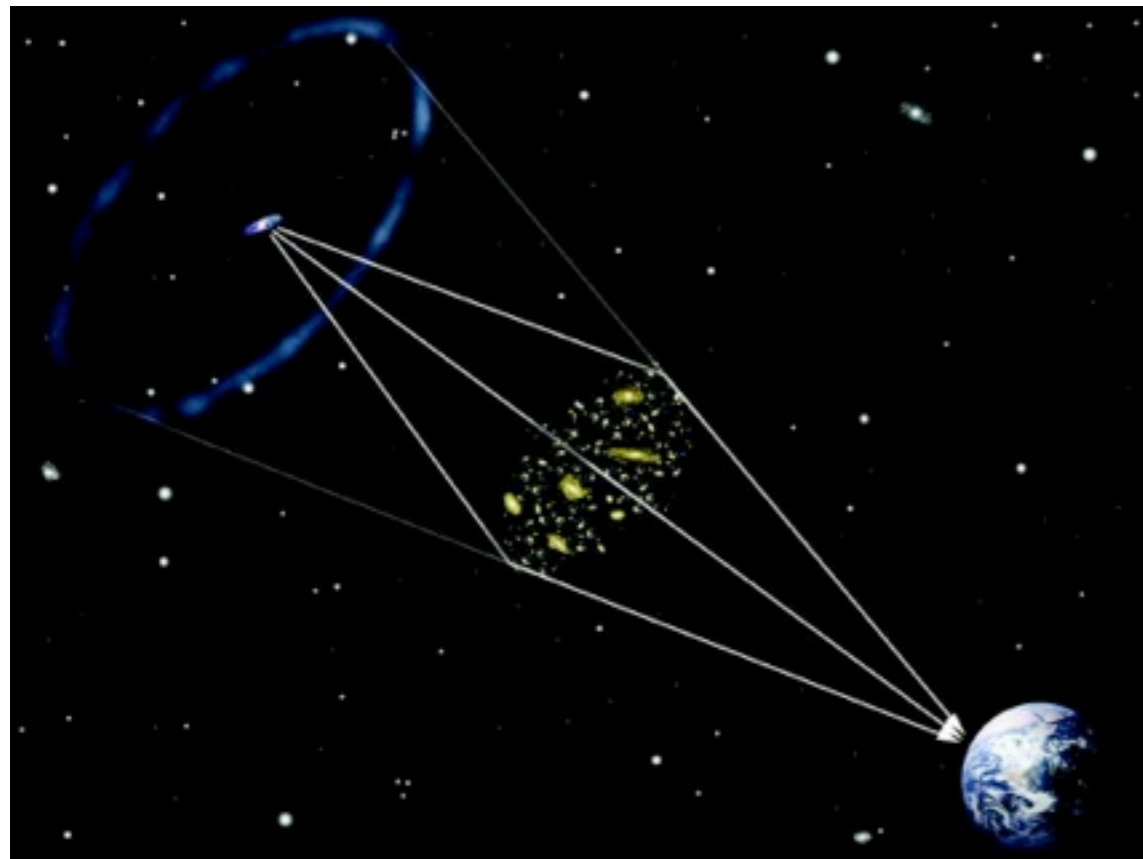
- Groups already reporting statistical uncertainties in μ as low as a few percent!



*Example from [Jauzac et al. 2014](#)

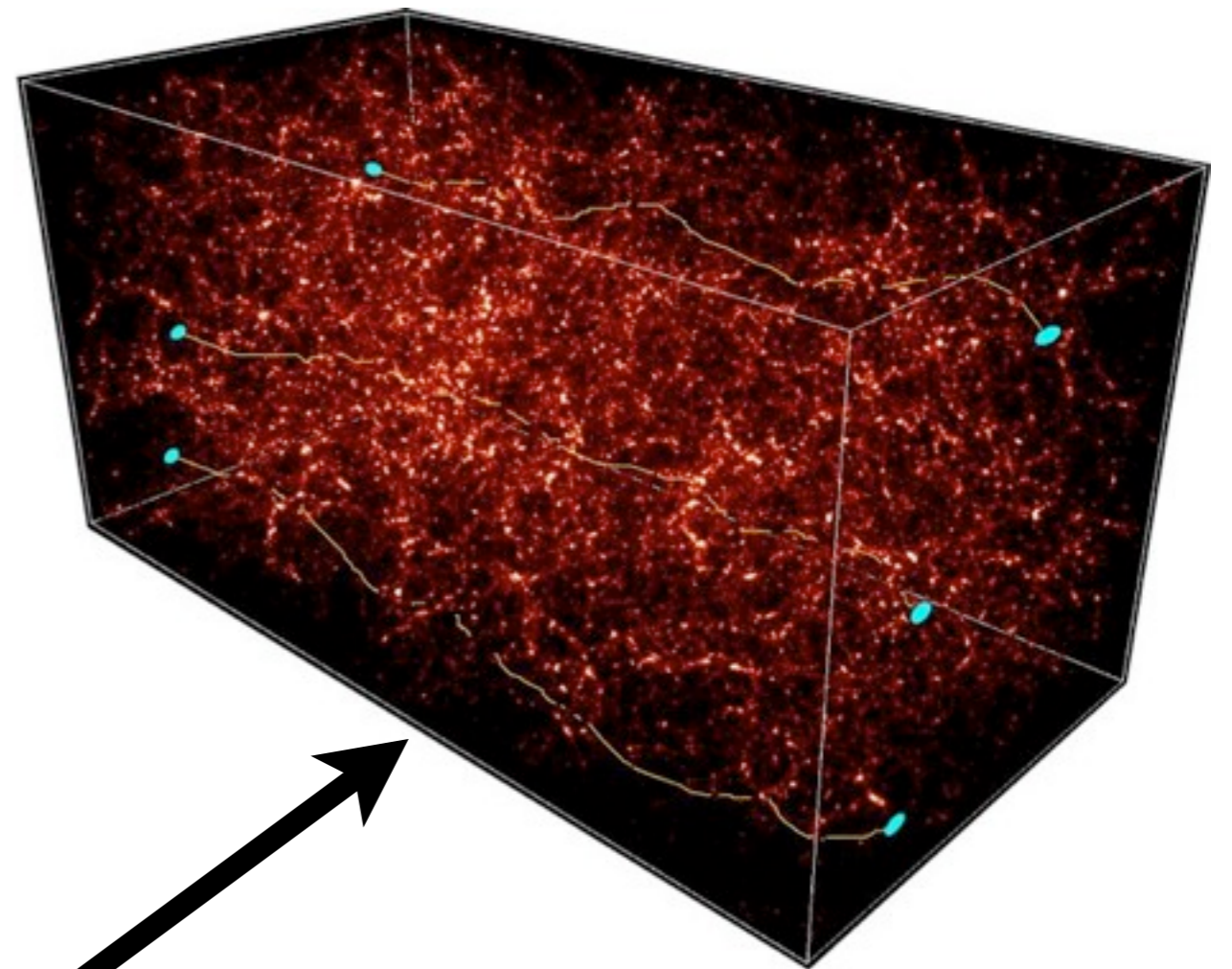
Intervening Large-Scale Structure

Strong-Lensing by Cluster



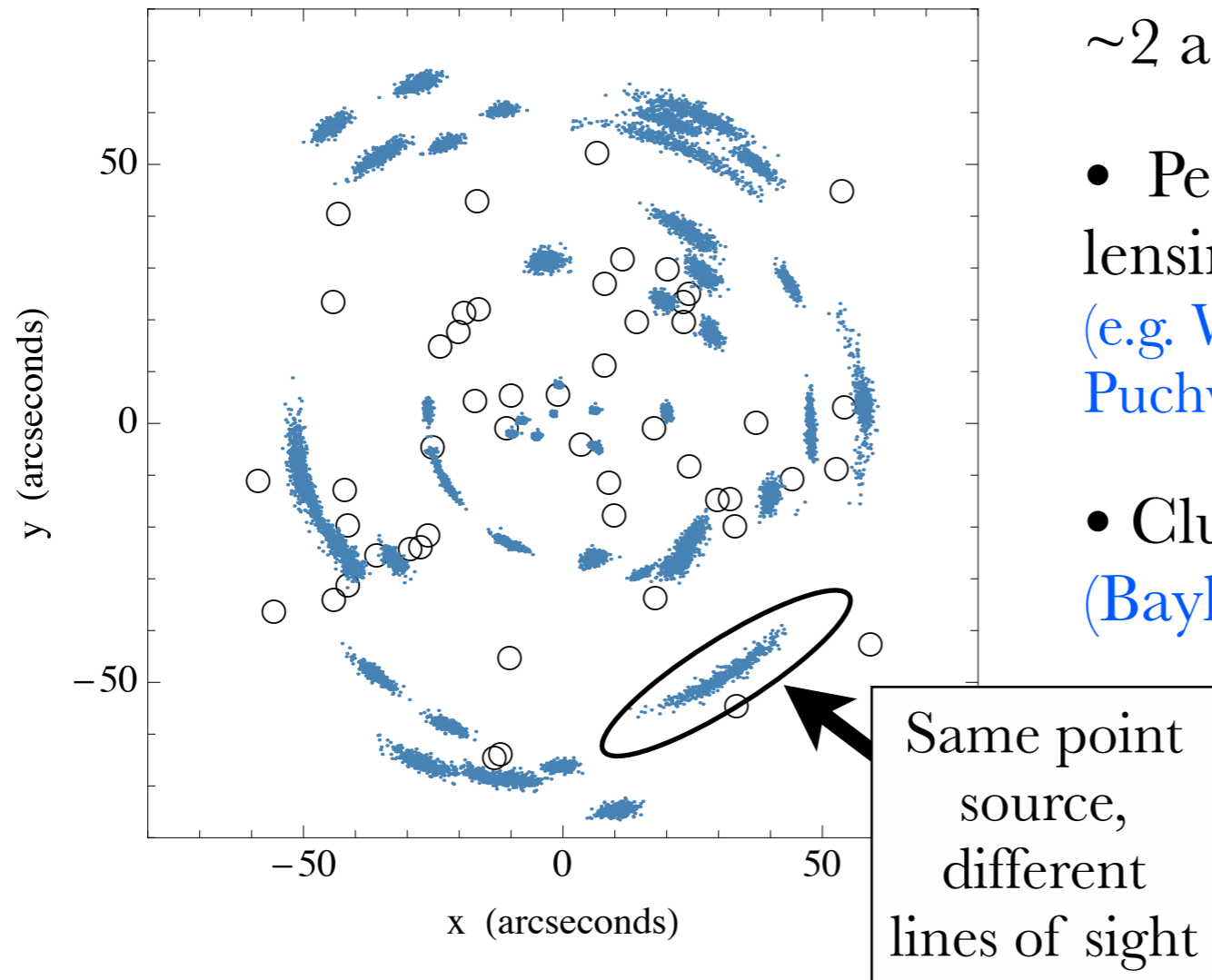
<http://www.lsst.org>

Weak Lensing by LSS



Note, these magnification effects are NOT simply additive.

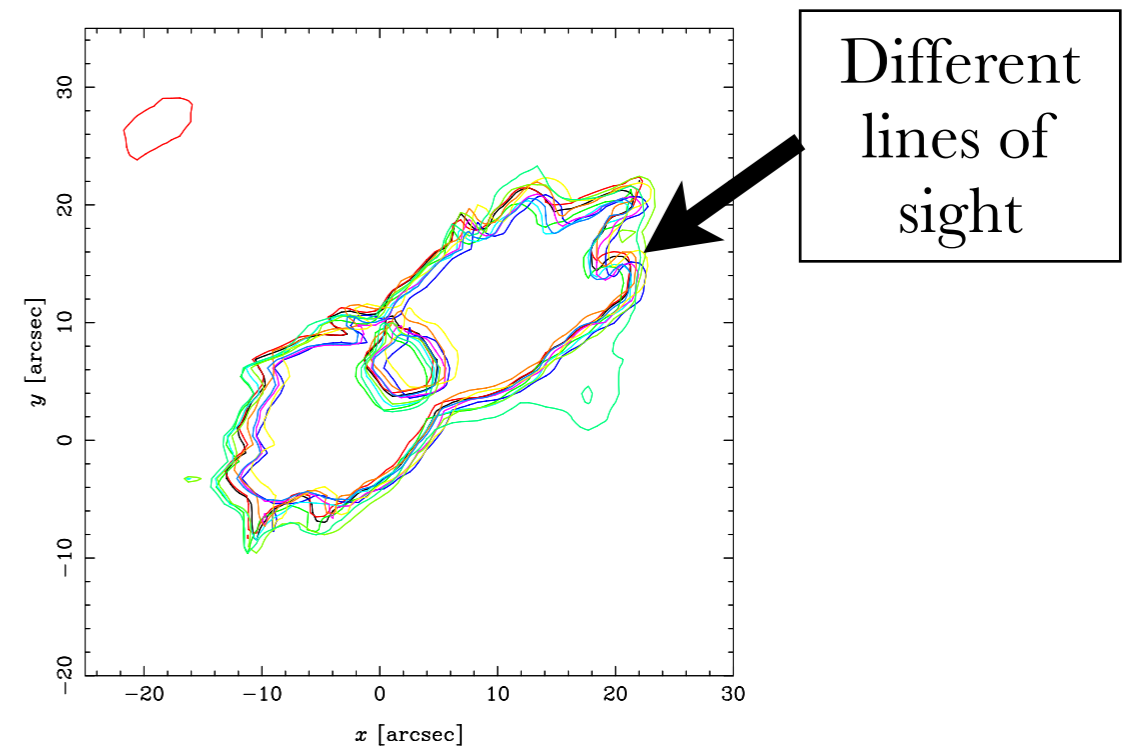
Intervening Large-Scale Structure



*From [D'Aloisio & Natarajan 2011](#)

see e.g. [Wambsganss et al. 2005](#); [Dalal et. al. 2005](#); [Hilbert et. al. 2007](#); [Puchwein & Hilbert 2009](#); [Jullo et. al. 2010](#); [D'Aloisio & Natarajan 2011](#); [Host 2011](#)

- LSS's relative deflection of images:
 ~ 2 arcsec. ([D'Aloisio & Natarajan 2011](#); [Host 2011](#))
- Perturbs critical curves, boosts strong-lensing cross section by $\sim 50\%$
(e.g. [Wambsganss et. al. 2005](#); [Dalal et. al. 2005](#); [Puchwein & Hilbert 2009](#))
- Cluster-lenses are on special lines of sight.
([Bayliss, Johnson, Sharon et. al. 2014](#))



*From [Dalal et. al. 2005](#)

Intervening Large-Scale Structure

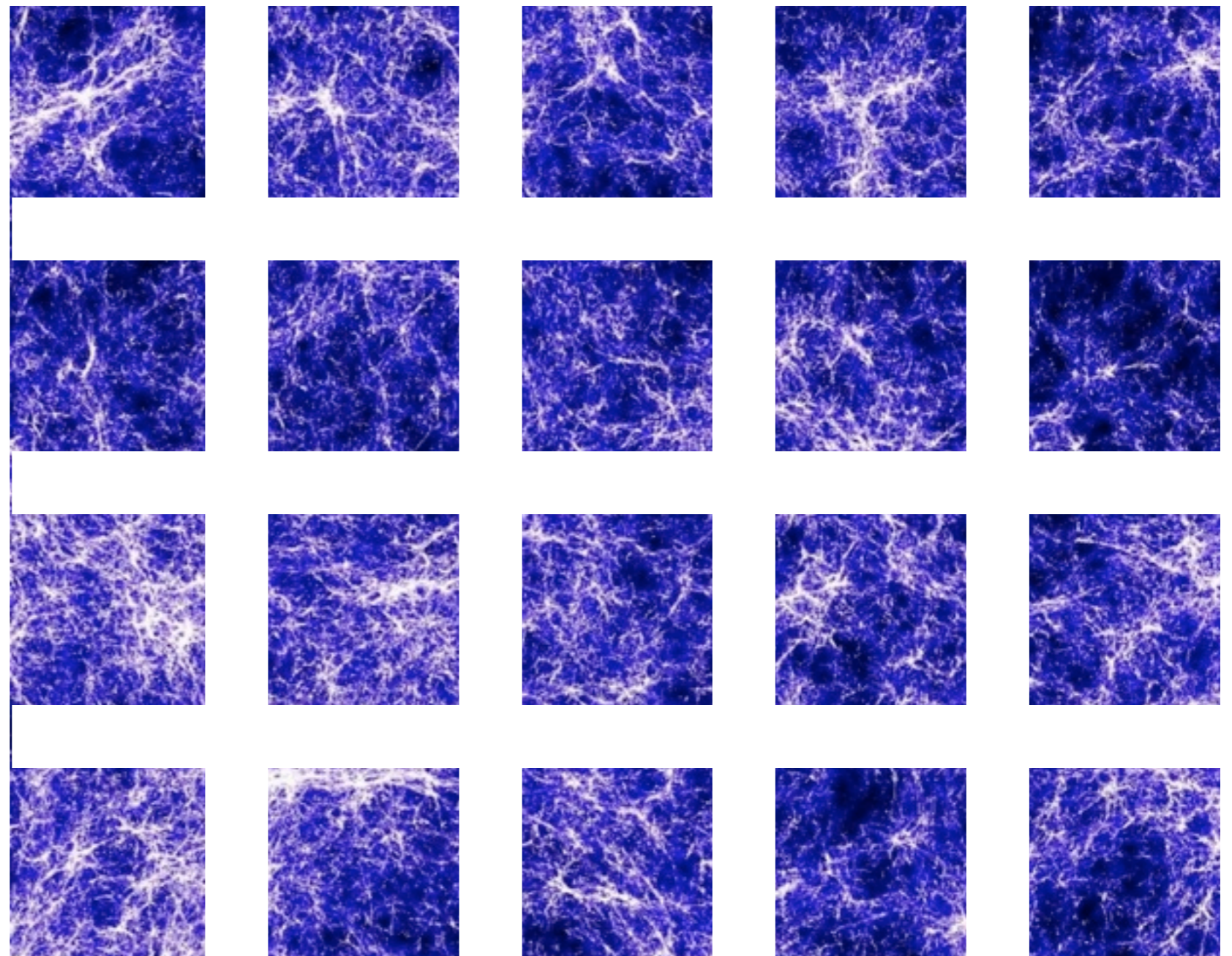
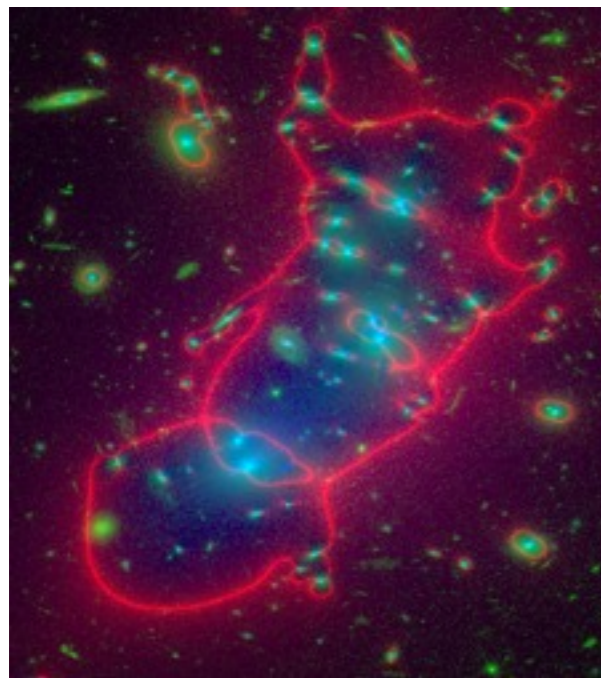
Question: How much can LSS contribute to the magnification maps of cluster-lenses?

- Approach: “semi-analytical” based on nonlinear matter power spectrum.
- A useful precursor to simulations:
 - Shot noise in ray-tracing, especially for large μ .
([Bradac et al. 2004](#); [Amara et al. 2006](#); [Li et al. 2006](#); [Xu et al. 2009](#); [Rau et al. 2013](#); [Angulo et al. 2014](#))
 - Finite mass-resolution of simulations, and power from $0.01 \lesssim k \lesssim 1000 \text{ Mpc}^{-1}$ contributes! (see [arXiv:1311.1614](#))

The Calculation: Concept

Ensemble of LSS realizations

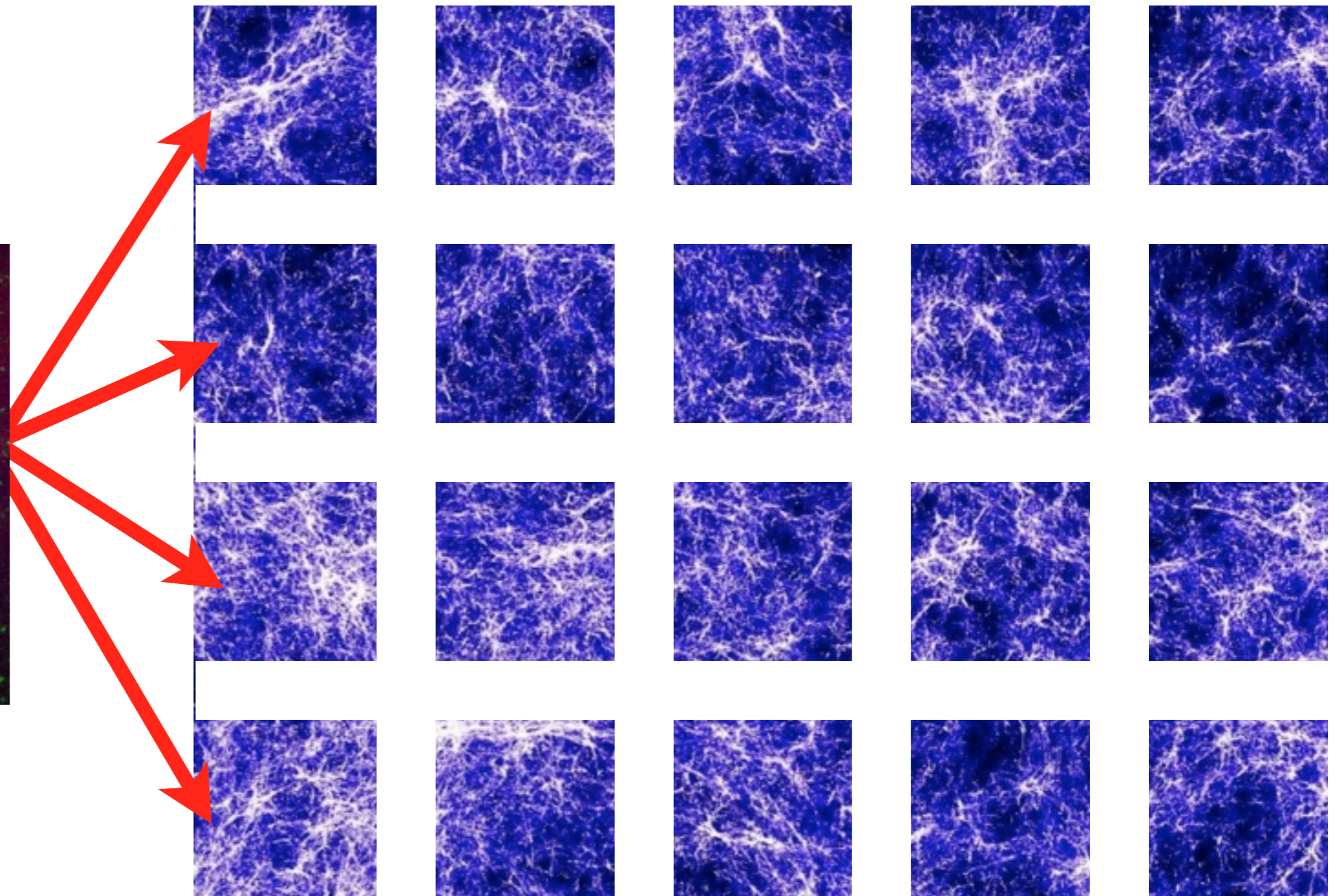
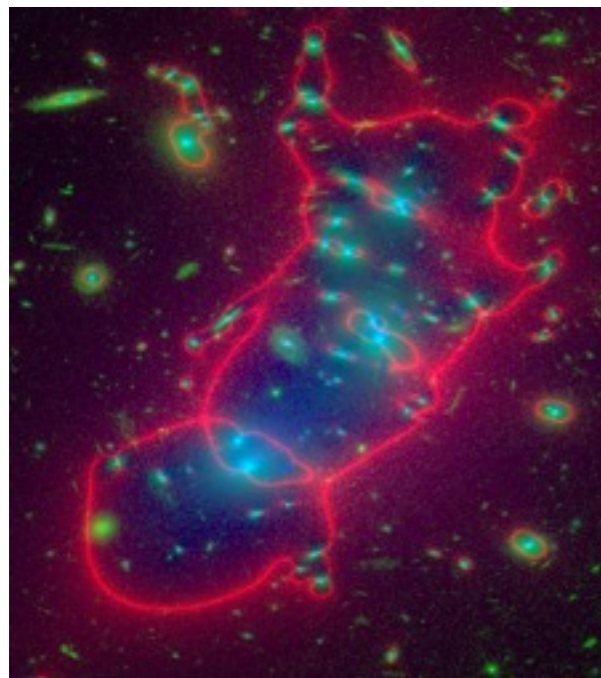
Isolated
Cluster-lens



The Calculation: Concept

Stick the cluster in ensemble and measure fluctuations across magnification maps

Isolated
Cluster-lens



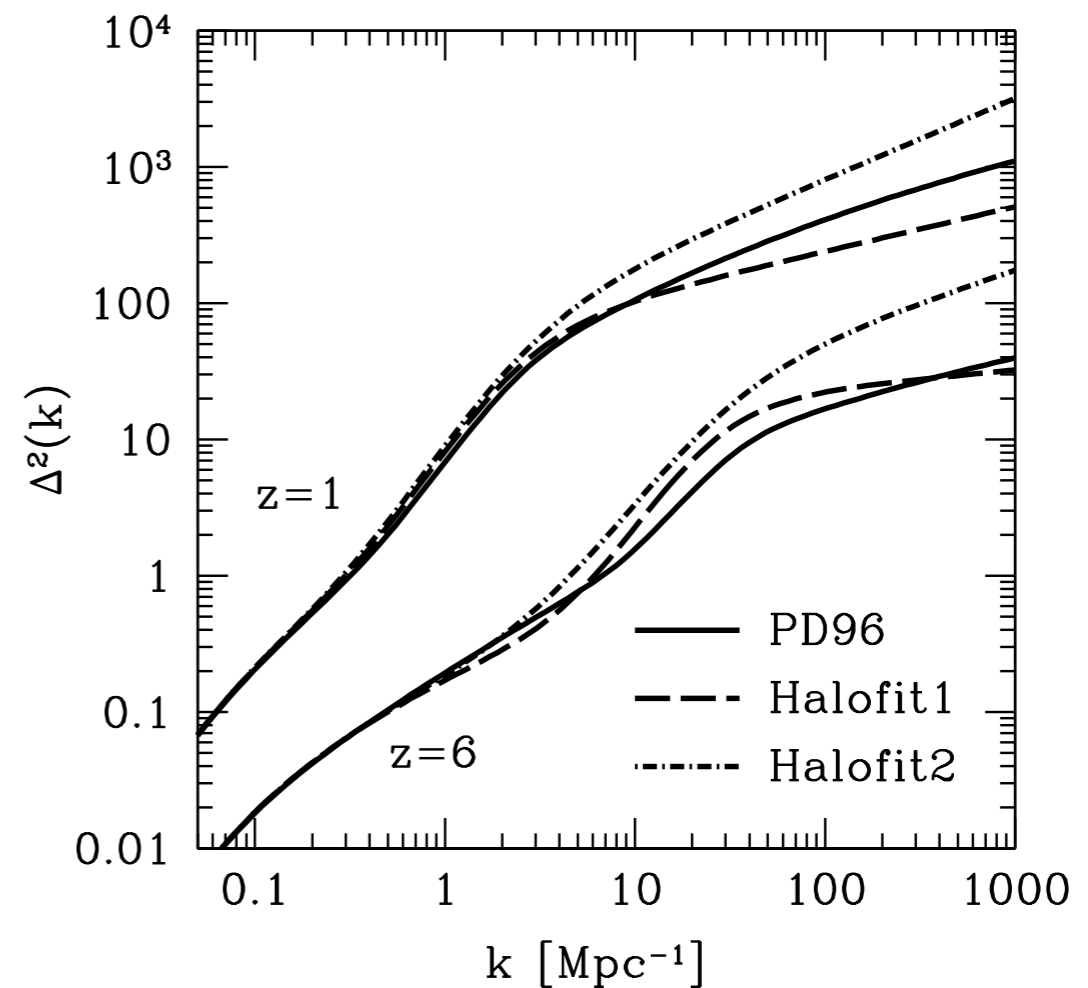
The Calculation: in Practice

- Lens equation: $\theta_{S,i} = \theta_{I,i} - \alpha_i(\mathbf{x}(\chi_L)) + \frac{2}{\chi_S} \int_0^{\chi_S} d\chi' \partial_i \Phi_{\text{LSS}}(\mathbf{x}, \chi') (\chi_S - \chi')$
- Expand Φ_{LSS} about $\mathbf{x}=0$ (Barkana 1996)
- Calculate fractional standard deviation of $1/\mu$

$$\frac{\sigma_{1/\mu}}{|\langle \mu^{-1} \rangle|}$$

- LSS encapsulated in matter power spectrum, $P(k)$.

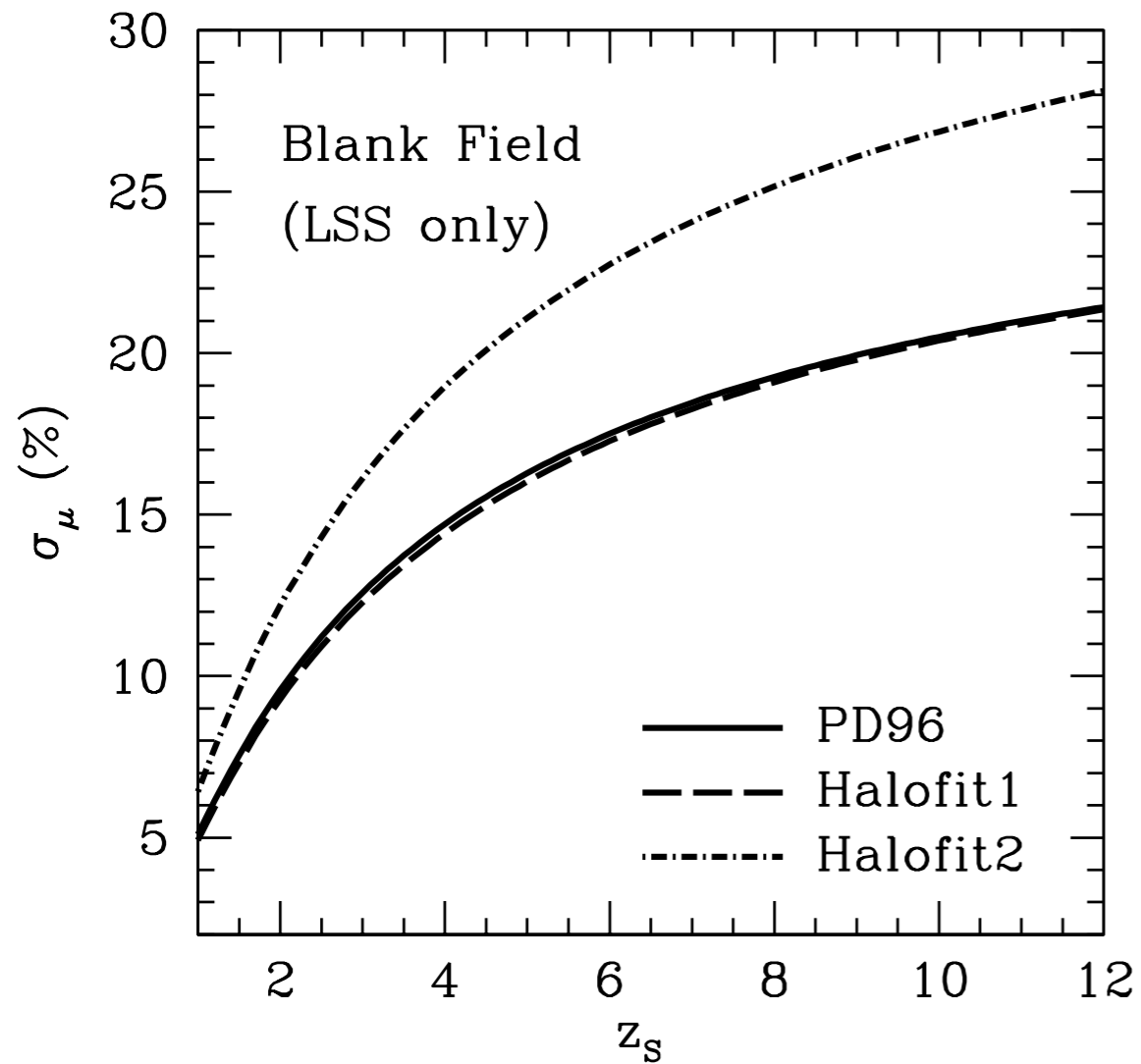
- Illustrative purposes: NFW lens.



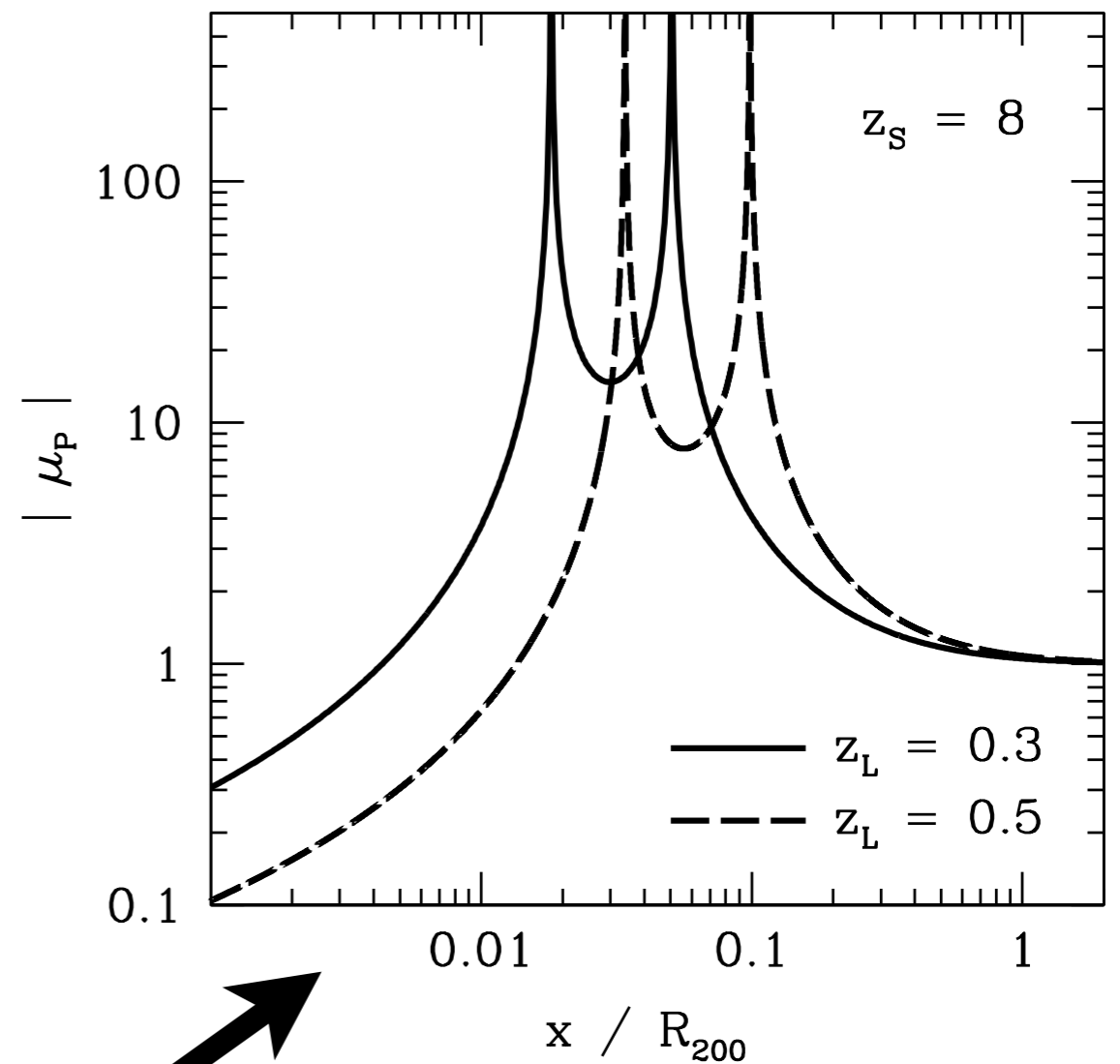
PD96 = Peacock & Dodds 1996
 Halofit1 = Smith et. al. 2003
 Halofit2 = Takahashi et. al. 2012

LSS (“Blank Field”) and Cluster Separately

LSS only



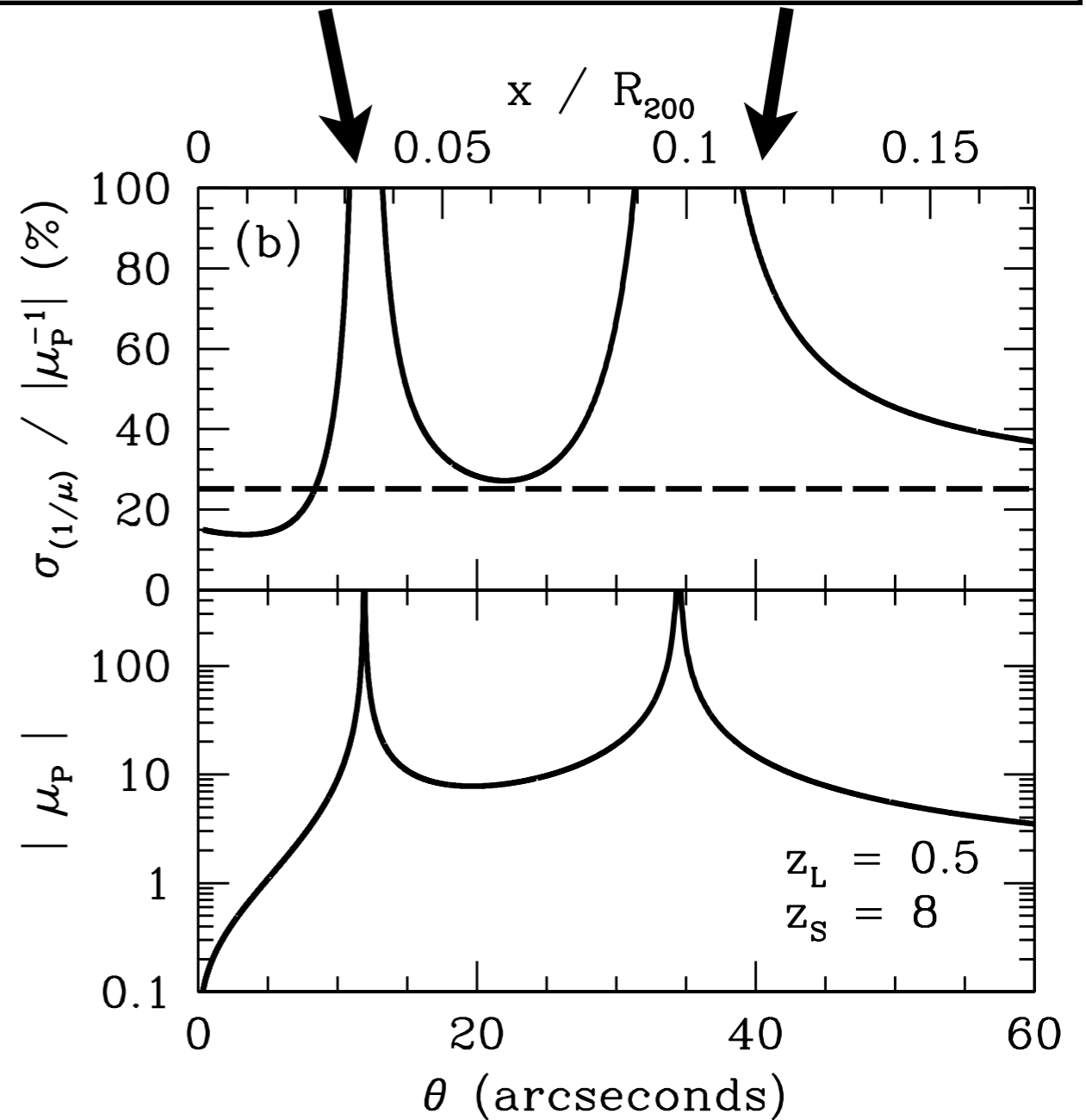
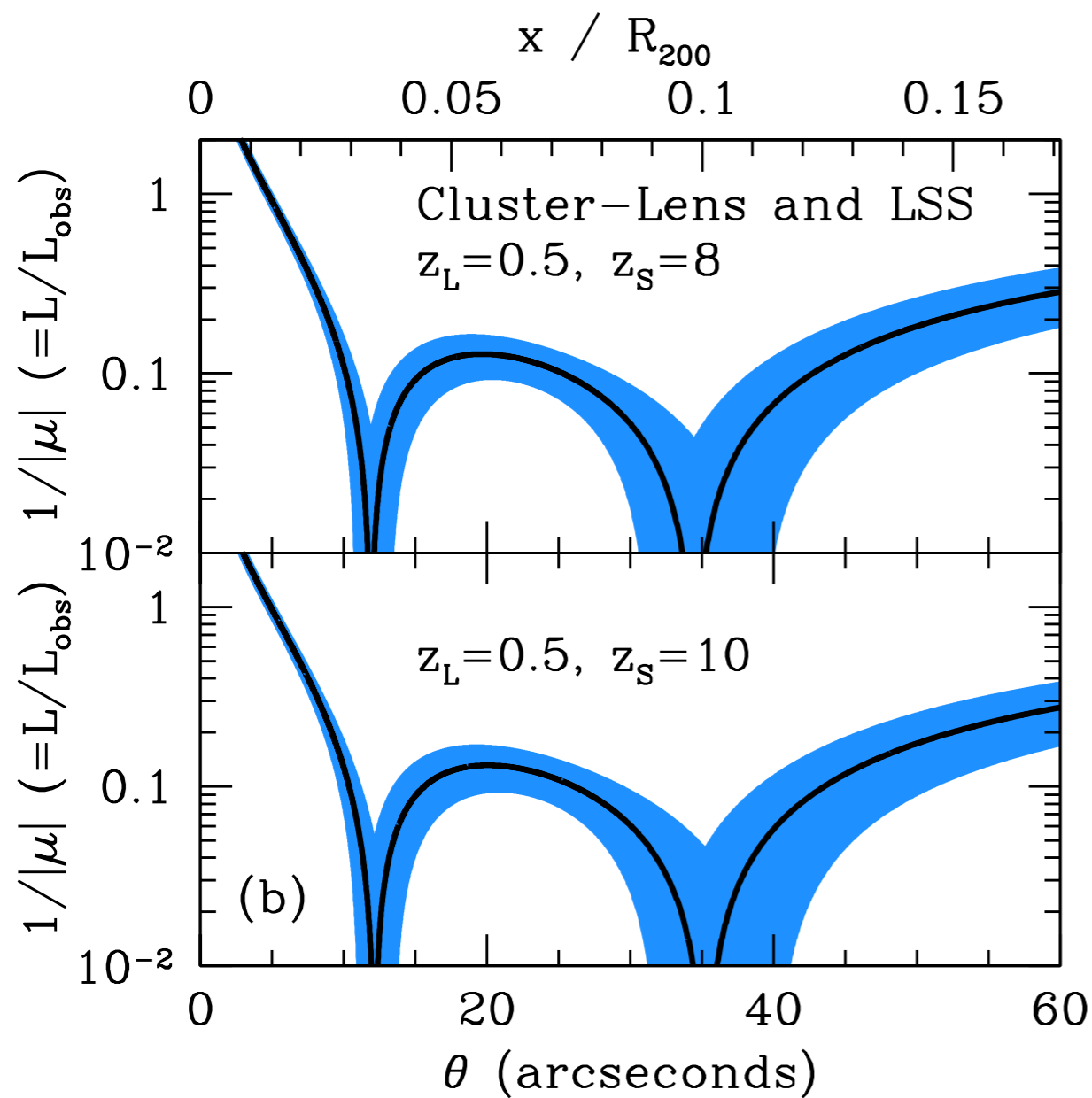
Cluster only



Simple NFW model (Bartelmann 1996) with $M_{200} = 2 \times 10^{15} M_\odot$, $c_{200} = 4$

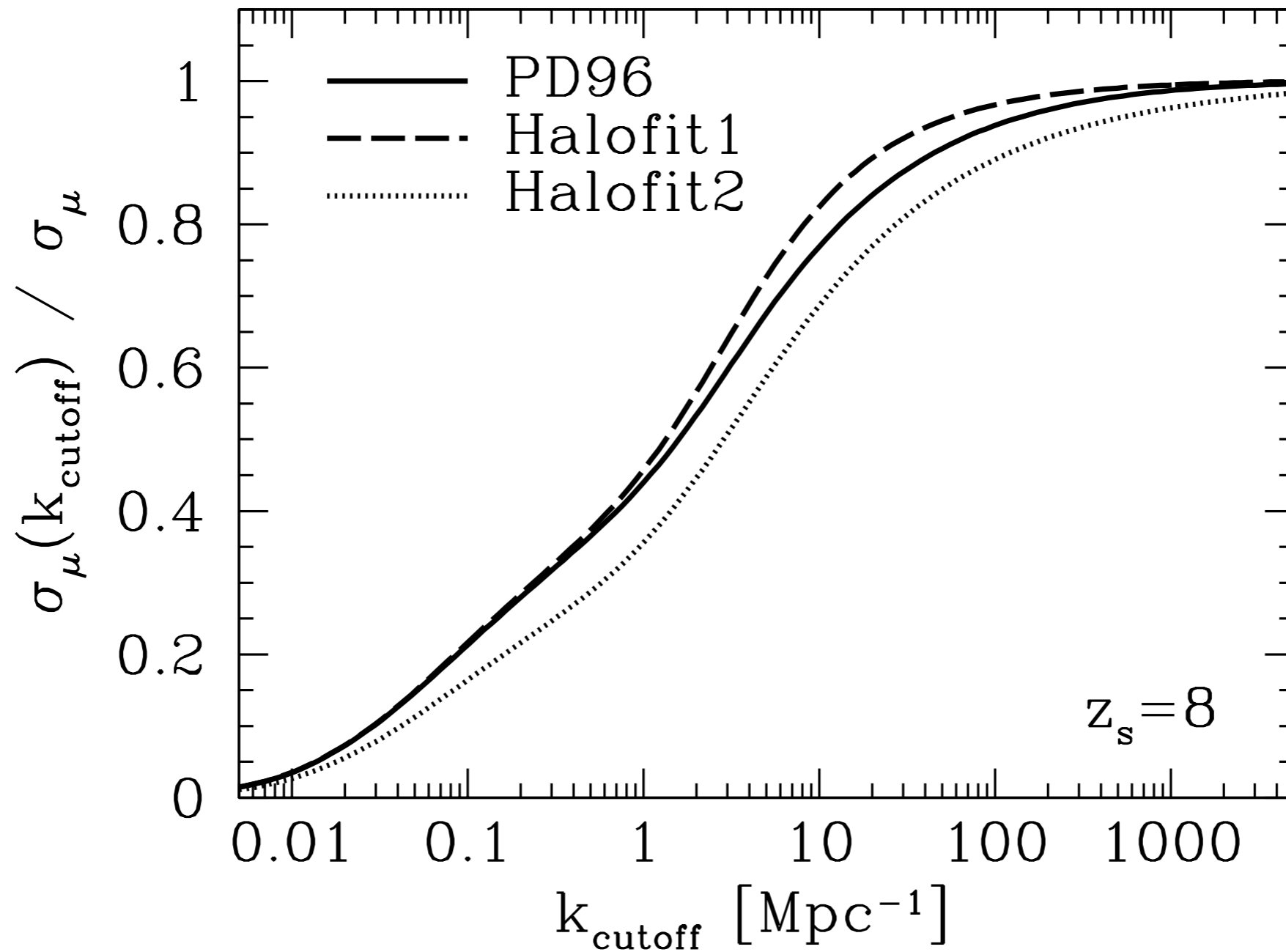
LSS and Cluster Combined

Because LSS perturbs critical curves



Results here from Halofit2 power spectrum

Contribution of “Small-Scale” Structure



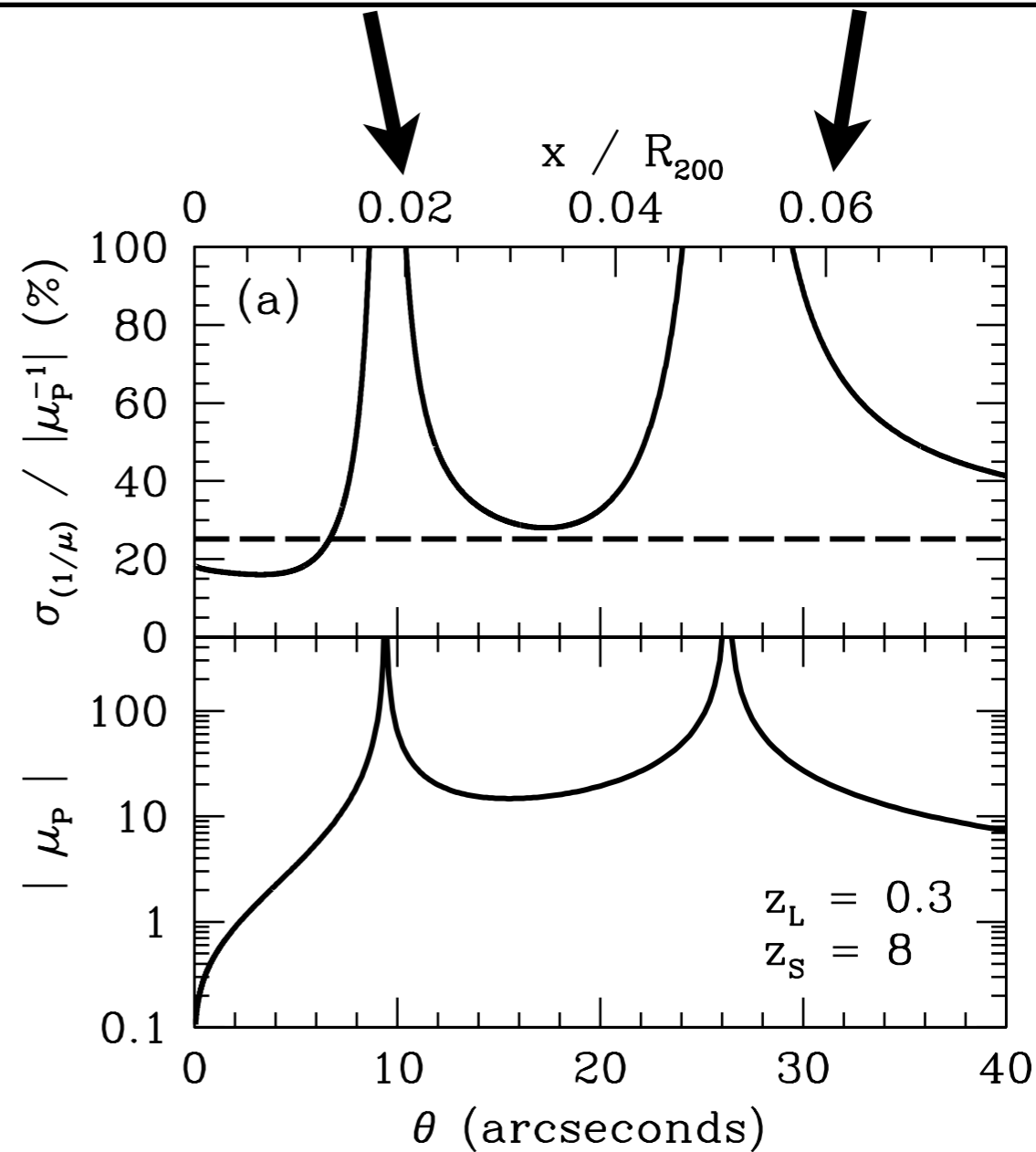
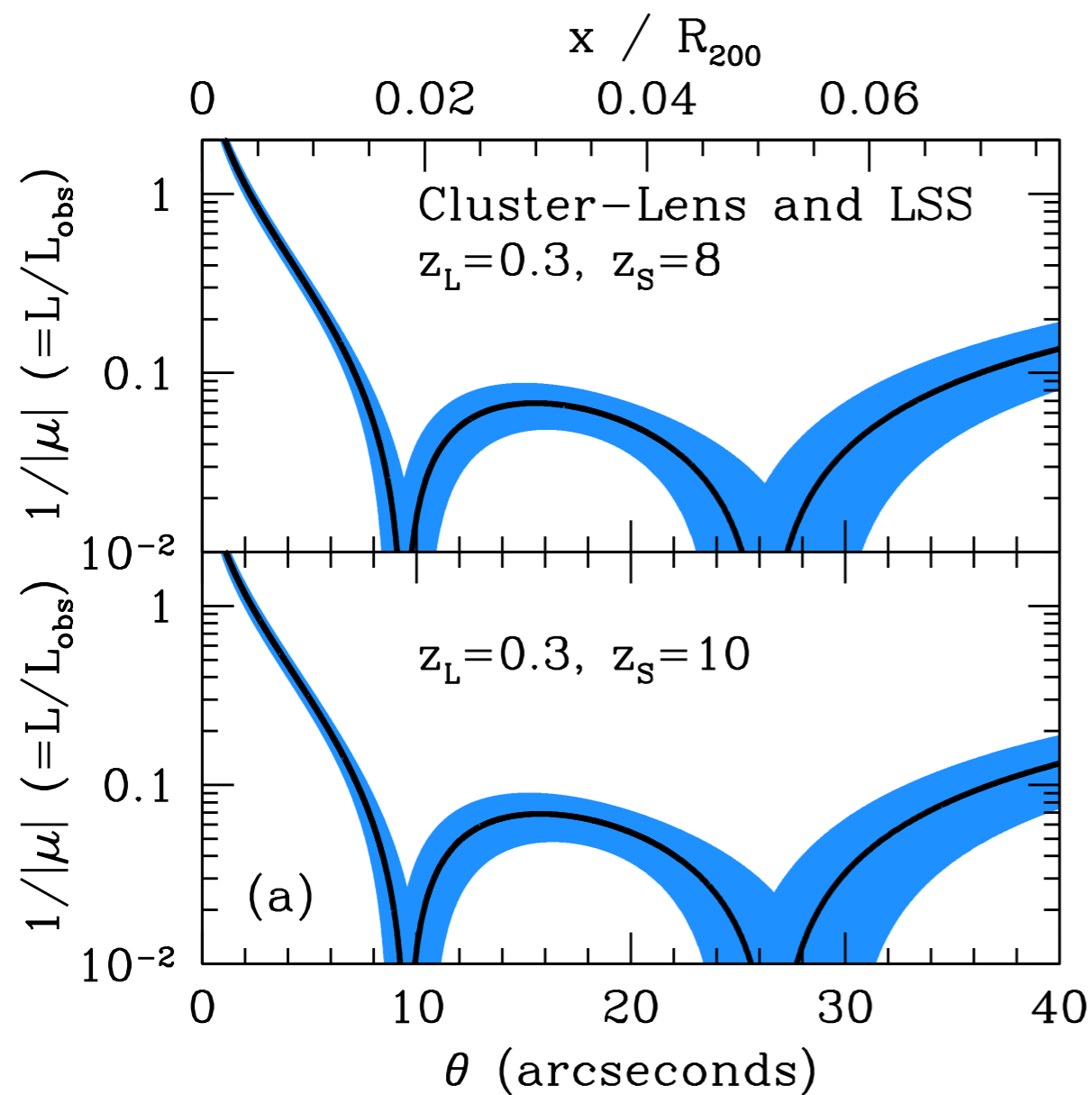
Conclusion

- For cluster-lenses at $z_L \sim 0.5$, fluctuations in the μ of sources (from LSS) at redshifts $z_S > 6$ are $\sim 10-20(20-30)\%$ for typical $\mu \sim 5(10)$.
- LSS tends to have its largest impact on the most magnified images (greater than order unity fluctuations in μ near critical curves!).

- These numbers do NOT represent μ -measurement errors.
- These results do NOT preclude accurate μ -measurements, e.g. may be possible to model LSS by extending existing methods to case with multiple source redshifts.
- Motivates future numerical work towards quantifying effects of LSS in cluster-lens reconstruction (e.g. Frontier Fields Comparison Project).

LSS and Cluster Combined

Because LSS perturbs critical curves



Results here from Halofit2 power spectrum