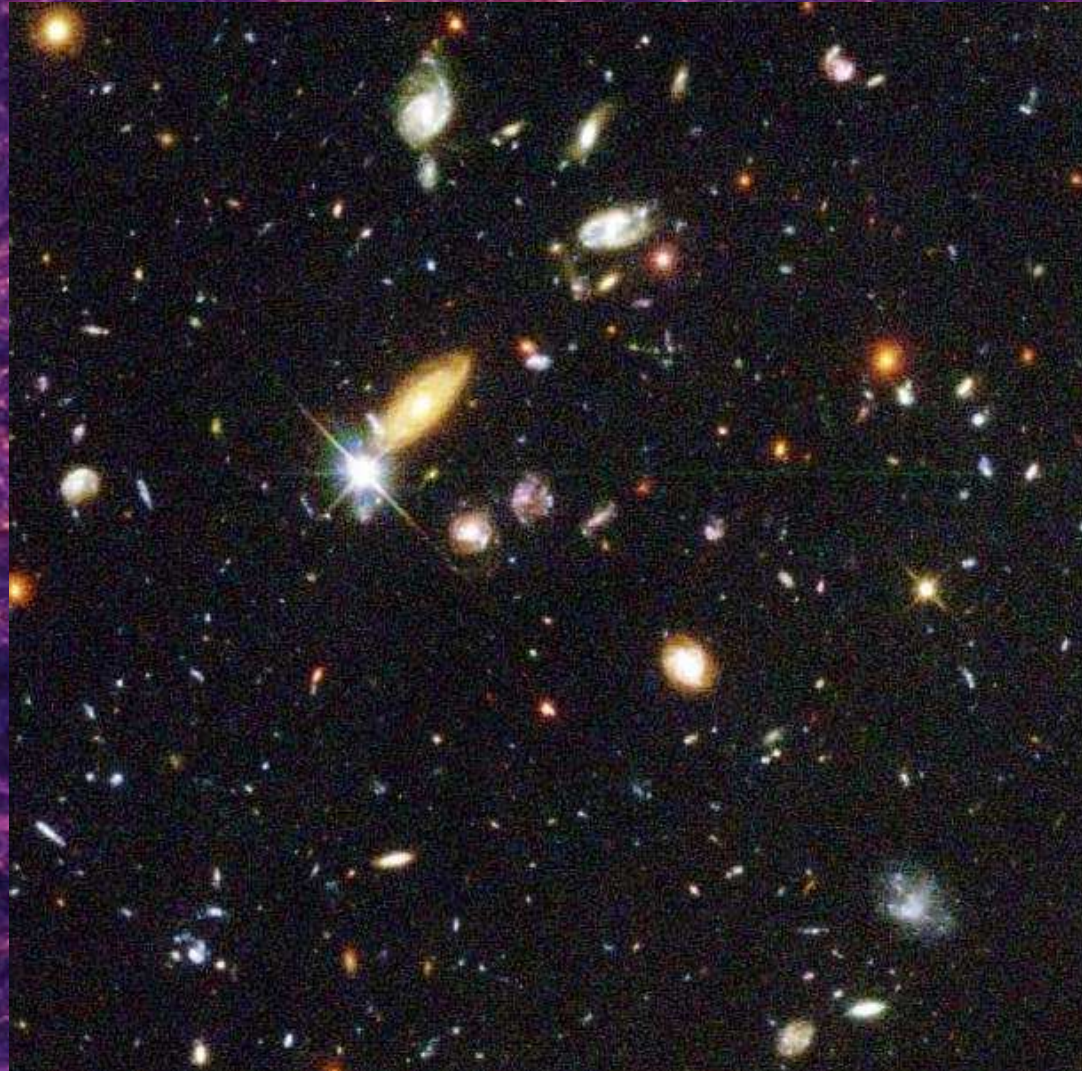


The Galaxy–Dark Matter Connection



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Introduction

PARADIGM: Galaxies live in extended Cold Dark Matter Haloes.

QUESTION: What Galaxy lives in What Halo?

- How many galaxies, on average, per halo?
- How does $\langle N \rangle$ depend on M and L ?
- What is $\langle L \rangle(M)$?
- How are galaxies distributed (**spatially & kinematically**) within halo?

The answers to these questions hold important information regarding

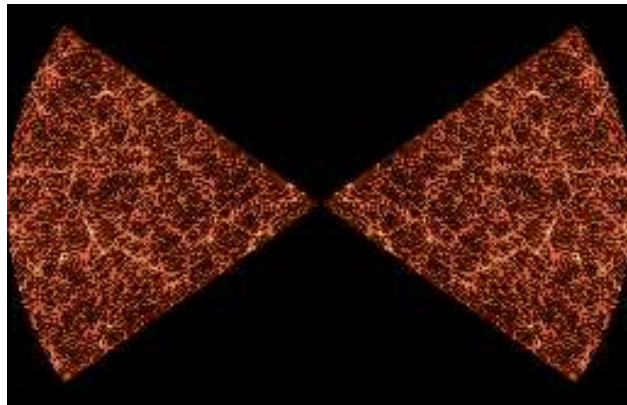
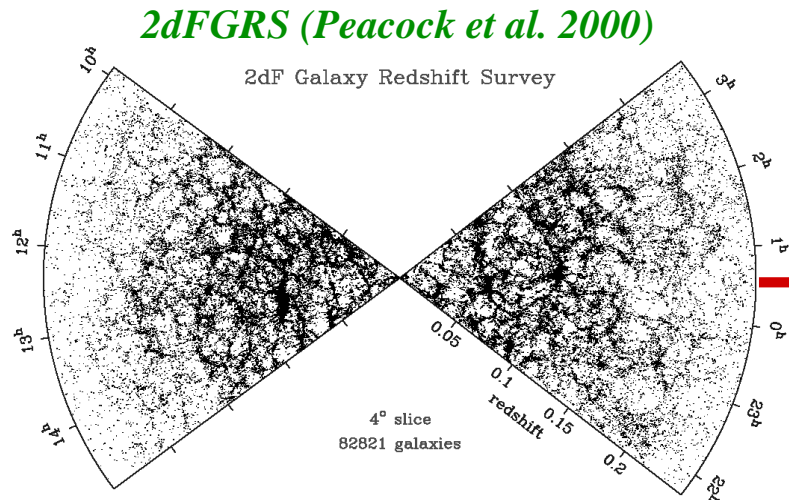
- **Galaxy Formation** (cooling/starformation/feedback)
- **Large Scale Structure** (galaxy bias)
- **Cosmology** (Halo mass function/CDM distribution)

The **galaxy-dark matter connection** can be studied

Physically: Ab initio galaxy formation models (**SAMs**)

Statistically: The Halo Occupation Distributions (**HODs**)

The Galaxy-Dark Matter Connection



HOD

$P(N|M)$

Seljak 2000

Scoccimarro et al. 2001

Berlind & Weinberg 2002

Zehavi et al. 2004

Zheng et al. 2004

Tinker et al. 2004

The **H**alo **O**ccupation **D**istribution $P(N|M)$ specifies the probability that a halo of mass M contains N galaxies.

It specifies the **galaxy bias** and links the galaxy-galaxy correlation function, $\xi_{gg}(r)$, to the halo-halo correlation function, $\xi_{hh}(r)$.

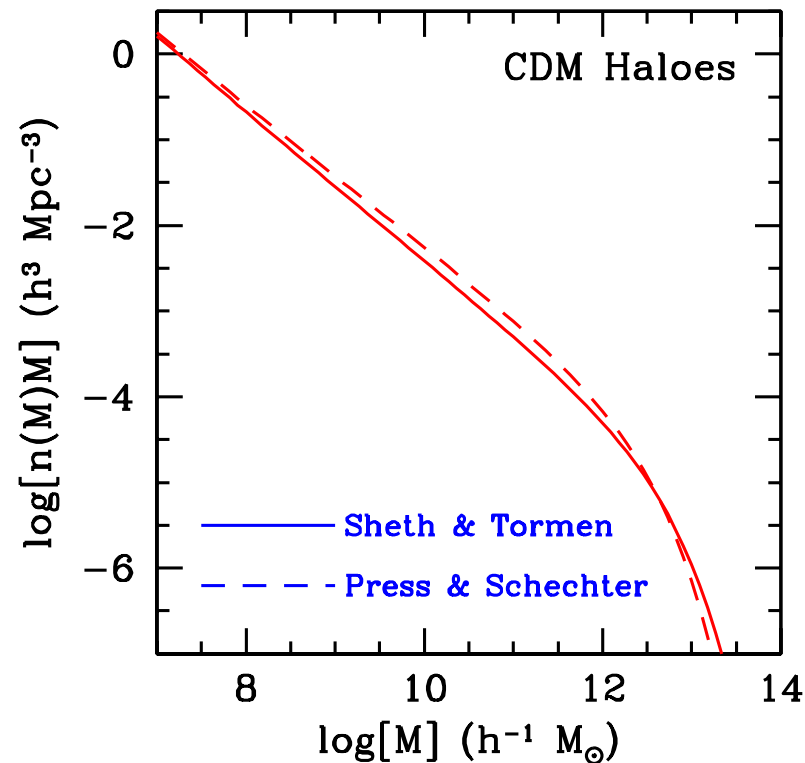
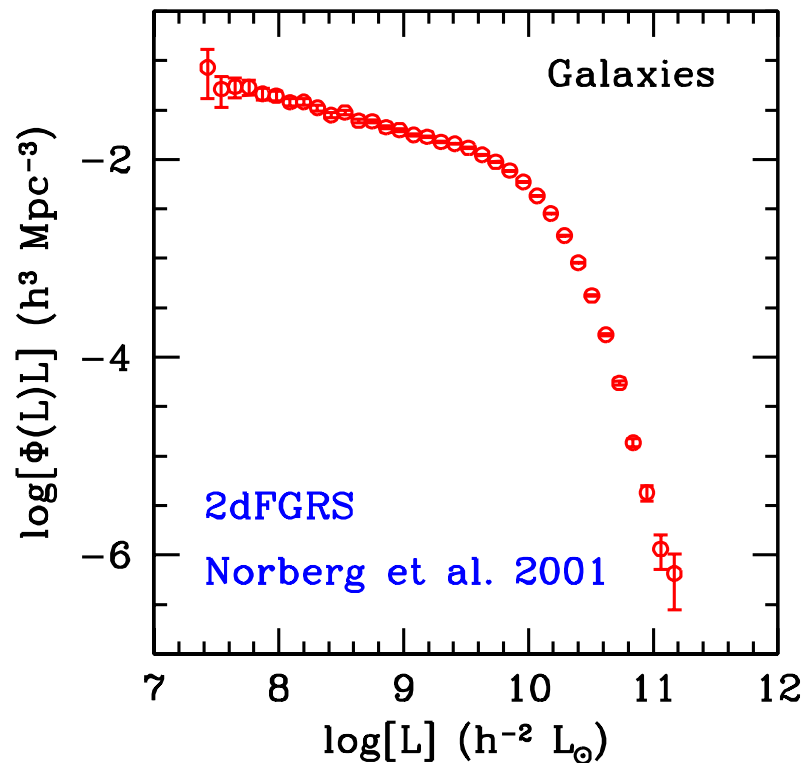
Lighting-Up the Dark Matter

Important Shortcoming: Galaxy bias depends on galaxy properties:

$$b_{\text{gal}} = b_{\text{gal}}(L, \text{type}, \dots)$$

This information is not encapsulated in **HOD** modeling.

To address $b_{\text{gal}}(L)$ we introduce the **Conditional Luminosity Function (CLF)**



The CLF, $\Phi(L|M)$, expresses the average number of galaxies with luminosity L that reside in a halo of mass M

The Conditional Luminosity Function

CLF is **direct** link between galaxy LF, $\Phi(L)$ and halo mass function, $n(M)$:

$$\Phi(L) = \int_0^\infty \Phi(L|M) n(M) dM$$

The CLF contains a lot of important information, such as:

- halo occupation **numbers** as function of luminosity:

$$N_M(L > L_1) = \int_{L_1}^\infty \Phi(L|M) dL$$

- The average relation between **light** and **mass**:

$$\langle L \rangle(M) = \int_0^\infty \Phi(L|M) L dL$$

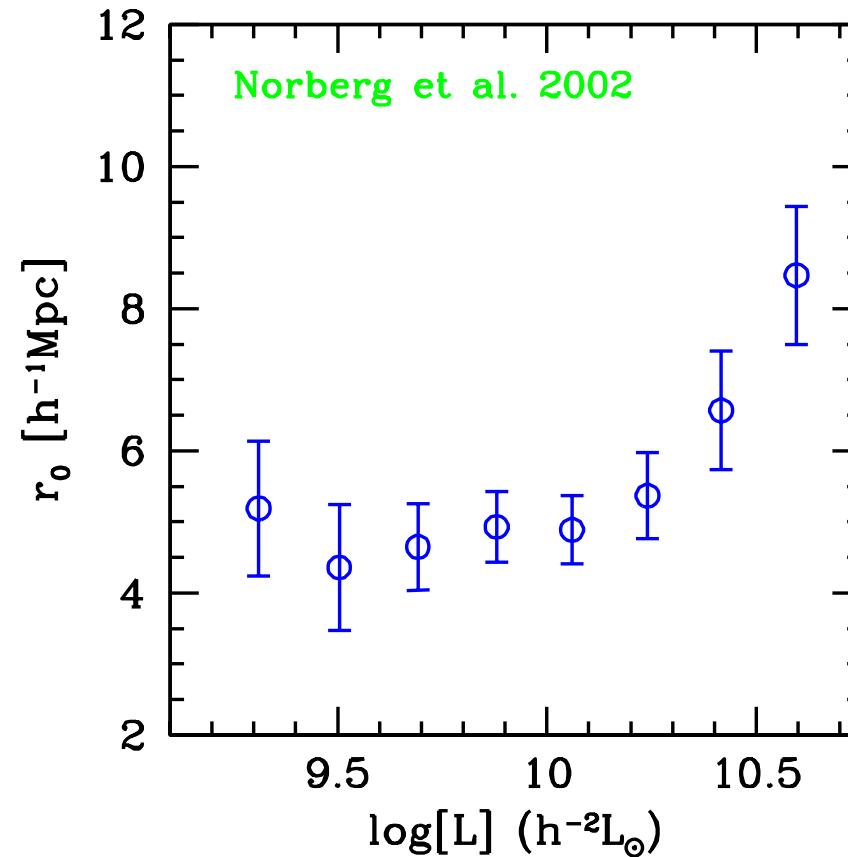
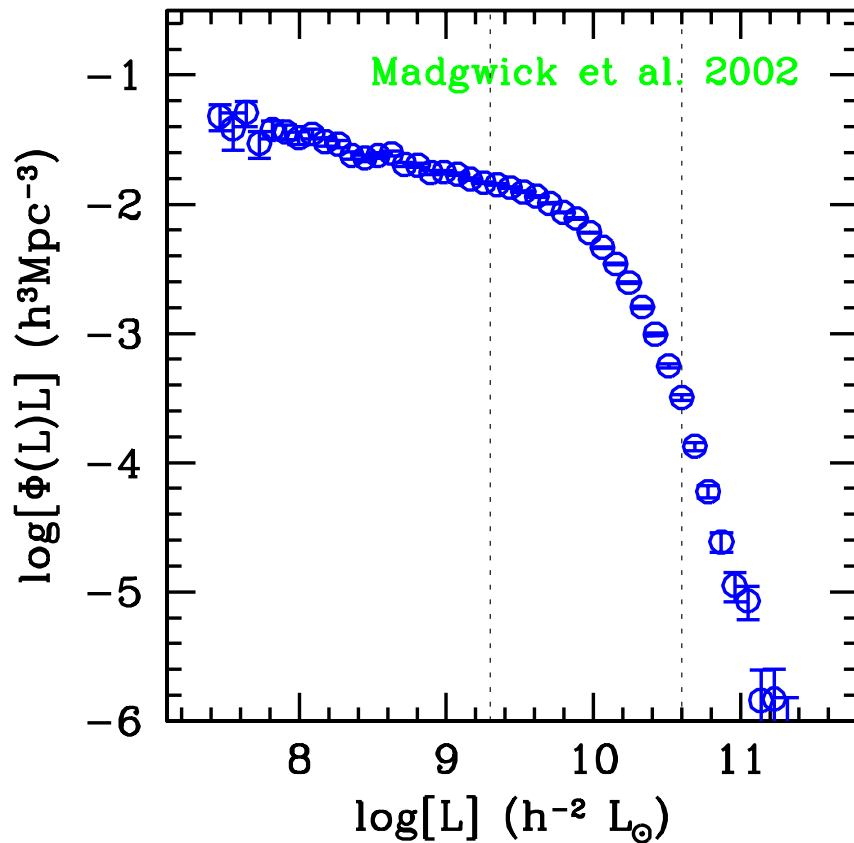
- Galaxy **clustering** properties as function of luminosity:

$$\xi_{gg}(r|L) = b^2(L) \xi_{dm}(r)$$

$$b(L) = \frac{1}{\Phi(L)} \int_0^\infty \Phi(L|M) b(M) n(M) dM$$

CLF is ideal statistical 'tool' to investigate Galaxy-Dark Matter Connection

Luminosity & Correlation Functions



- **2dFGRS:** More luminous galaxies are more strongly clustered.
- **Λ CDM:** More massive haloes are more strongly clustered.

More luminous galaxies reside in more massive haloes

REMINDER: Correlation length r_0 defined by $\xi(r_0) = 1$

The Model

- The LFs of clusters are well fit by a **Schechter** function
- The LF of all field galaxies has a **Schechter** form
- The halo mass function has a **Press-Schechter** form

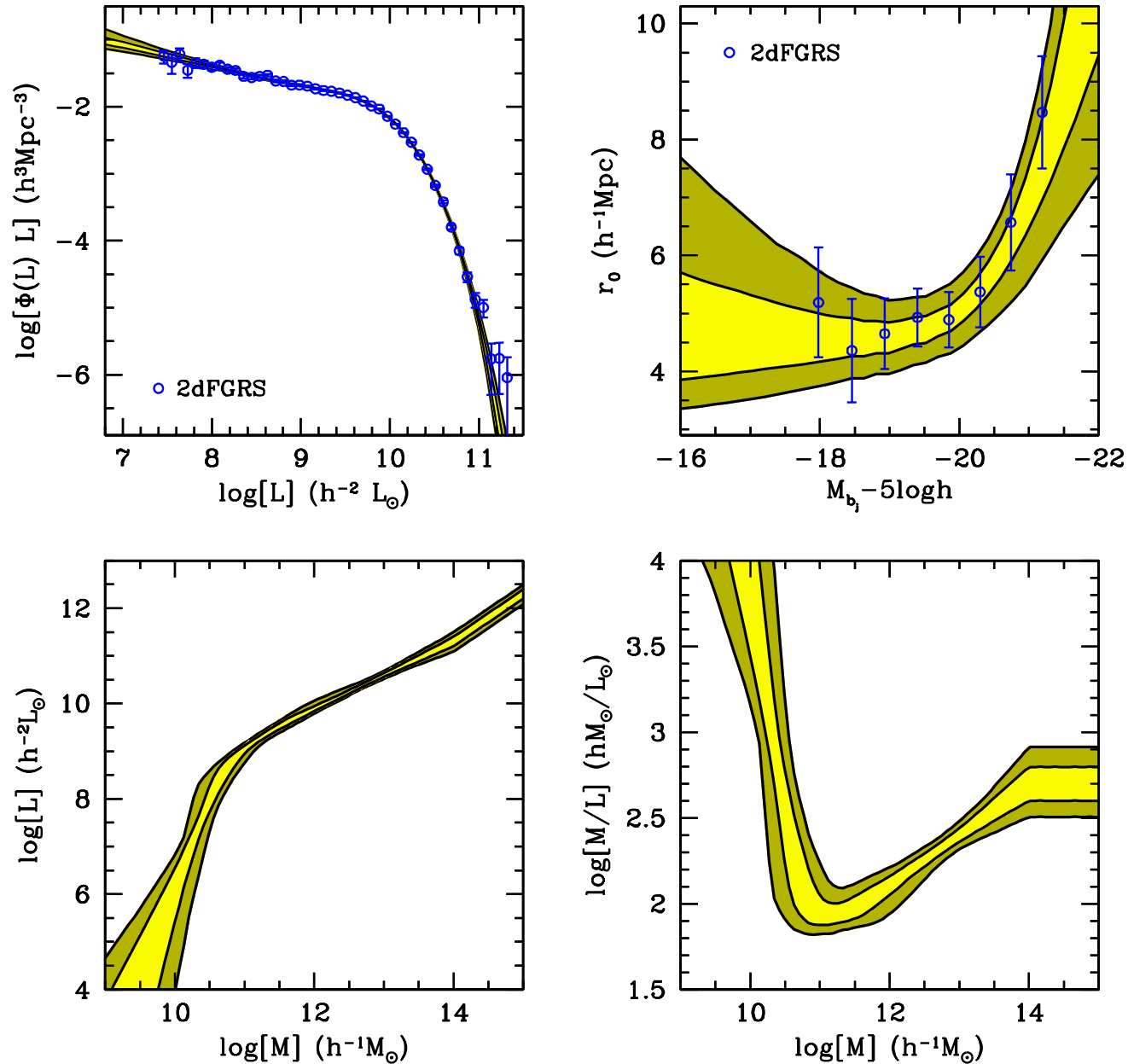
We therefore **assume** that the CLF also has the **Schechter** form:

$$\Phi(L|M)dL = \frac{\tilde{\Phi}^*}{\tilde{L}^*} \left(\frac{L}{\tilde{L}^*}\right)^{\tilde{\alpha}} \exp(-L/\tilde{L}^*) dL$$

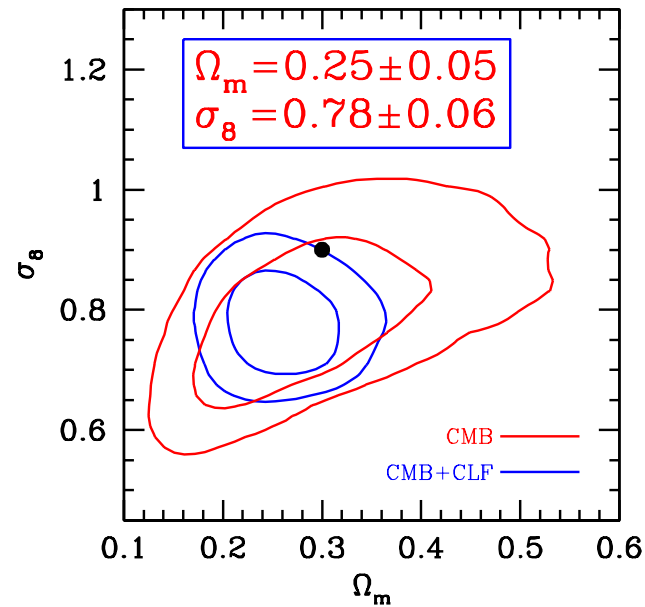
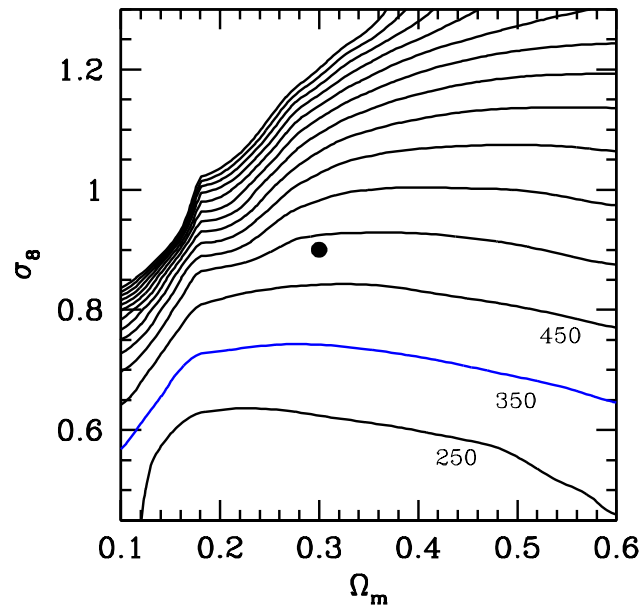
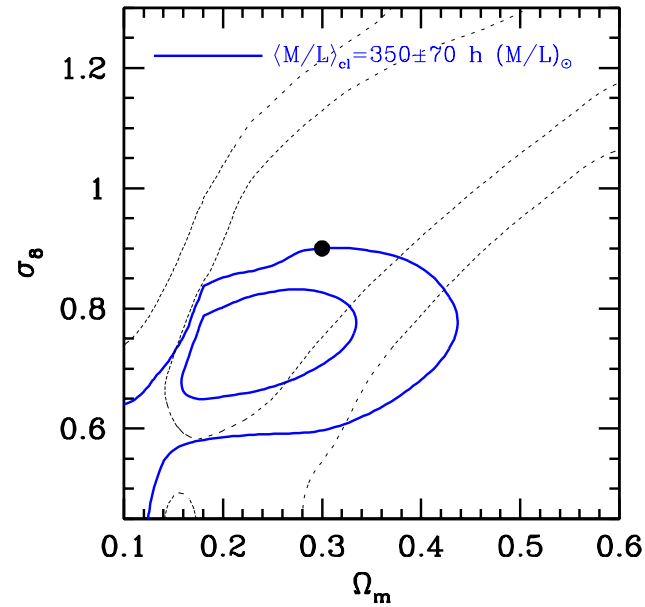
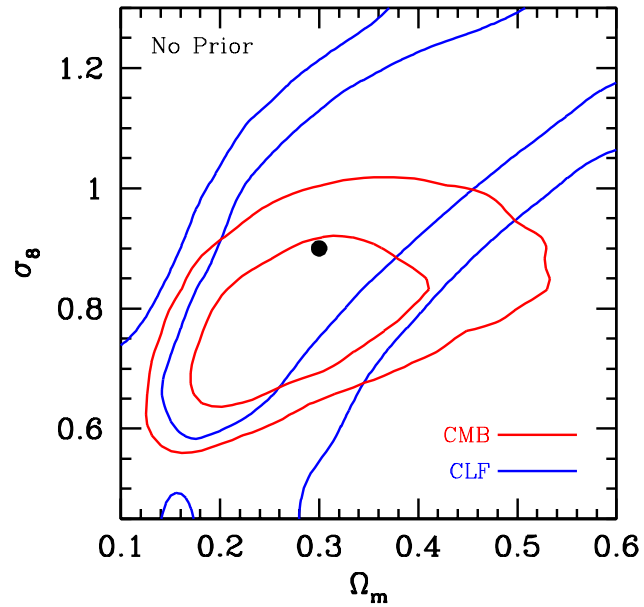
Here $\tilde{\Phi}^*$, \tilde{L}^* and $\tilde{\alpha}$ all depend on M .

- Parameterize $\tilde{\Phi}^*$, \tilde{L}^* and $\tilde{\alpha}$. In total our model has **8 free parameters**
- Construct **Monte-Carlo Markov Chain** to sample posterior distribution of free parameters. ($N_{\text{eq}} = 10^4$, $N_{\text{step}} = 4 \times 10^7$, $N_{\text{chain}} = 2000$)
- Use **MCMC** to put confidence levels on derived quantities such as $\langle M/L \rangle(M)$ and $\tilde{\alpha}(M)$.
- Use **MCMC** to explore **degeneracies** and **correlations** between various parameters.

The Relation between Light & Mass

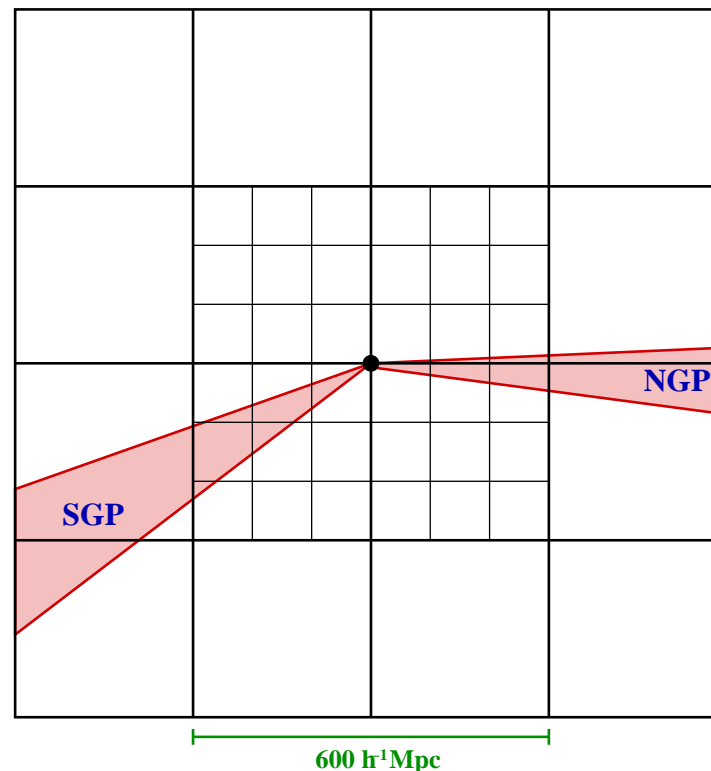


Constraints on Ω_m and σ_8



Constructing Mock Surveys

- Run **numerical simulations**: Λ CDM concordance cosmology; $L_{\text{box}} = 100h^{-1}$ Mpc and $L_{\text{box}} = 300h^{-1}$ Mpc with 512^3 CDM particles each.
- Identify **dark matter haloes** (**FOF** algorithm, $b = 0.2$).
- **Populate haloes** with galaxies using **CLF**.
- Stack boxes to create **virtual universe** and mimic observations (**magnitude limit, completeness, geometry**)



Large Scale Structure: Theory

Observations yield $\xi(r_p, \pi)$ with r_p and π the pair separations perpendicular and parallel to the line-of-sight.

redshift space CF: $\xi(s)$ with $s = \sqrt{r_p^2 + \pi^2}$.

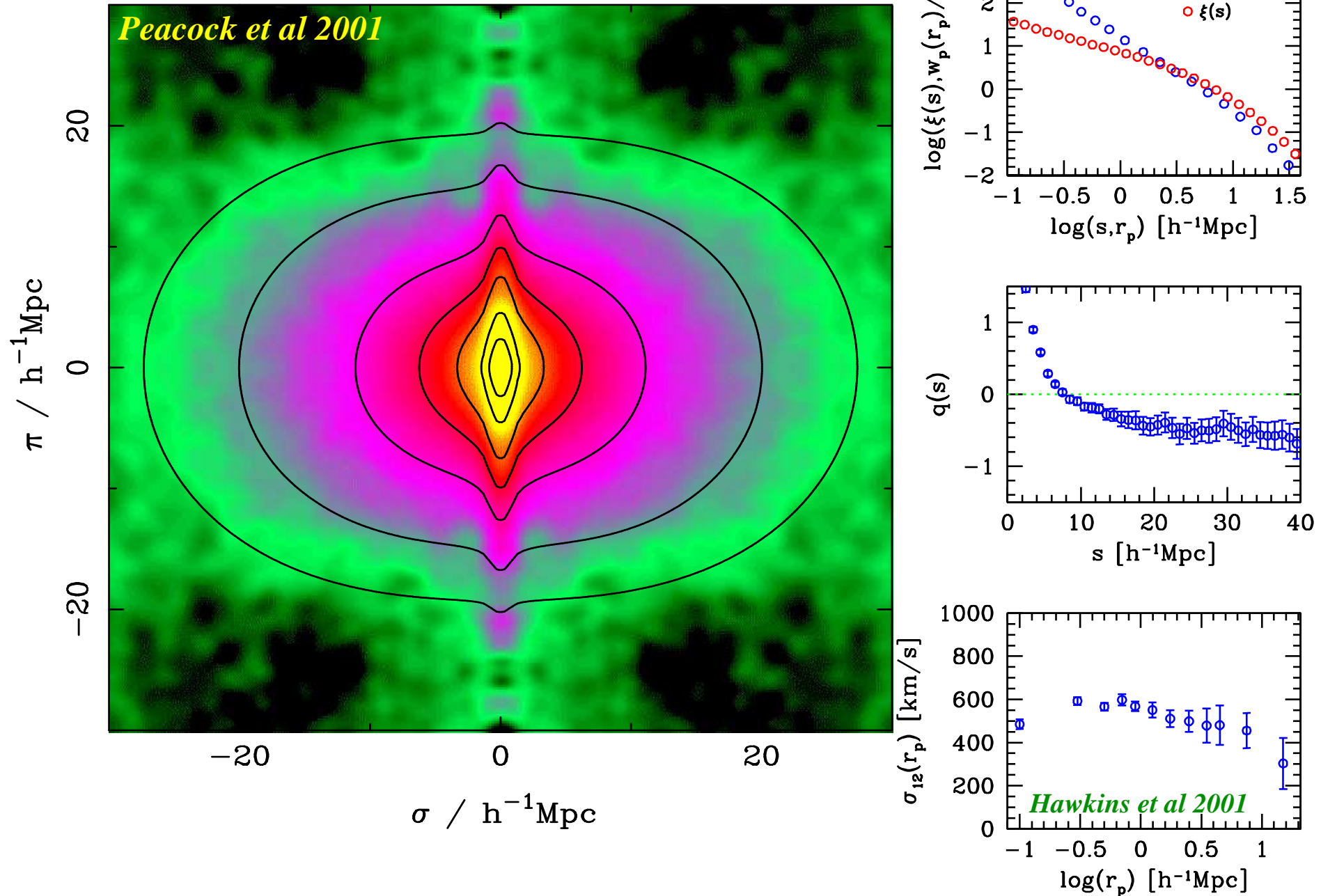
$$\text{projected CF: } w_p(r_p) = \int_{-\infty}^{\infty} \xi(r_p, \pi) d\pi = 2 \int_{r_p}^{\infty} \xi(r) \frac{r dr}{\sqrt{r^2 - r_p^2}}$$

Peculiar velocities cause anisotropy of $\xi(r_p, \pi)$ and differences between $\xi(s)$ and $\xi(r)$.

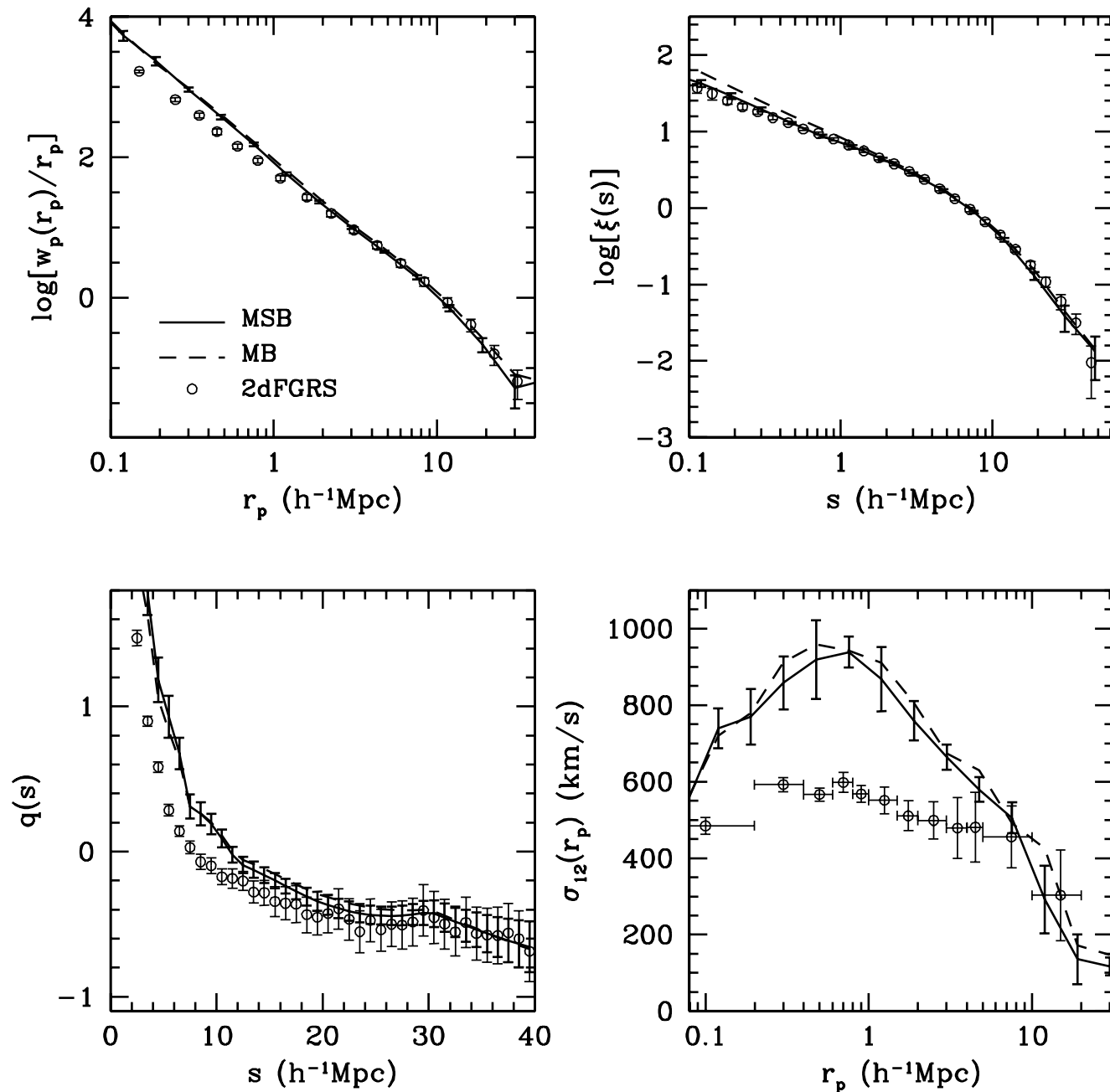
Anisotropy of $\xi(r_p, \pi)$ is quantified by **quadrupole-to-monopole ratio** denoted by $q(s)$.

- **Large Scales:** Infall (“Kaiser Effect”); boosts $\xi(s)$ w.r.t. $\xi(r)$. $q(s)$ is negative and a measure of $\beta \equiv \Omega_m^{0.6} / b$.
- **Small Scales:** Virialized motion (“Finger-of-God”); suppresses $\xi(s)$ w.r.t. $\xi(r)$. $q(s)$ is positive and a measure for the **pairwise velocity dispersions** (PVDs) denoted by σ_{12} .

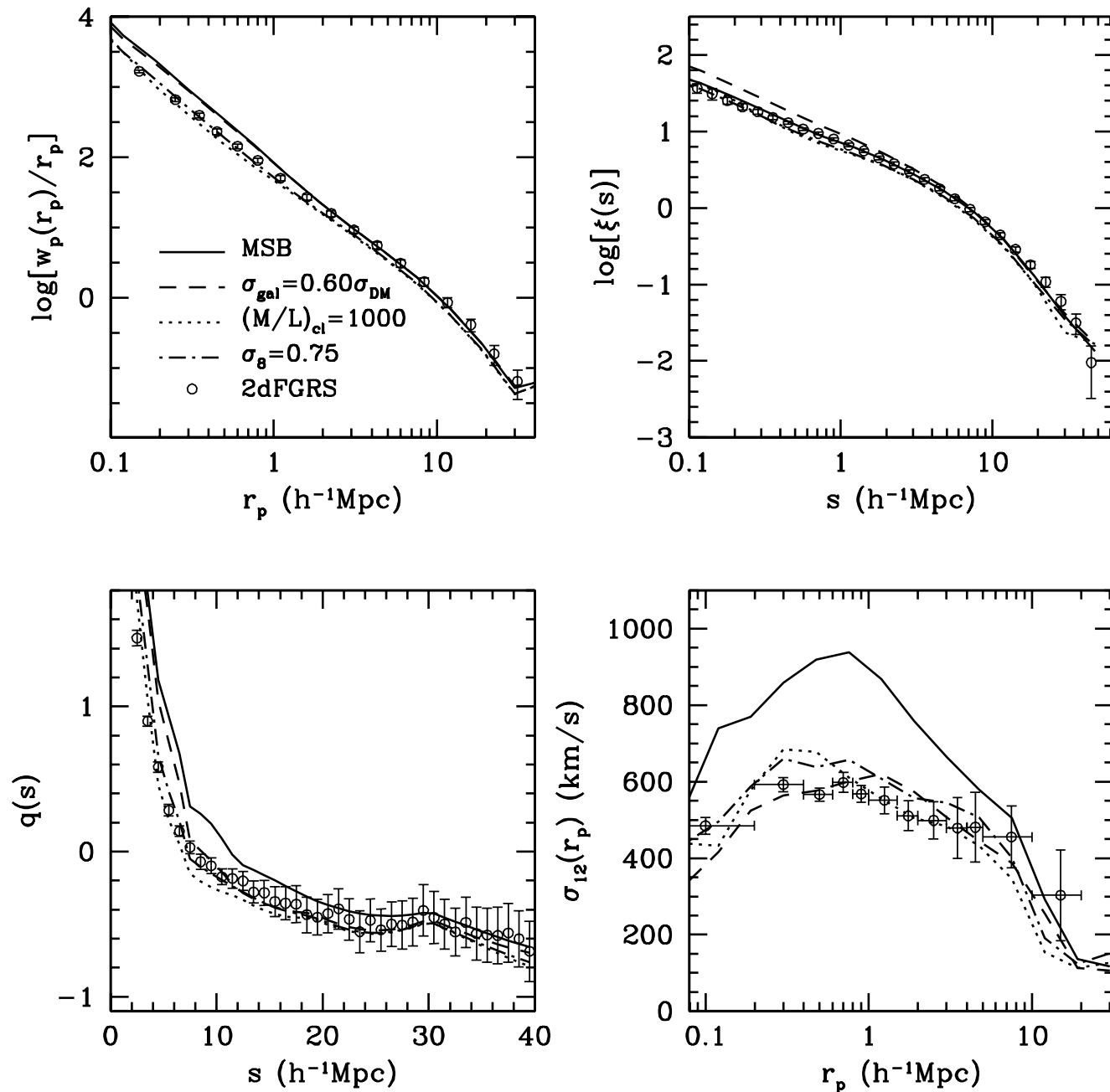
Large Scale Structure: The 2dFGRS



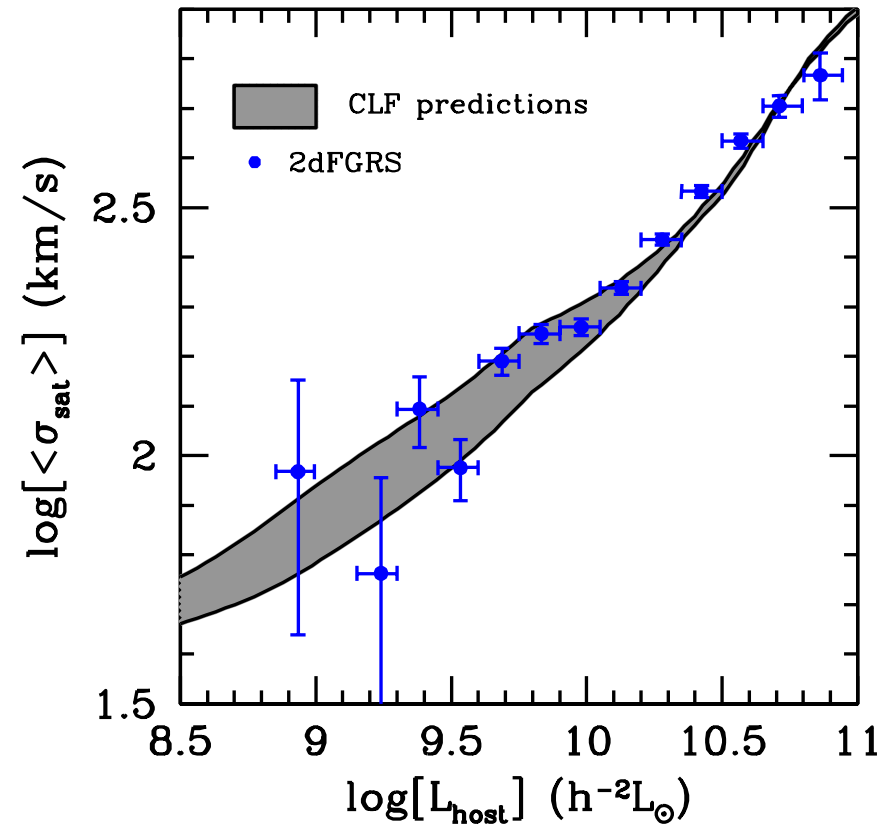
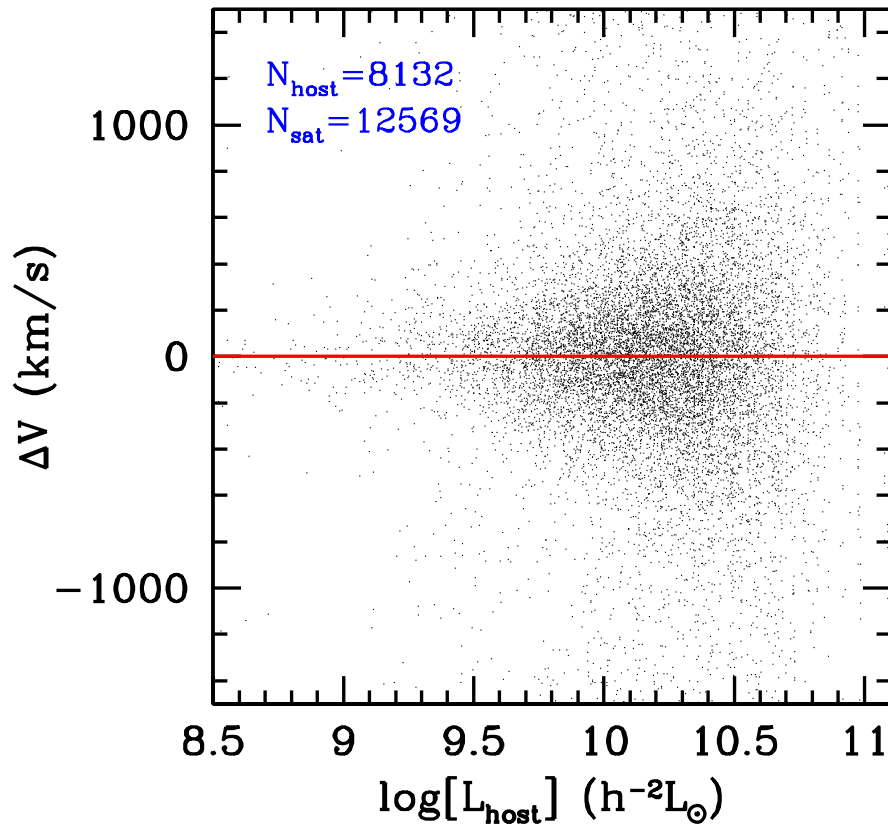
Mock versus 2dFGRS: round 1



Mock versus 2dFGRS: round 2



Satellite Kinematics in the 2dFGRS



- Mocks are used to **optimize** host-satellite selection criteria
- Using an **iterative, adaptive** selection criterion **minimizes** interlopers
- Application to **2dFGRS** yields 12569 satellites & 8132 hosts
- Independent **dynamical evidence** to support CLF results

vdB, Norberg, Mo & Yang, 2004, MNRAS, 352, 1302

vdB, Yang, Mo & Norberg, 2005, MNRAS, 356, 1233

Conclusions: CLF

- $\Phi(L|M)$ is a powerful **statistical** tool. It is strongly constrained by $\Phi(L)$ and $r_0(L)$ (Yang, Mo & vdB 2003)
- $\Phi(L|M)$ yields **mass-to-light ratios** $\langle M/L \rangle(M)$ and **galaxy bias** as function of luminosity, type, etc (vdB, Yang & Mo 2003)
- Relation between mass and light inferred from $\Phi(L|M)$ in excellent agreement with **satellite kinematics** (vdB, Norberg, Mo & Yang 2004)
- $\Phi(L|M)$ ideal to construct **mock galaxy redshift surveys** and to study **large scale structure** (Yang, Mo, Jing, vdB & Chu 2004)
- There are two **characteristic scales** in **Galaxy Formation**, at $\sim 10^{11} h^{-1} M_{\odot}$ and $\sim 10^{13} h^{-1} M_{\odot}$. (vdB, Yang, Mo & Norberg 2005; Yang, Mo, vdB & Jing 2005)

The Λ CDM concordance cosmology predicts too many massive clusters, unless $\langle M/L \rangle_{cl} \simeq 1000h (M/L)_{\odot}$ or $\sigma_8 \simeq 0.75$.
