

# The Galaxy–Dark Matter Connection

constraining cosmology & galaxy formation



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# Outline, Motivation & Techniques

## Why study the Galaxy-Dark Matter Connection?

- To constrain the physics of **Galaxy Formation**
- To constrain **Cosmological Parameters**



## Two Methods to Constrain Galaxy-Dark Matter Connection

- Large Scale Structure
- Galaxy-Galaxy Lensing

## New Cosmological Constraints

- Precision cosmology using **non-linear** structure

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● Outline, Motivation & Techniques

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# The Conditional Luminosity Function

In order to parameterize the Halo Occupation Statistics we introduce the **Conditional Luminosity Function** (CLF),  $\Phi(L|M)$ , which is the direct link between the halo mass function  $n(M)$  and the galaxy luminosity function  $\Phi(L)$ :

$$\Phi(L) = \int_0^\infty \Phi(L|M) n(M) dM$$

The CLF contains a wealth of information, such as:

- The average relation between **light** and **mass**:

$$\langle L \rangle(M) = \int_0^\infty \Phi(L|M) L dL$$

- The occupation numbers of galaxies:

$$\langle N \rangle(M) = \int_{L_{\min}}^\infty \Phi(L|M) dL$$

We have constrained CLF using four different, independent techniques

**Galaxy Group Catalogues**

**Large Scale Structure**

**Satellite Kinematics**

**Galaxy-Galaxy Lensing**

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# The CLF Model

Motivated by results obtained from **galaxy group catalogue**, we split CLF in **central** and **satellite** components

$$\Phi(L|M)dL = \Phi_c(L|M)dL + \Phi_s(L|M)dL$$

- For **centrals** we adopt a log-normal distribution

$$\Phi_c(L|M)dL = \frac{1}{\sqrt{2\pi}\sigma_c} \exp\left[-\left(\frac{\ln(L/L_c)}{\sqrt{2}\sigma_c}\right)^2\right] \frac{dL}{L}$$

- For **satellites** we adopt a modified Schechter function

$$\Phi_s(L|M)dL = \frac{\Phi_s}{L_s} \left(\frac{L}{L_s}\right)^{\alpha_s} \exp[-(L/L_s)^2] dL$$

Note that  $L_c$ ,  $L_s$ ,  $\sigma_c$ ,  $\phi_s$  and  $\alpha_s$  all depend on halo mass  $M$

Free parameters are constrained by fitting data

Use **Monte-Carlo Markov Chain** to sample the posterior distribution of free parameters, and to put confidence levels on derived quantities

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# Occupation Statistics from Clustering

- Galaxies occupy dark matter halos.
- CDM: more massive halos are more strongly clustered.
- Clustering strength of given population of galaxies indicates the characteristic halo mass

Clustering strength measured by correlation length  $r_0$

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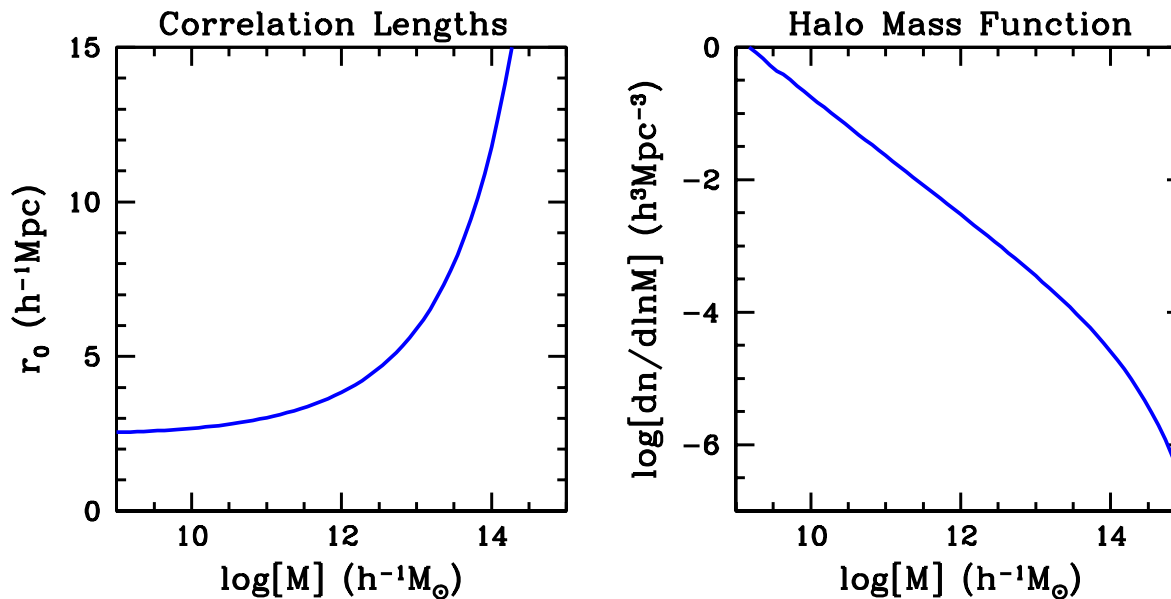
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# Occupation Statistics from Clustering

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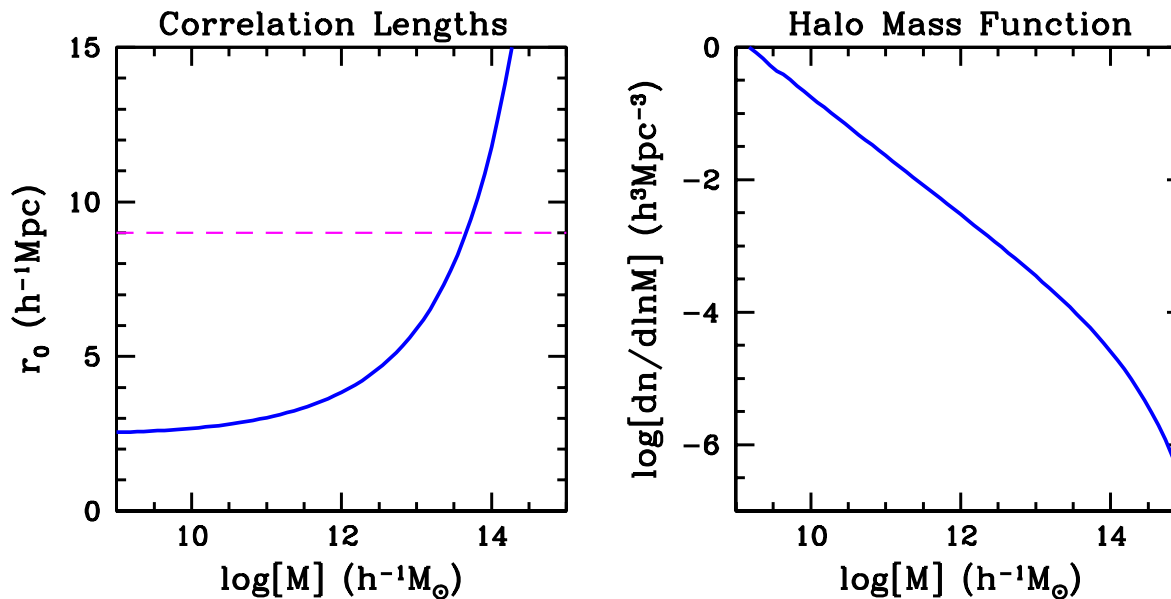
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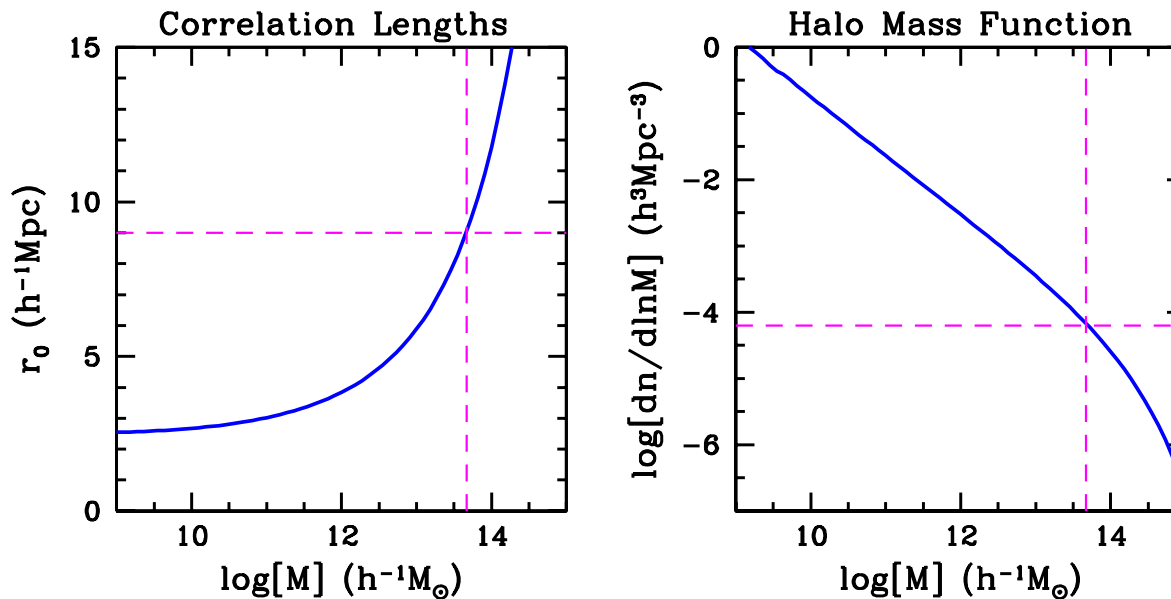
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# Occupation Statistics from Clustering

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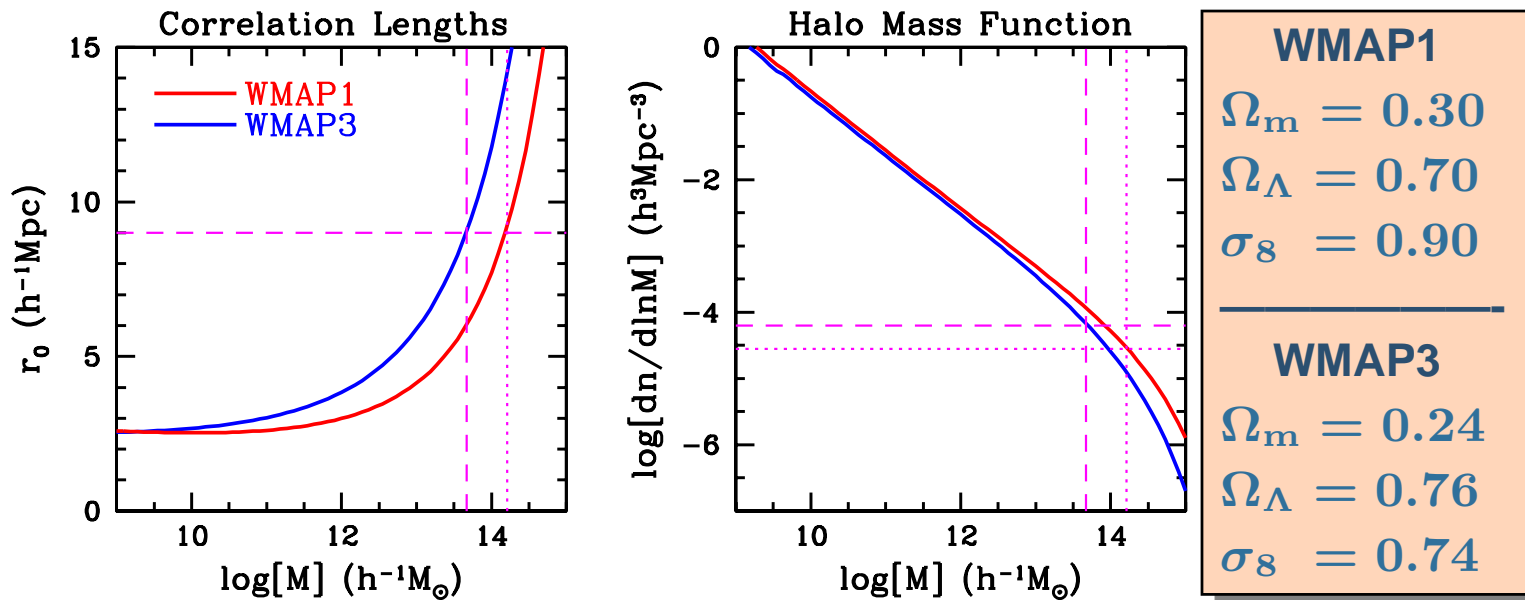




# Occupation Statistics from Clustering

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Clustering strength measured by correlation length  $r_0$



CAUTION: Results depend on cosmological parameters

# Luminosity & Correlation Functions

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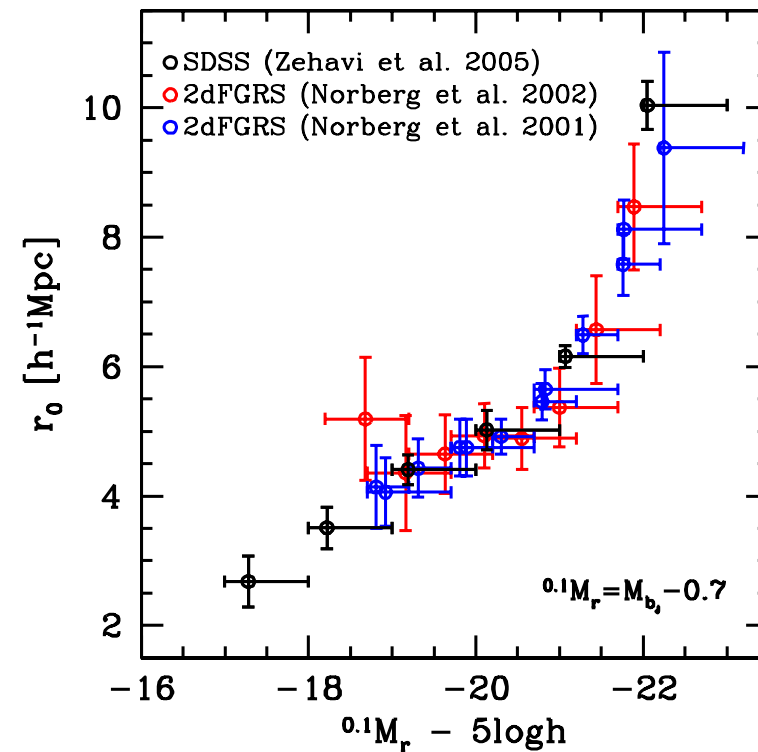
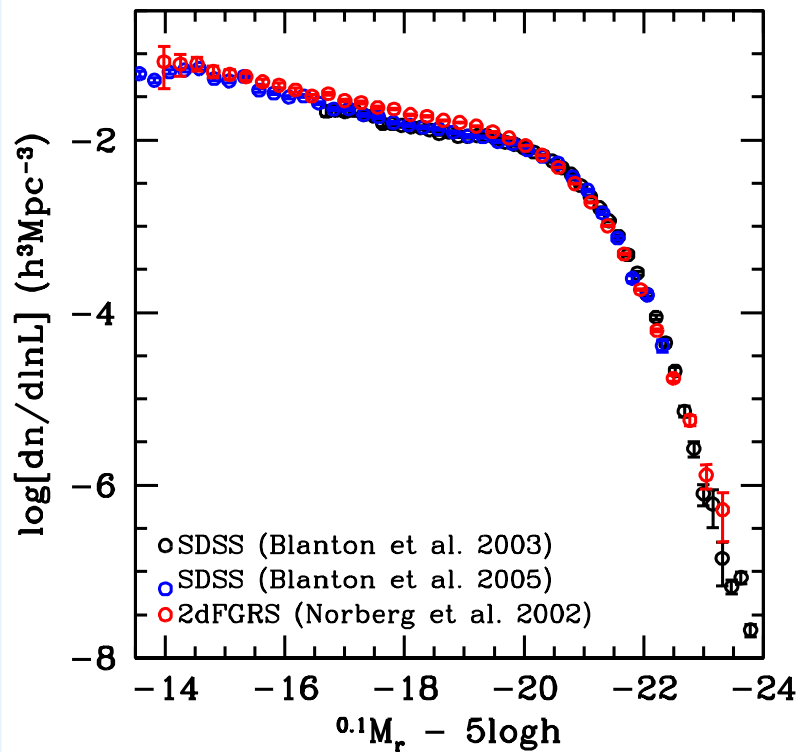
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- **DATA:** More luminous galaxies are more strongly clustered.
- **$\Lambda$ CDM:** More massive haloes are more strongly clustered.

More luminous galaxies reside in more massive haloes

**REMINDER:** Correlation length  $r_0$  defined by  $\xi(r_0) = 1$

# Results

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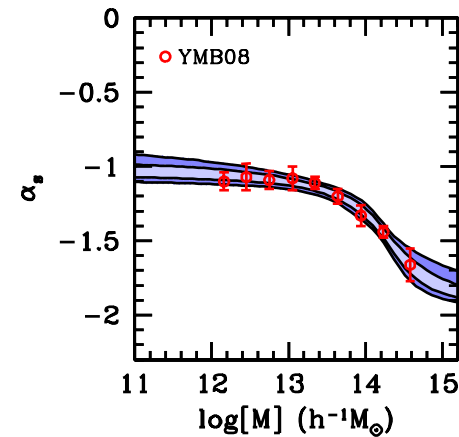
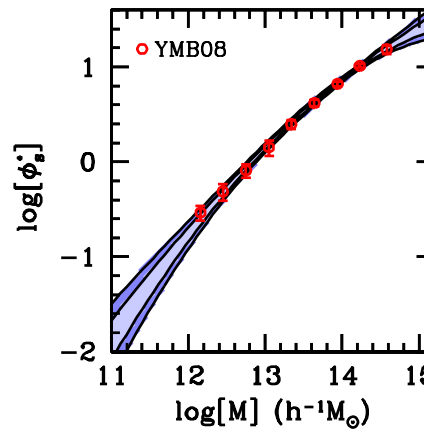
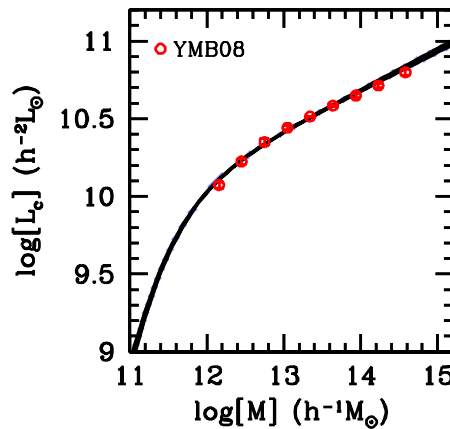
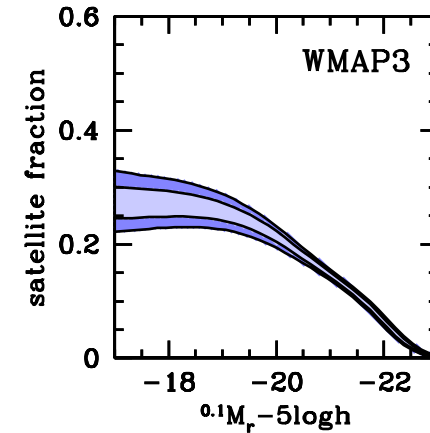
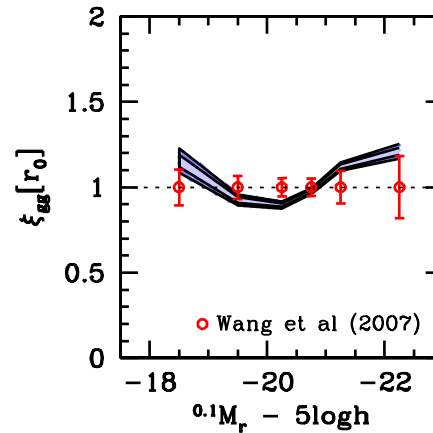
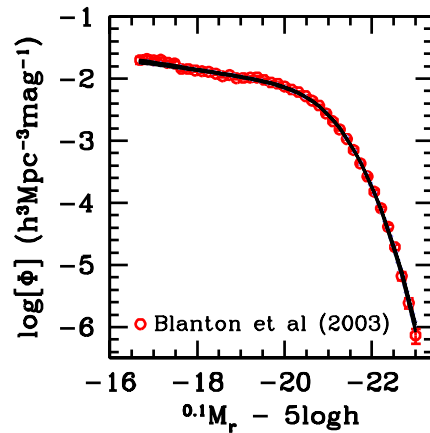
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(Cacciato, vdB et al. 2008)

**Model fits data extremely well with  $\chi_{\text{red}}^2 \sim 1$**   
**Same model in excellent agreement with results from SDSS galaxy group catalogue of Yang et al. (2008)**

# Cosmology Dependence

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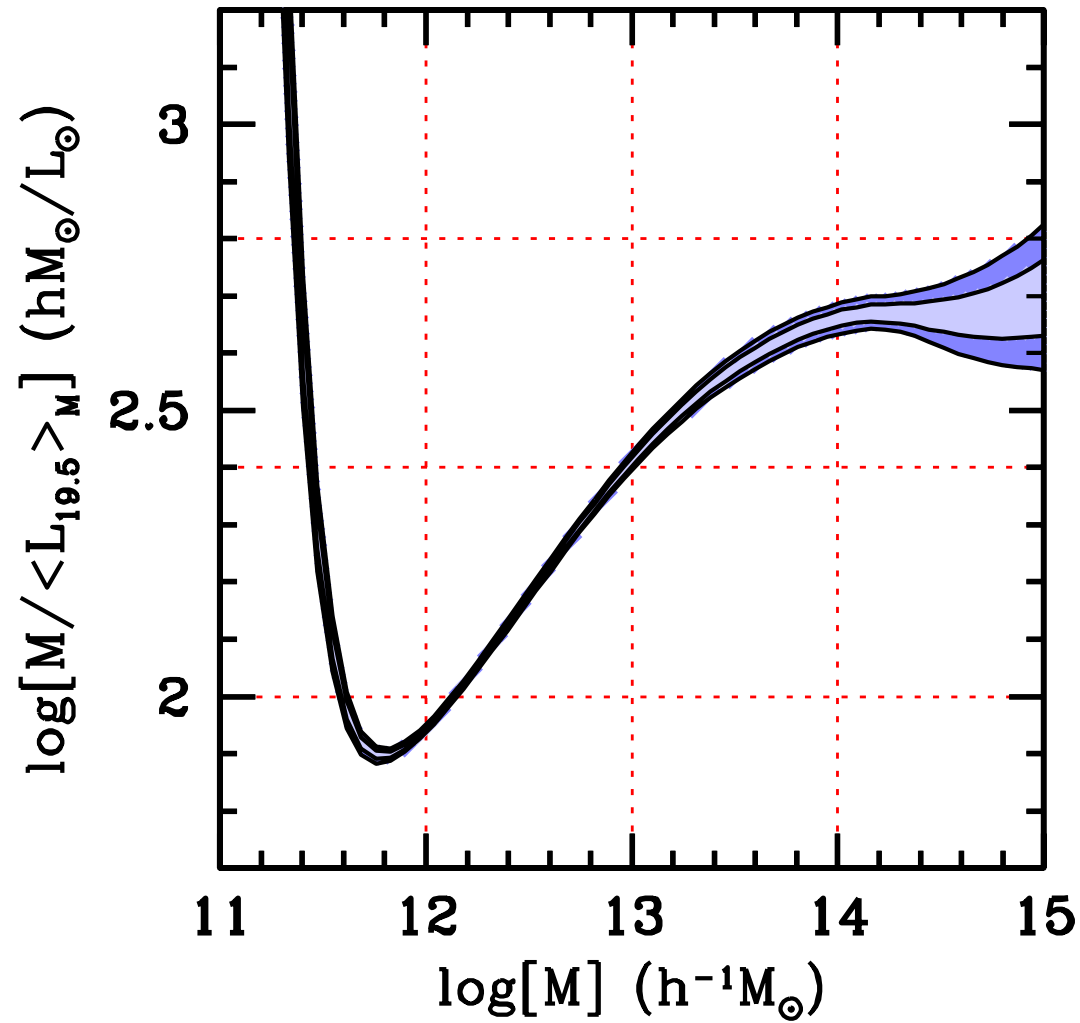
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# Cosmology Dependence

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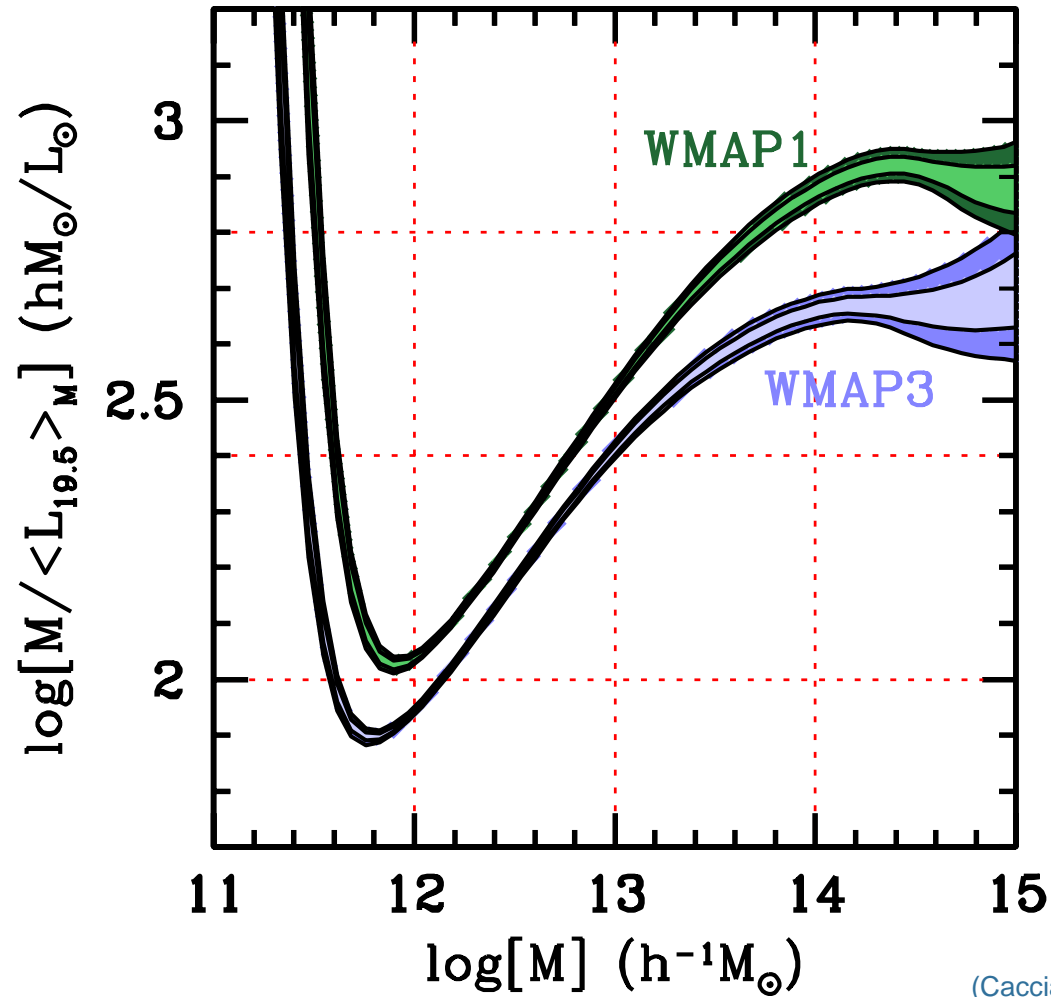
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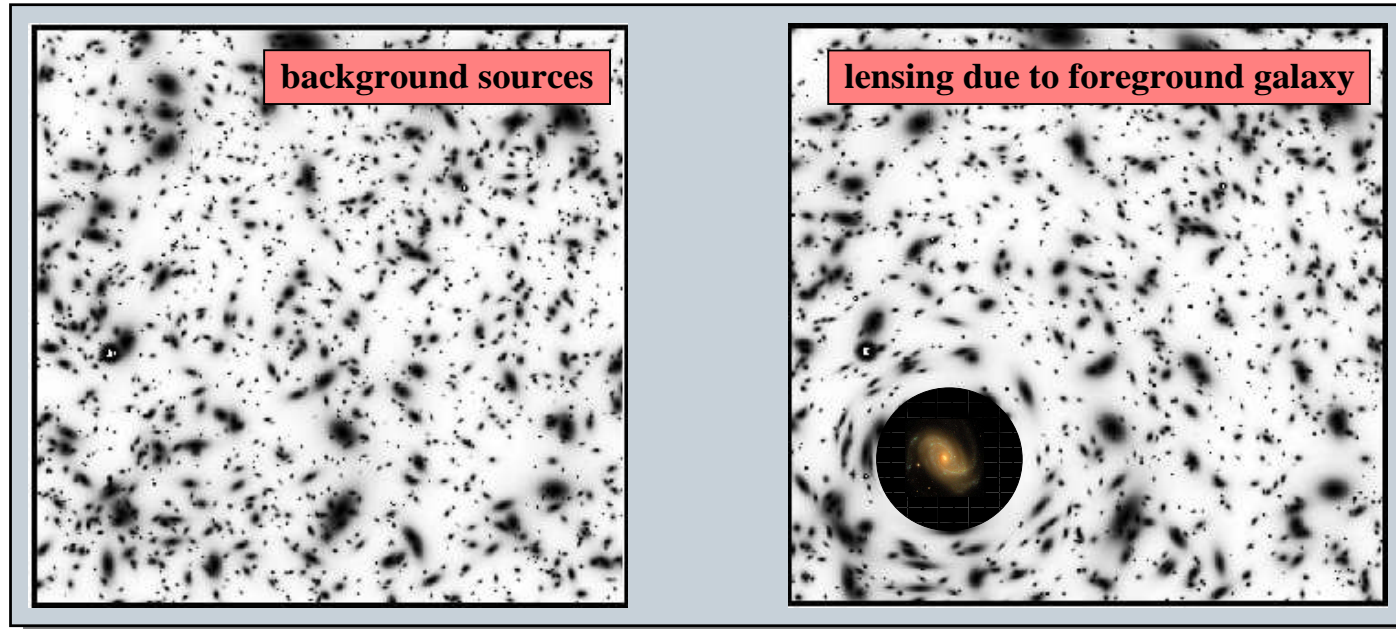


(Cacciato, vdB et al. 2008)

**Mass-to-Light ratios tightly constrained,  
but with strong dependence on cosmology**

# Galaxy-Galaxy Lensing

The mass associated with galaxies lenses background galaxies



Lensing causes correlated ellipticities, the **tangential shear**,  $\gamma_t$ , which is related to the **excess surface density**,  $\Delta\Sigma$ , according to

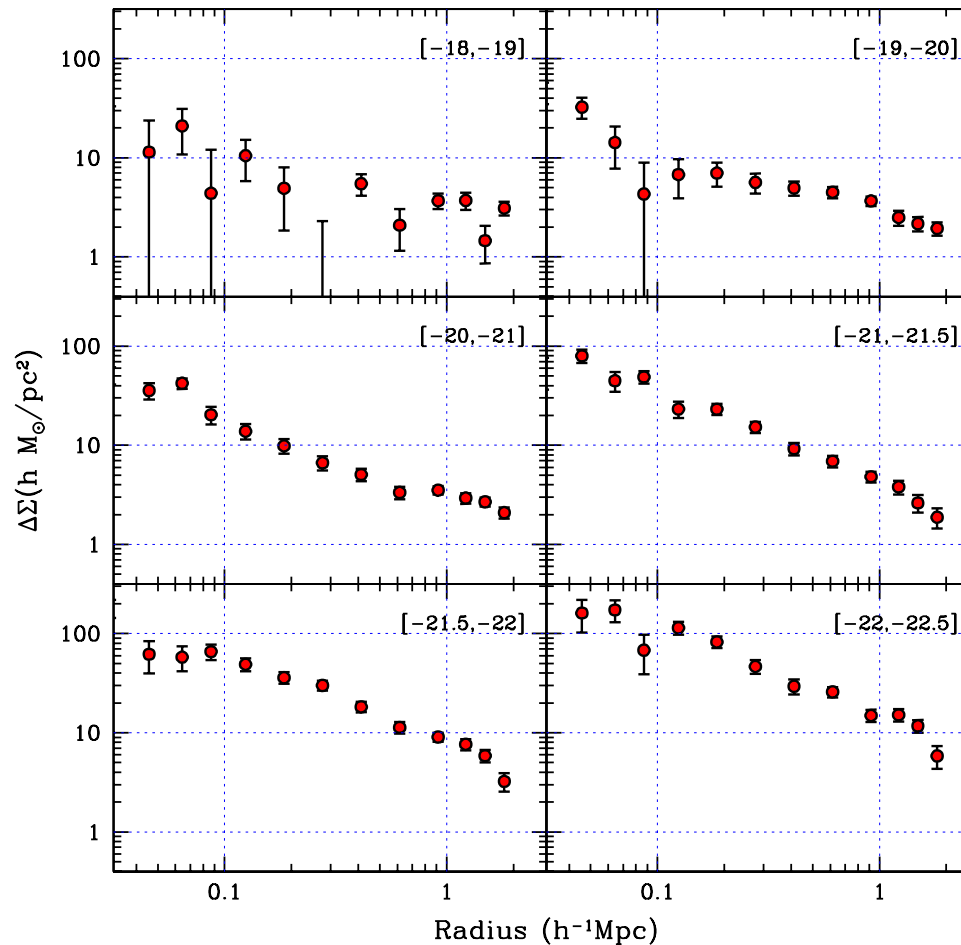
$$\gamma_t(R) \Sigma_{\text{crit}} = \Delta\Sigma(R) = \bar{\Sigma}(< R) - \Sigma(R)$$

$\Sigma(R)$  is line-of-sight projection of **galaxy-matter cross correlation**:

$$\Sigma(R) = \bar{\rho} \int_0^{D_S} [1 + \xi_{g, \text{dm}}(r)] d\chi$$

# The Measurements

- Number of background sources per lens is limited.
- Measuring  $\gamma_t$  with sufficient  $S/N$  requires **stacking** of many lenses
- $\Delta\Sigma(R|L_1, L_2)$  has been measured using the **SDSS** by Mandelbaum et al. (2005) for different bins in lens luminosity



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• Comparison with CLF

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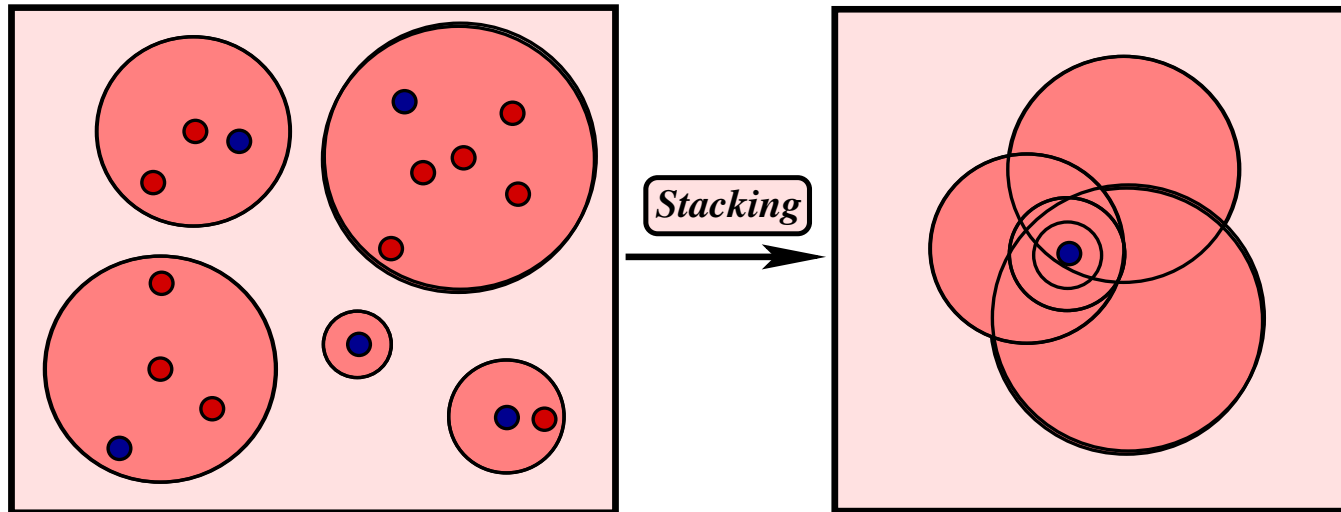
• WMAP3 vs. WMAP1

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# How to interpret the signal?



Because of **stacking** the lensing signal is difficult to interpret

In order to model the data, what is required is:

$$P_{\text{cen}}(M|L) \quad P_{\text{sat}}(M|L) \quad f_{\text{sat}}(L)$$

These can all be computed from the **CLF**

Using  $\Phi(L|M)$  constrained from **clustering data**, we can predict the **lensing signal**  $\Delta\Sigma(R|L_1, L_2)$



# Comparison with CLF Predictions

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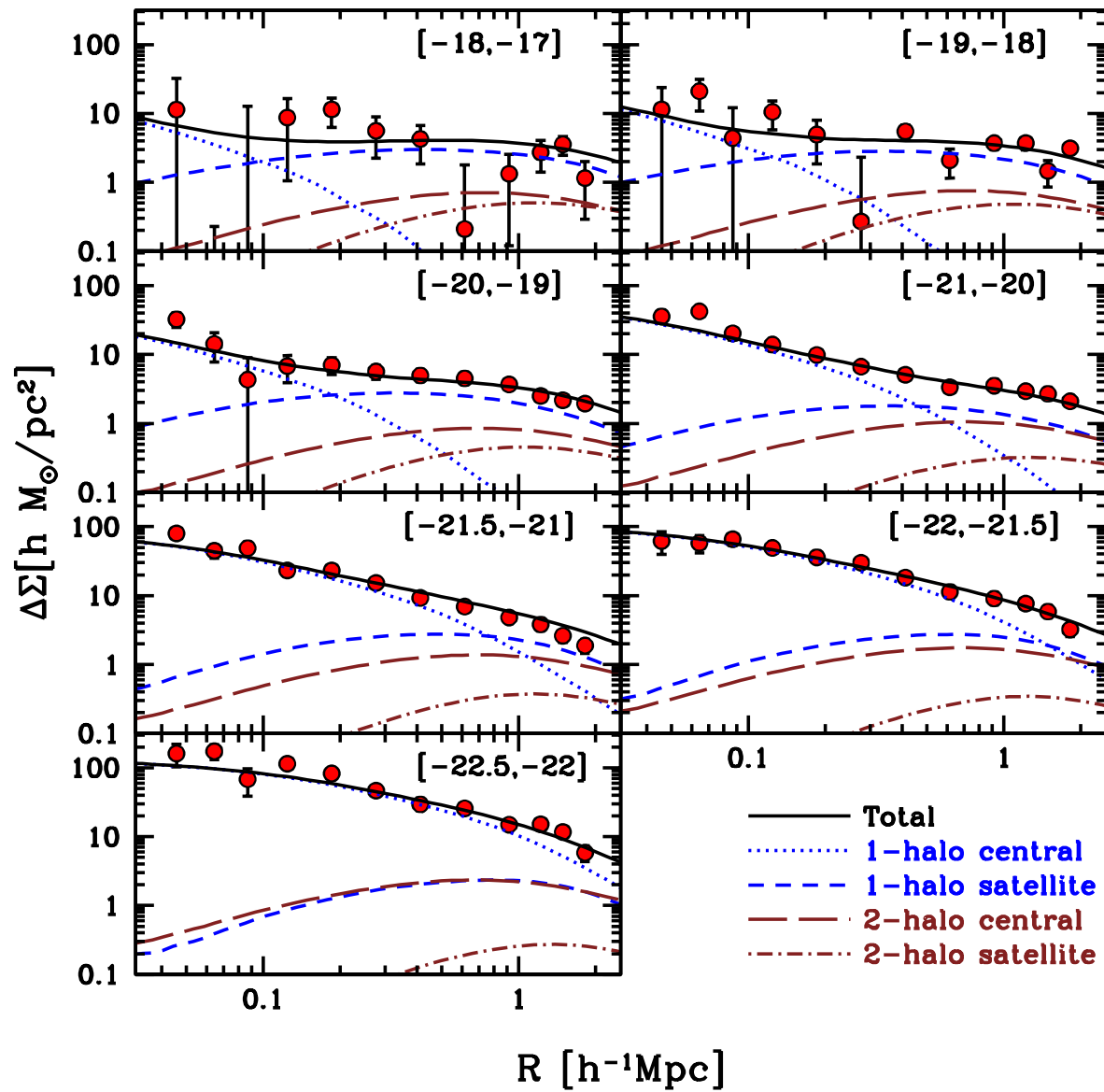
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**NOTE:** This is not a fit, but a prediction based on CLF

# Comparison with CLF Predictions

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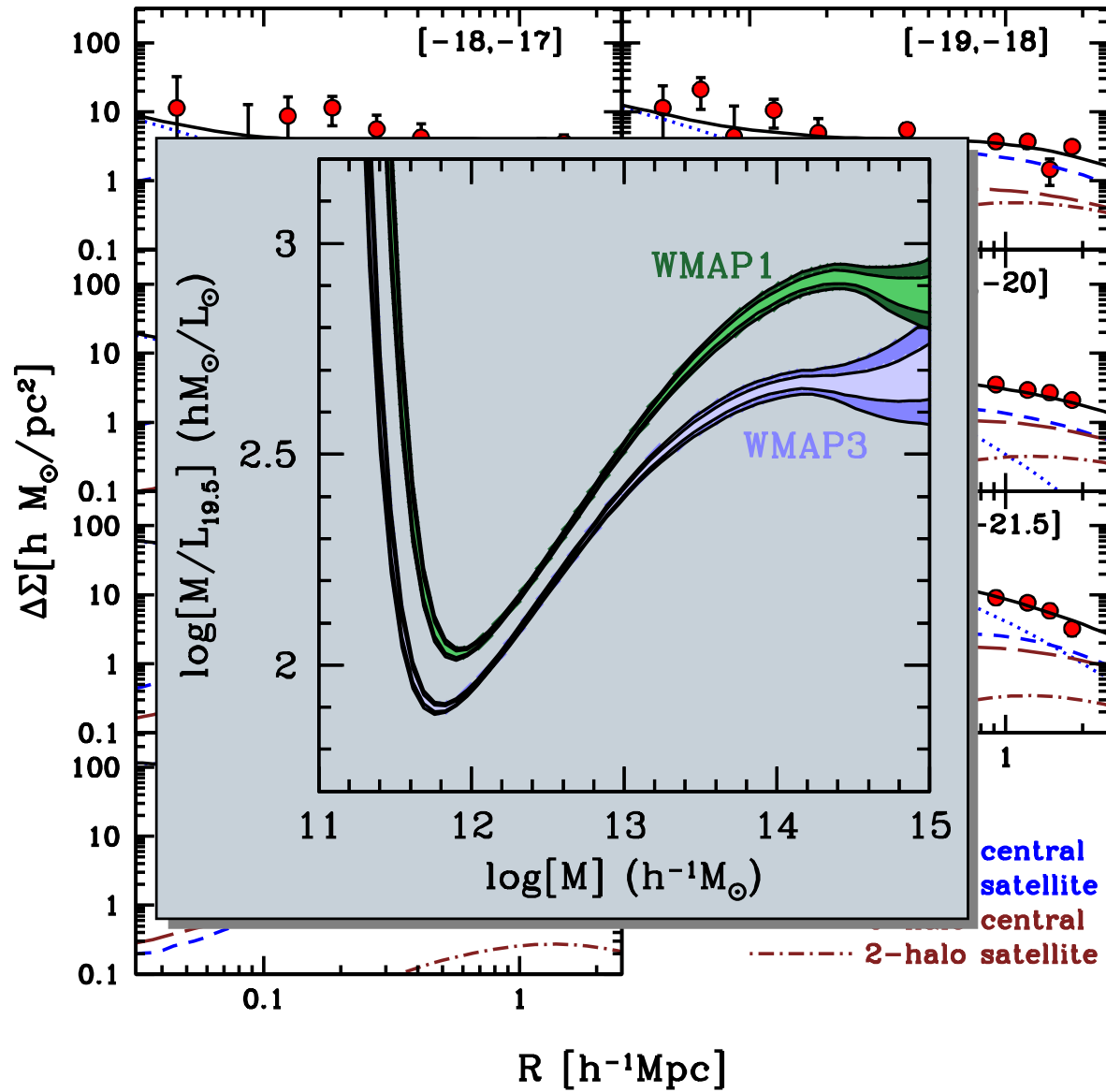
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**NOTE:** This is not a fit, but a prediction based on CLF

# WMAP3 vs. WMAP1

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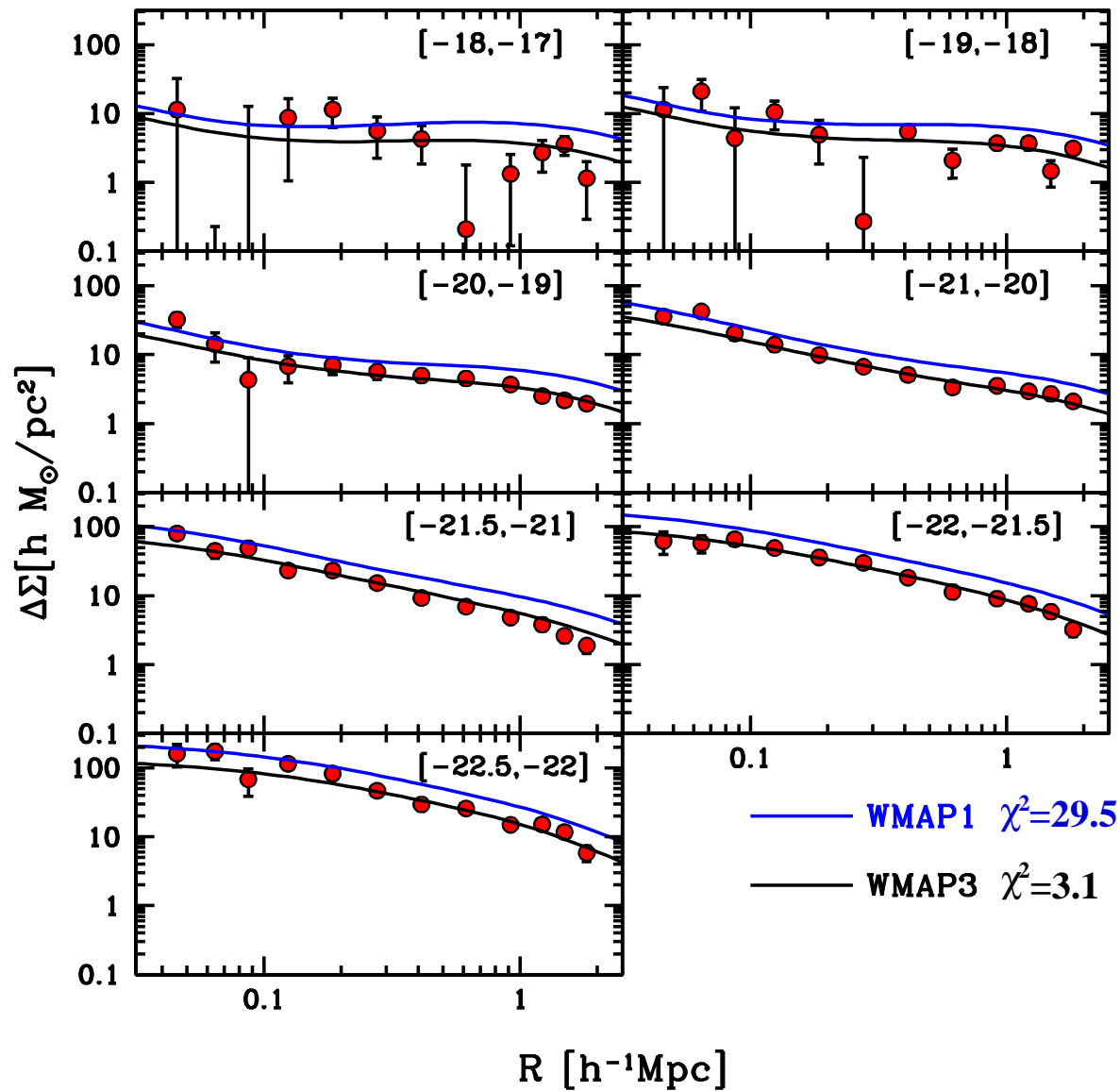
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**WMAP3 cosmology clearly preferred over WMAP1 cosmology**



# Cosmological Constraints

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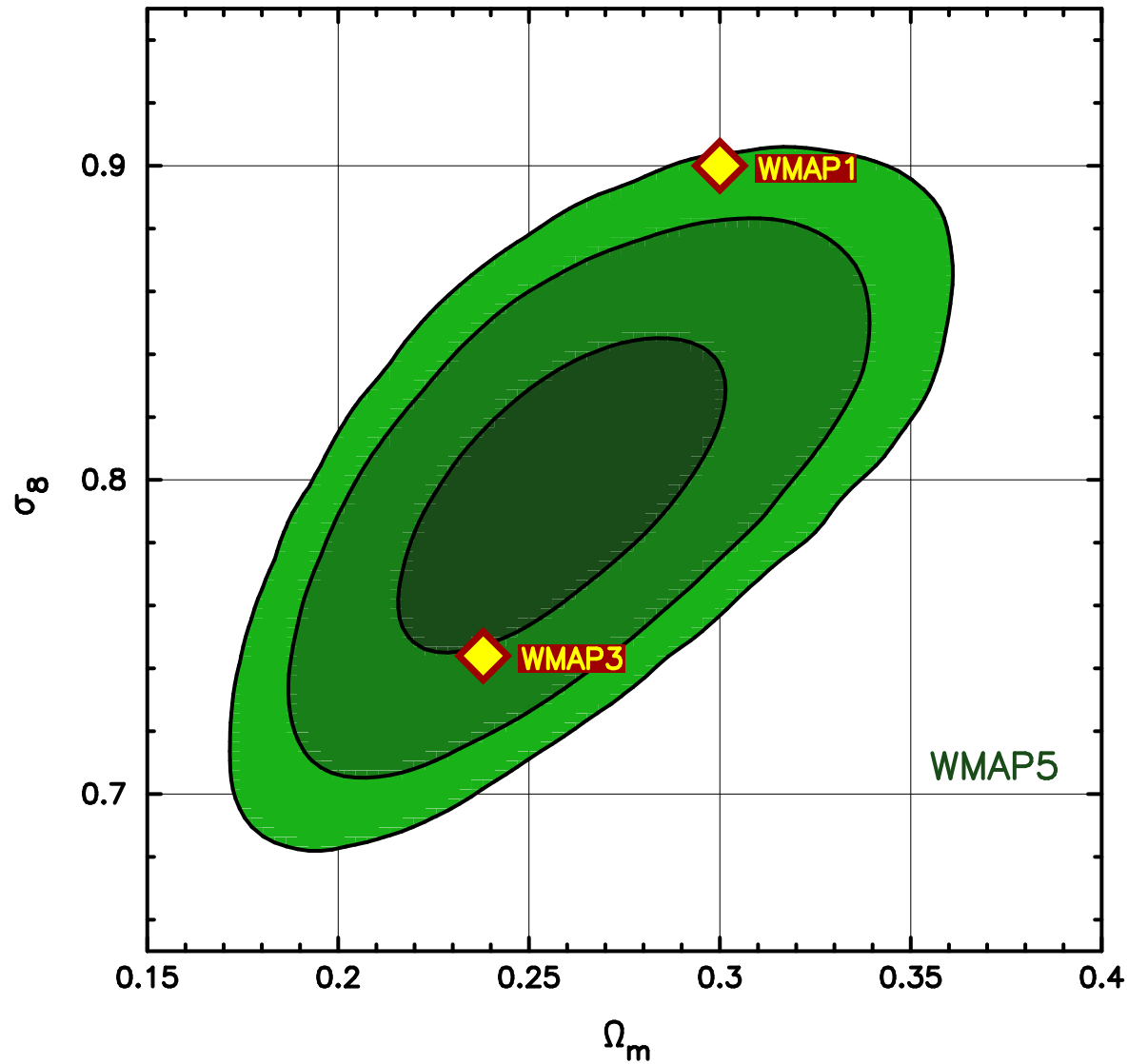
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● **Cosmological Constraints**

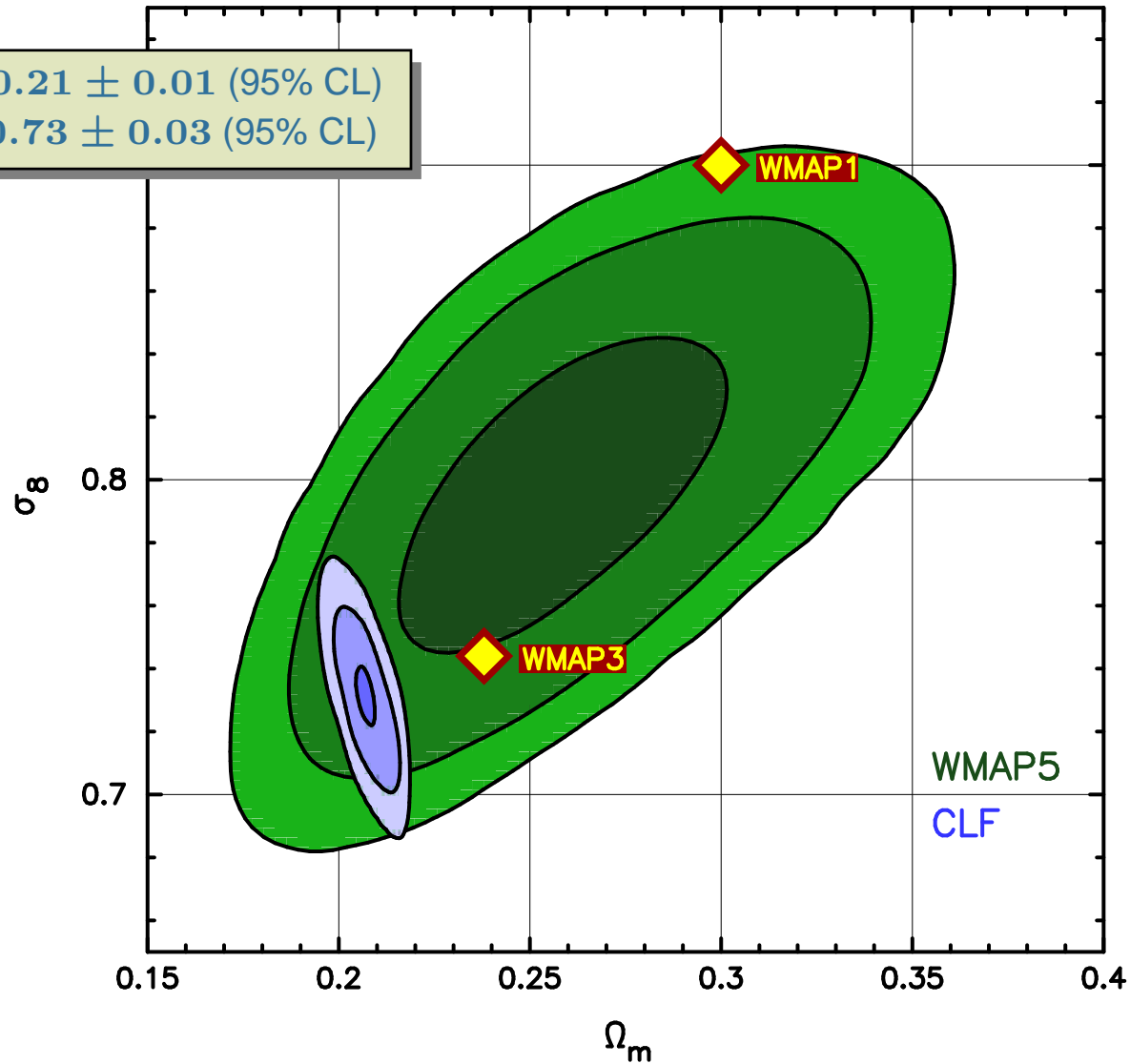
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# Cosmological Constraints

$\Omega_m = 0.21 \pm 0.01$  (95% CL)  
 $\sigma_8 = 0.73 \pm 0.03$  (95% CL)



**Precision Cosmology using non-linear structure!!**

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# Conclusions

For a given cosmology, luminosity dependence of clustering yields tight constraints on **CLF**, and thus on **galaxy formation**

Combining **clustering** and **galaxy-galaxy lensing** we obtain tight constraints on cosmological parameters, which are in excellent agreement with **CMB** constraints

Current (**preliminary**) results suggest

$$\begin{aligned}\Omega_m &= 0.21 \pm 0.01 \text{ (95\% CL)} \\ \sigma_8 &= 0.73 \pm 0.03 \text{ (95\% CL)}\end{aligned}$$

This technique is competitive with and complementary to **BAO**, **cosmic shear**, **SN Ia** and **Ly $\alpha$  forest**

If anything, our results indicate that our model for structure formation is accurate on non-linear scales

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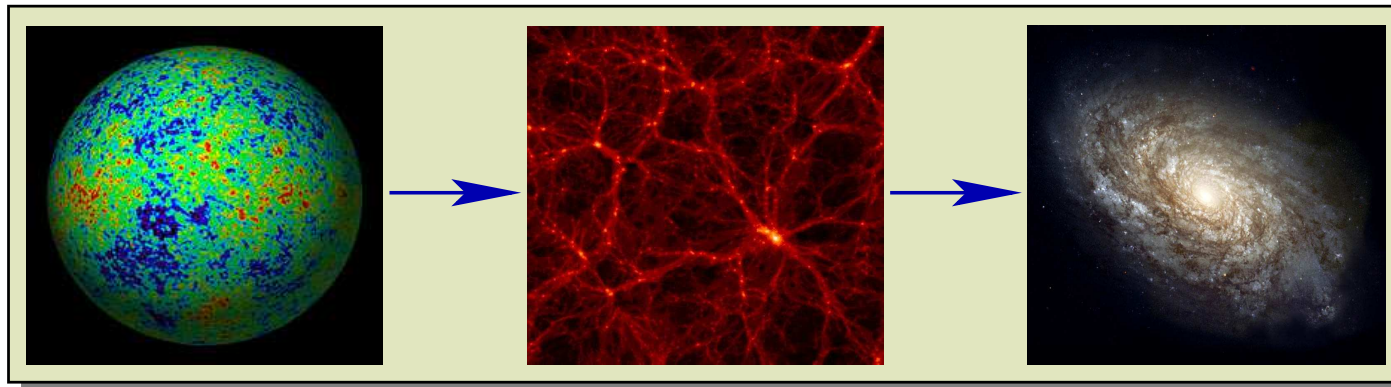
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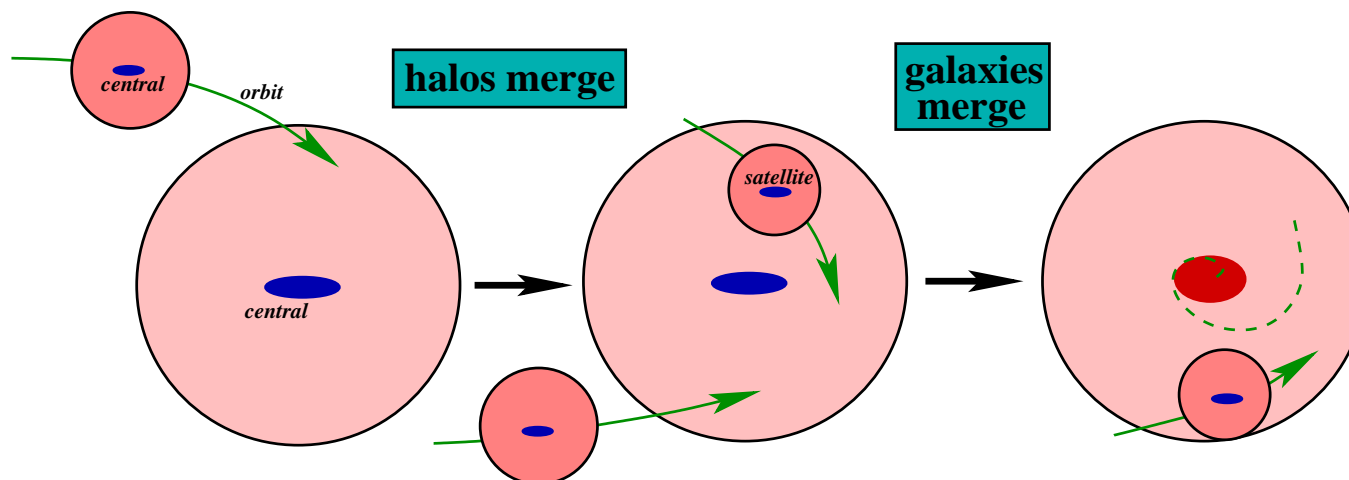
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# Galaxy Formation in a Nutshell



- Perturbations grow due to gravitational instability and collapse to produce (virialized) dark matter halos
- Baryons cool, accumulate at center, and form stars  $\Rightarrow$  galaxy
- Dark matter halos merge, causing hierarchical growth
- Halo mergers create satellite galaxies that orbit halo



# Satellite Weighting or Host Weighting?

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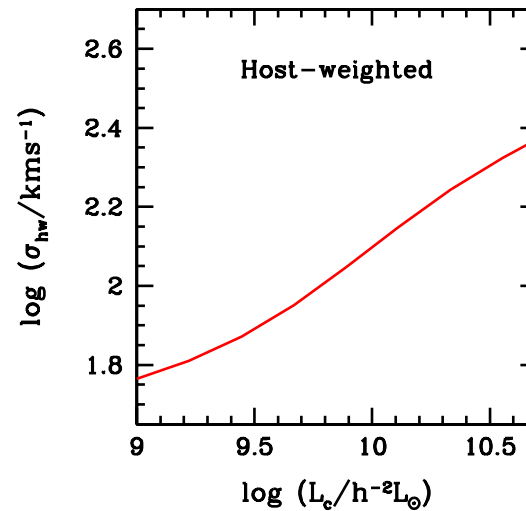
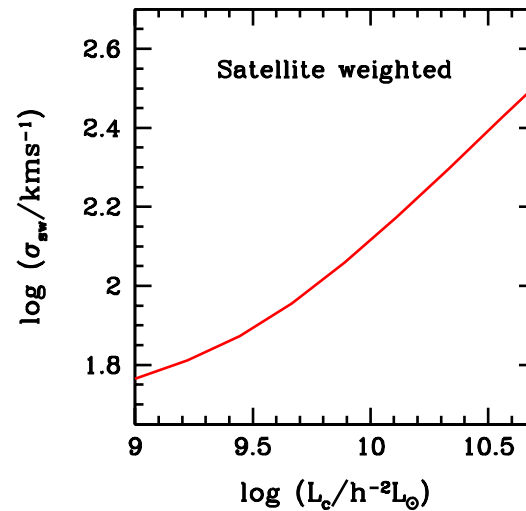
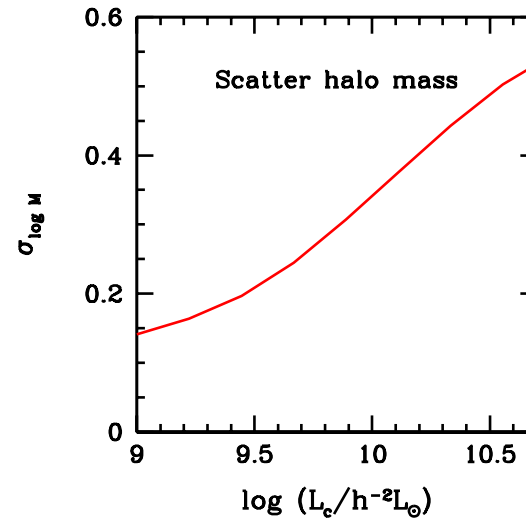
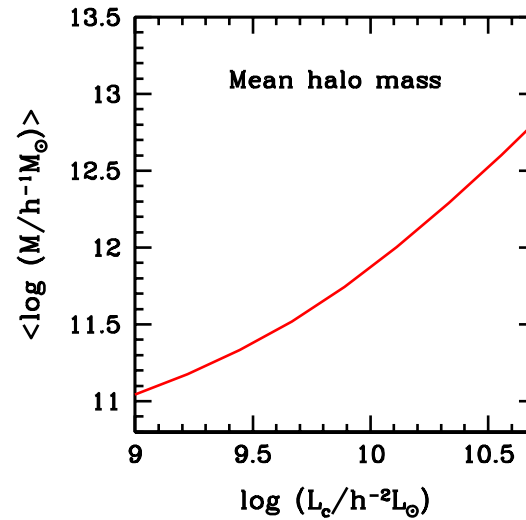
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# Satellite Weighting or Host Weighting?

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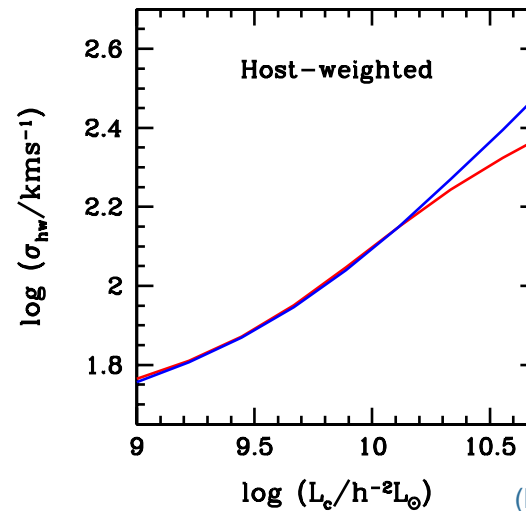
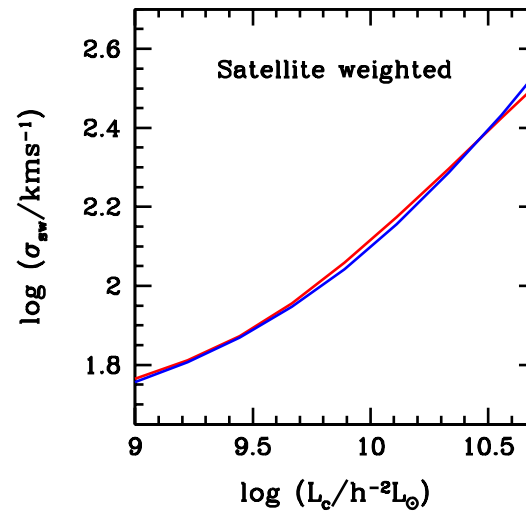
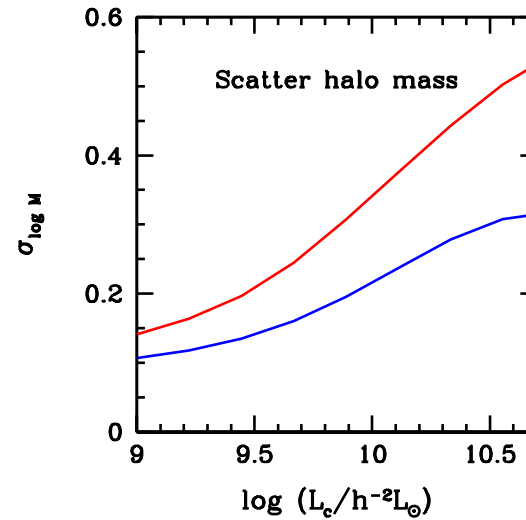
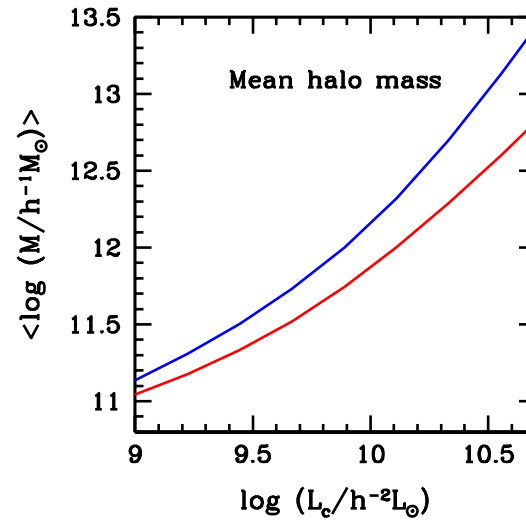
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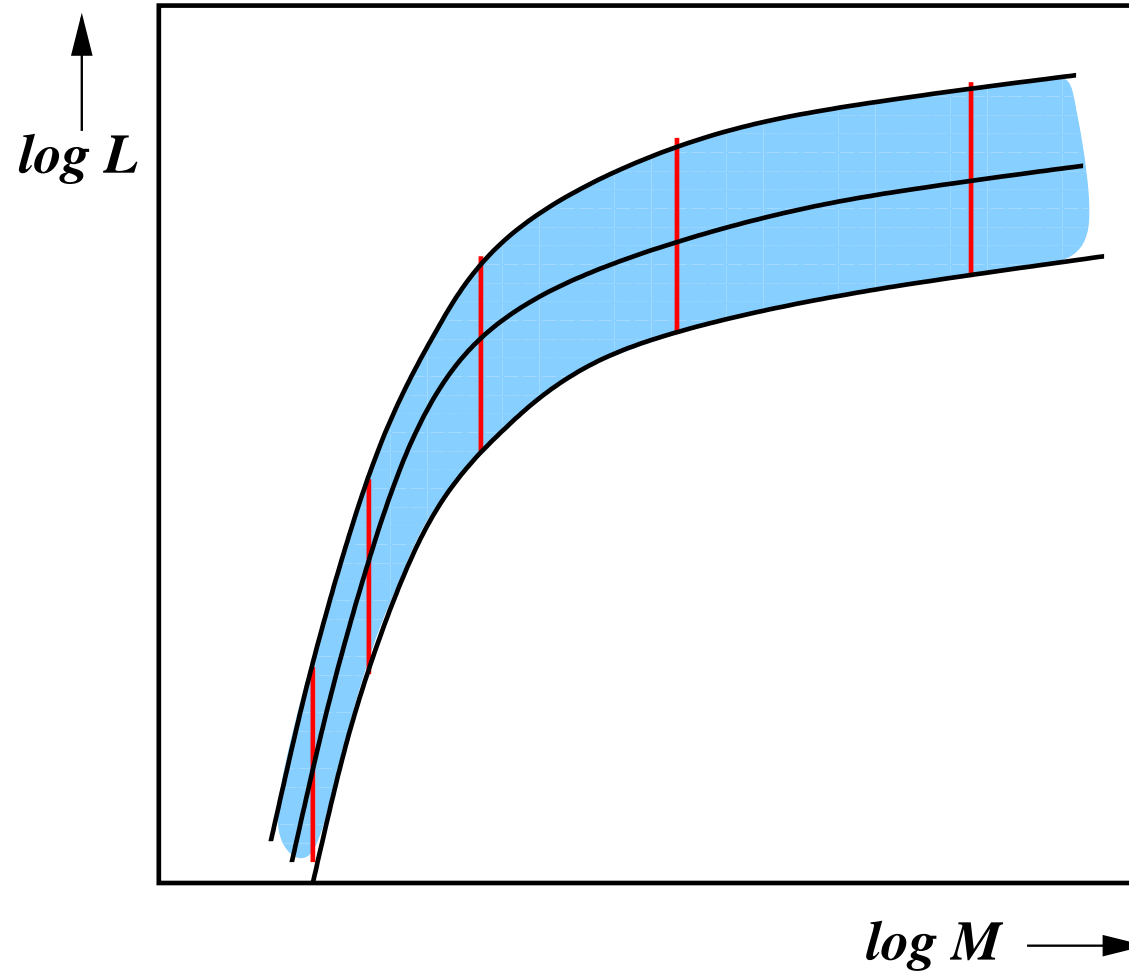
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(More, vdB et al. 2008)

The combination of  $\sigma_{sw}$  and  $\sigma_{hw}$  allows one to determine mean and scatter of  $P(M|L_c)$



- The scatter in  $P(L_{\text{cen}}|M)$  is independent of  $M$

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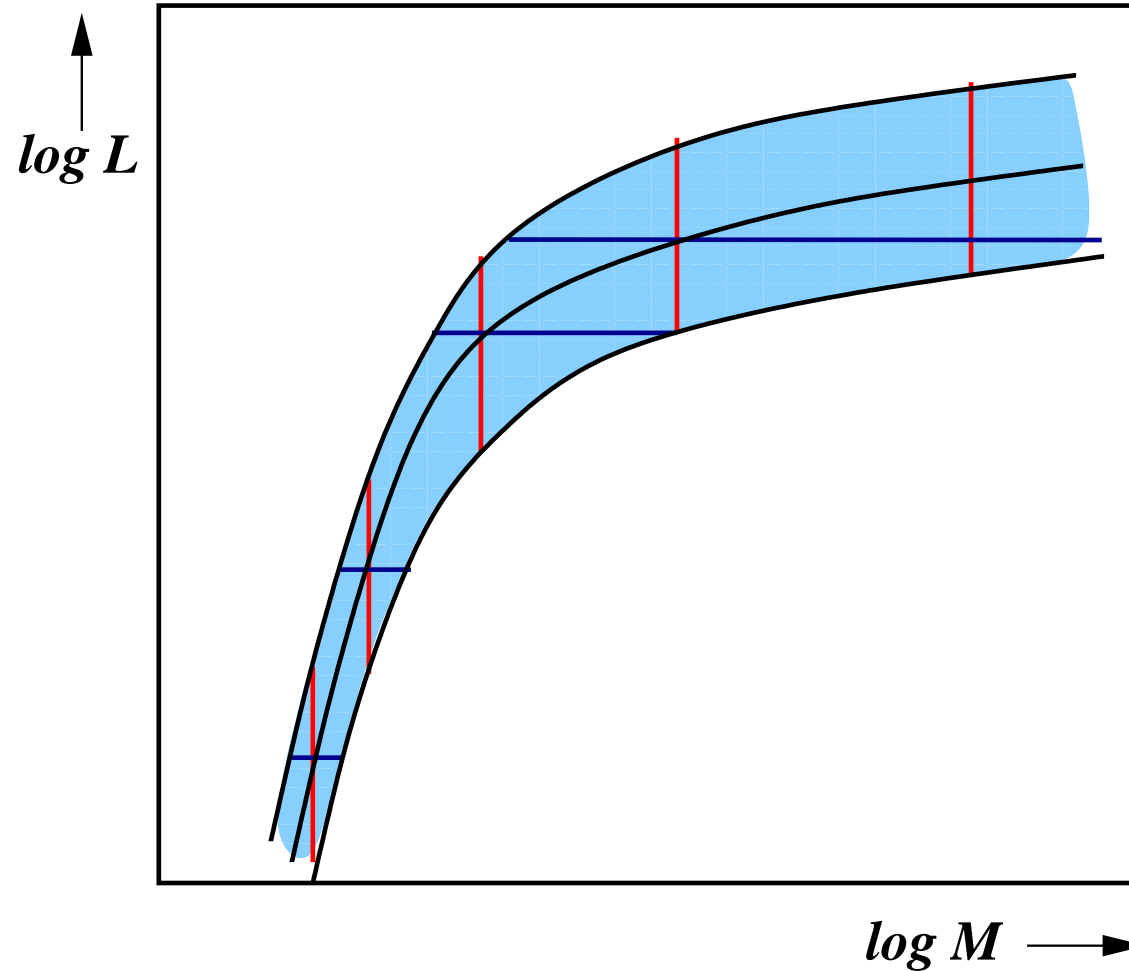
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- The scatter in  $P(L_{\text{cen}}|M)$  is independent of  $M$
- The scatter in  $P(M|L_{\text{cen}})$  increases strongly with  $L_{\text{cen}}$

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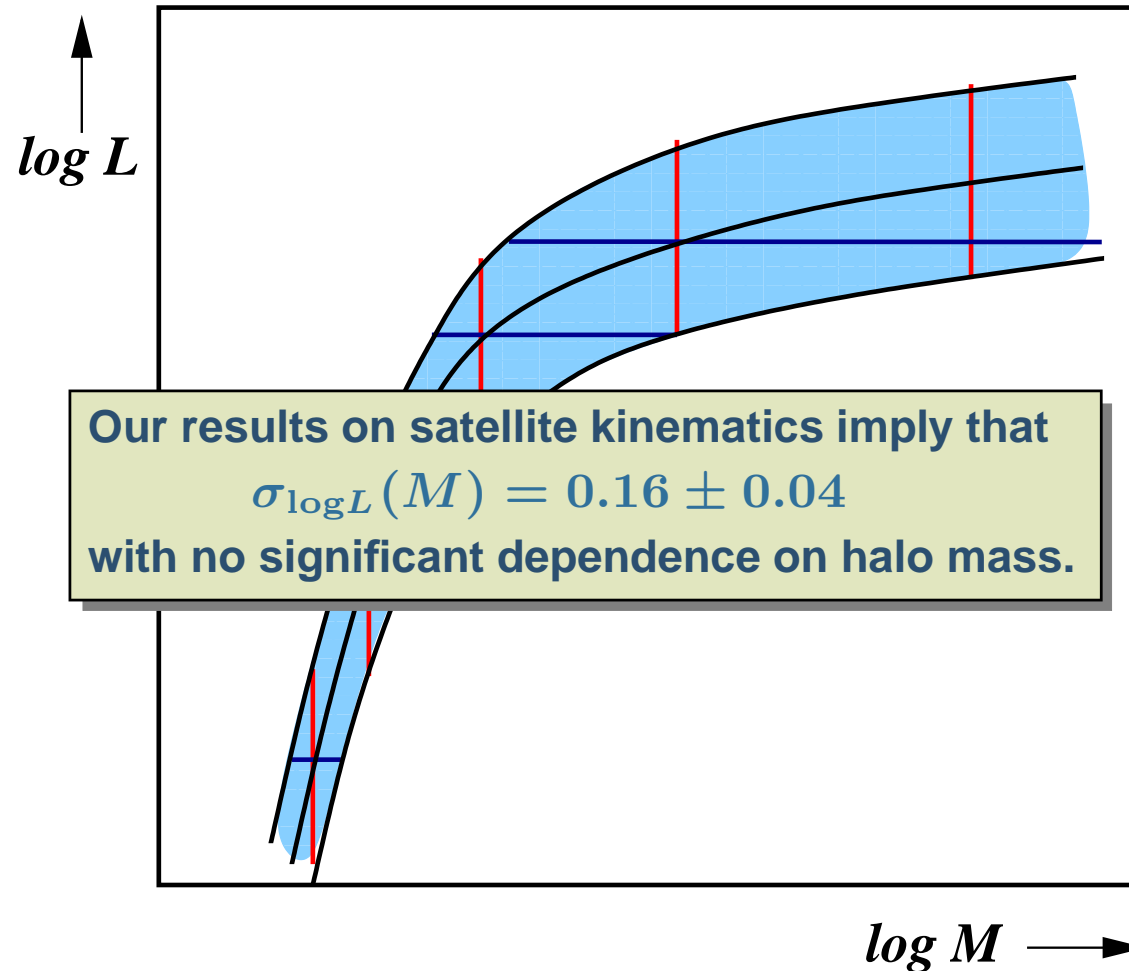
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# Implications for Galaxy Formation Stochasticity



- The scatter in  $P(L_{\text{cen}}|M)$  is independent of  $M$
- The scatter in  $P(M|L_{\text{cen}})$  increases strongly with  $L_{\text{cen}}$

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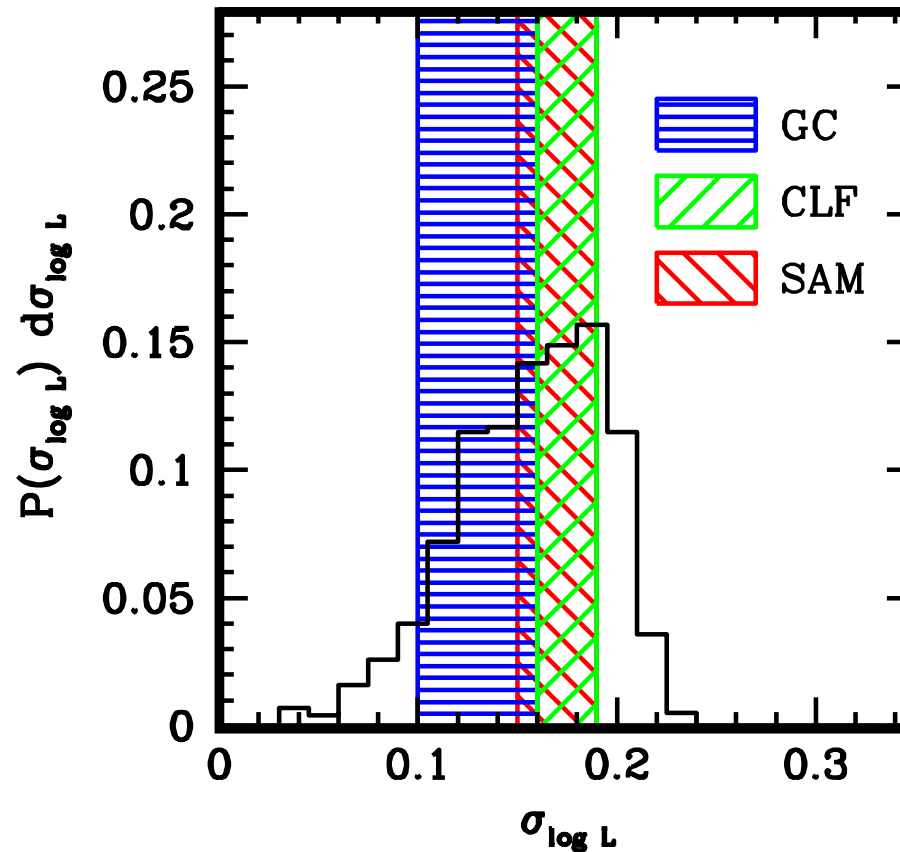
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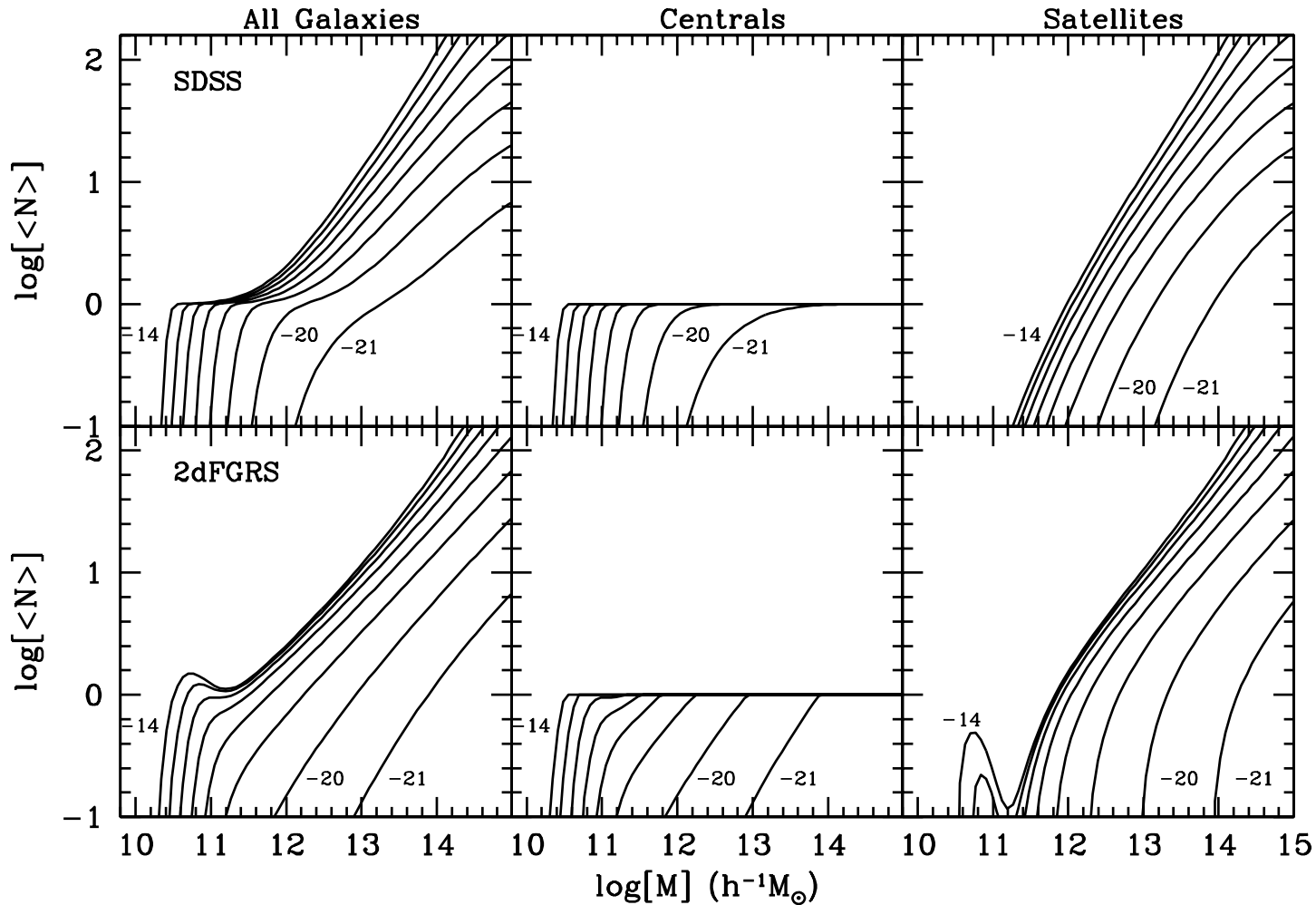
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- Probability Distribution from Satellite Kinematics
- Constraints from Galaxy Group Catalogue (Yang et al. 2008)
- Constraints from Clustering Analysis (Cooray 2006)
- Predictions from Semi Analytical Model (Croton et al. 2006)

# Halo Occupation Numbers



- Unlike **2dFGRS**, the **SDSS** reveals clear shoulders at  $\langle N \rangle_M = 1$
- Most likely this is an 'artefact' of the functional form of the **CLF**