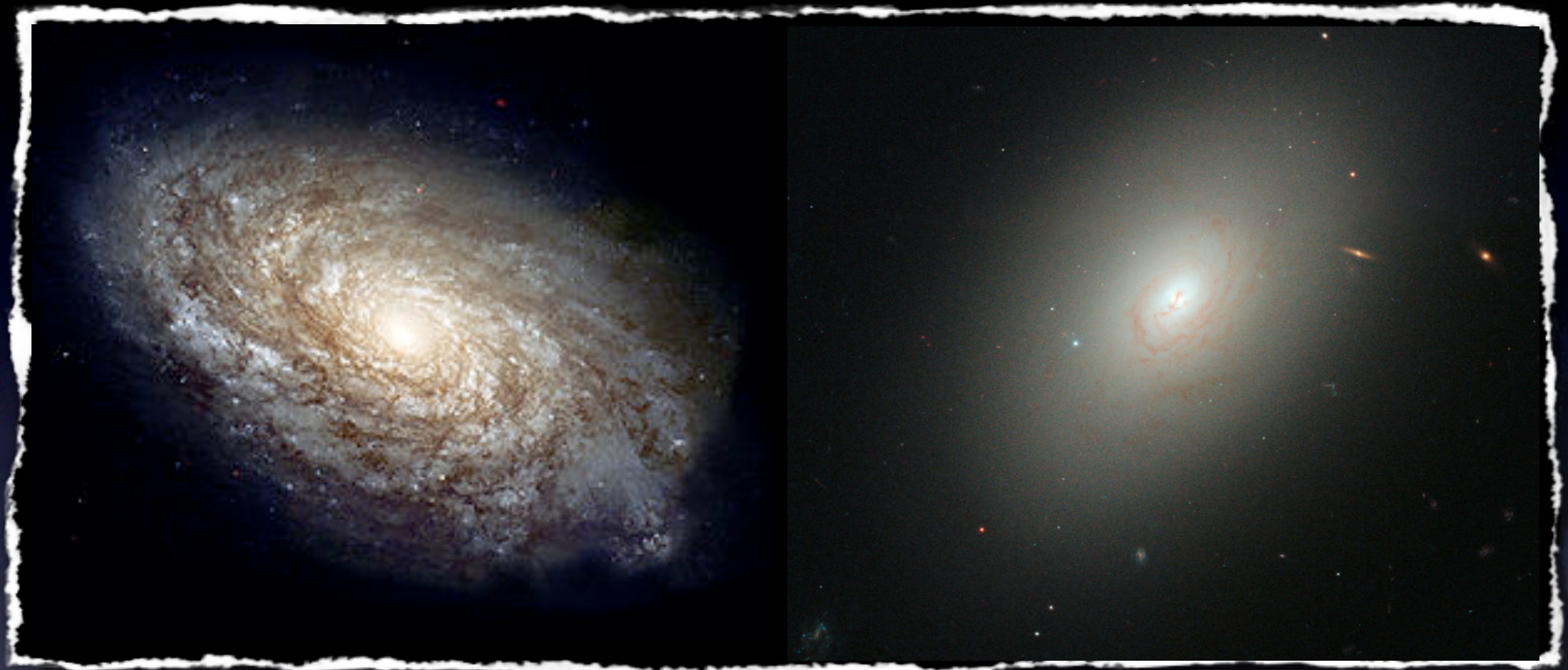


# Dark Halo Response and the Stellar IMF in Early- and Late-Type Galaxies



**FRANK VAN DEN BOSCH**  
YALE UNIVERSITY



In collaboration with:

**Aaron Dutton, Charlie Conroy,  
Surhud More, Trevor Mendel, Stephane Courteau  
Luc Simard, Avishai Dekel, Francisco Prada**

# Scaling Relations

Both **Late**- and **Early**-Type Galaxies follow tight Scaling Relations

## Tully-Fisher (TF) Relation

$$L \propto V_{\text{rot}}^{\alpha} \quad (\alpha \sim 3.5)$$

scatter NOT correlated with size

## Faber-Jackson (FJ) Relation

$$L \propto \sigma^{\beta} \quad (\beta \sim 4)$$

scatter correlated with size



## Fundamental Plane Relation

$$L \propto \sigma^{\beta} R_e^{\gamma}$$

These scaling relations can be used as distance indicators, but are also interesting for understanding galaxy formation

# The Origin of Galaxy Scaling Relations

The origin of the TF and FJ relations is believed to be that all DM halos have same density, which implies that

$$V_{\text{vir}} \propto R_{\text{vir}} \propto M_{\text{vir}}^{1/3}$$

Using that less massive halos are more concentrated, this becomes

$$V_{\text{max,h}} \propto M_{\text{vir}}^{0.29}$$

This scaling is similar to observed stellar mass TF & FJ relations

$$V_{2.2} \propto M_*^{0.28}$$

[Dutton et al. 2010]

$V_{2.2}$  is disk rotation velocity  
at 2.2 disk scale lengths

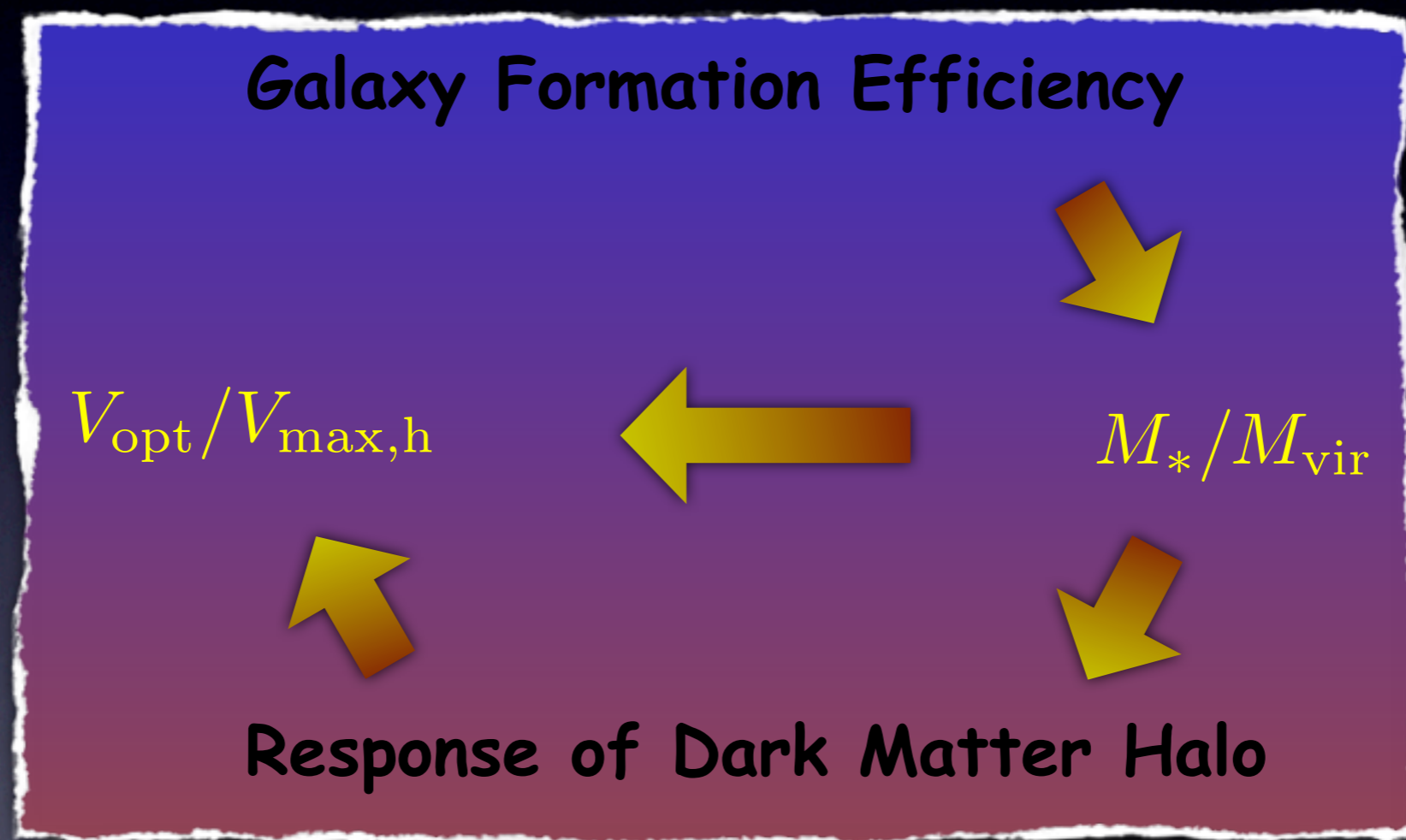
$$\sigma_e \propto M_*^{0.29}$$

[Gallazzi et al. 2006]

$\sigma_e$  is velocity dispersion  
inside effective radius

# The Origin of Galaxy Scaling Relations

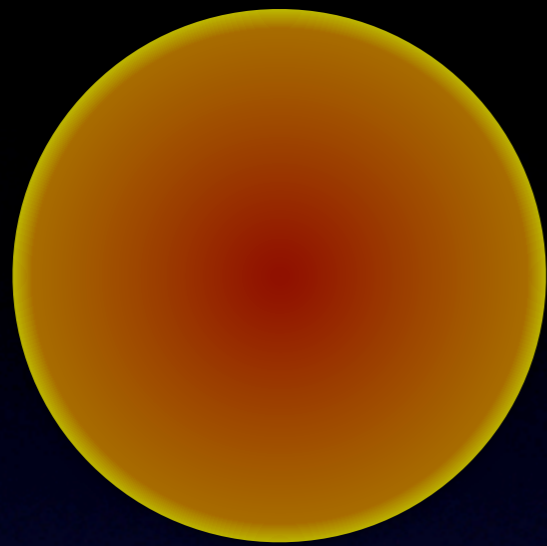
For the  $V_{\max,h} - M_{\text{vir}}$  relation to be the direct origin of the TF & FJ relations requires that  $V_{\text{opt}}/V_{\max,h}$  and  $M_*/M_{\text{vir}}$  are both constants! ✦



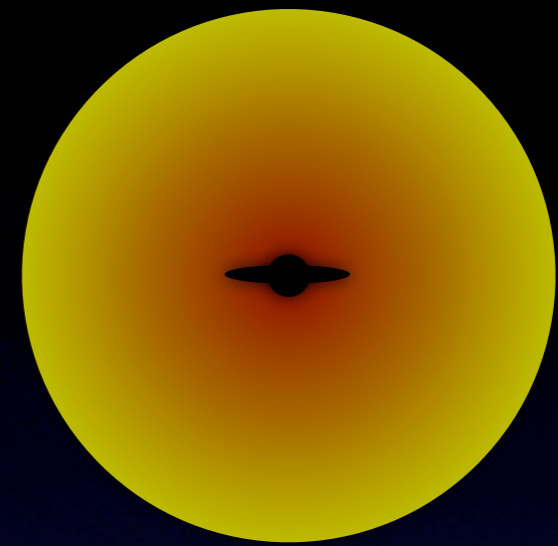
Hence, there is hope that the observed TF & FJ relations can shed light on Galaxy Formation and Halo Response.

✦ Here  $V_{\text{opt}} = V_{2.2}$  for late-types, and  $V_{\text{opt}} = \sigma_e$  for early-types

# Dark Halo Response



When baryons collect at center,  
the dark matter halo contracts...



In the limit where the process is slow, the response is adiabatic

spherical symmetry:  $r_i M_i(r_i) = r_f M_f(r_f)$

no shell crossing:  $M_{h,i}(r_i) = M_{h,f}(r_f)$

initially well mixed:  $M_{b,i}(r_i) = f_b M_{h,i}(r_i)$



$$\frac{r_f}{r_i} = \Gamma_{AC} = \frac{M_{h,i}(r_i)}{M_{b,f}(r_f) + (1 - f_b)M_{h,i}(r_i)}$$

Blumenthal et al. (1986)

In general, system is not spherically symmetric and the process of galaxy formation may not be adiabatic. We therefore adopt the more general form:

$$\frac{r_f}{r_i} = \Gamma_{AC}^\nu$$

Here  $\nu$  is a free parameter, to be constrained by the data:  $\begin{cases} \nu = 1 & \text{standard AC} \\ \nu = 0 & \text{no contraction} \\ \nu < 0 & \text{expansion} \end{cases}$

[Based on cosmological, hydrodynamical simulations, Gnedin et al. (2004) suggest  $\nu \simeq 0.8$ ]

# Structural Models

Galaxies consist of three components:

## Dark Matter Halo

Modelled as spherical NFW halo.  
Concentration mass relation of Maccio et al. (2007)  
Completely specified by its mass,  $M_h$

## Stellar Component

Modelled as sum of two Sersic profiles:  $n=1$  plus  $n=4$ .  
In case of late-type,  $n=1$  component is thin disk.  
In case of early-type,  $n=1$  component is spherical.  
Specified by four free parameters:  $M_d, M_b, R_d, R_b$

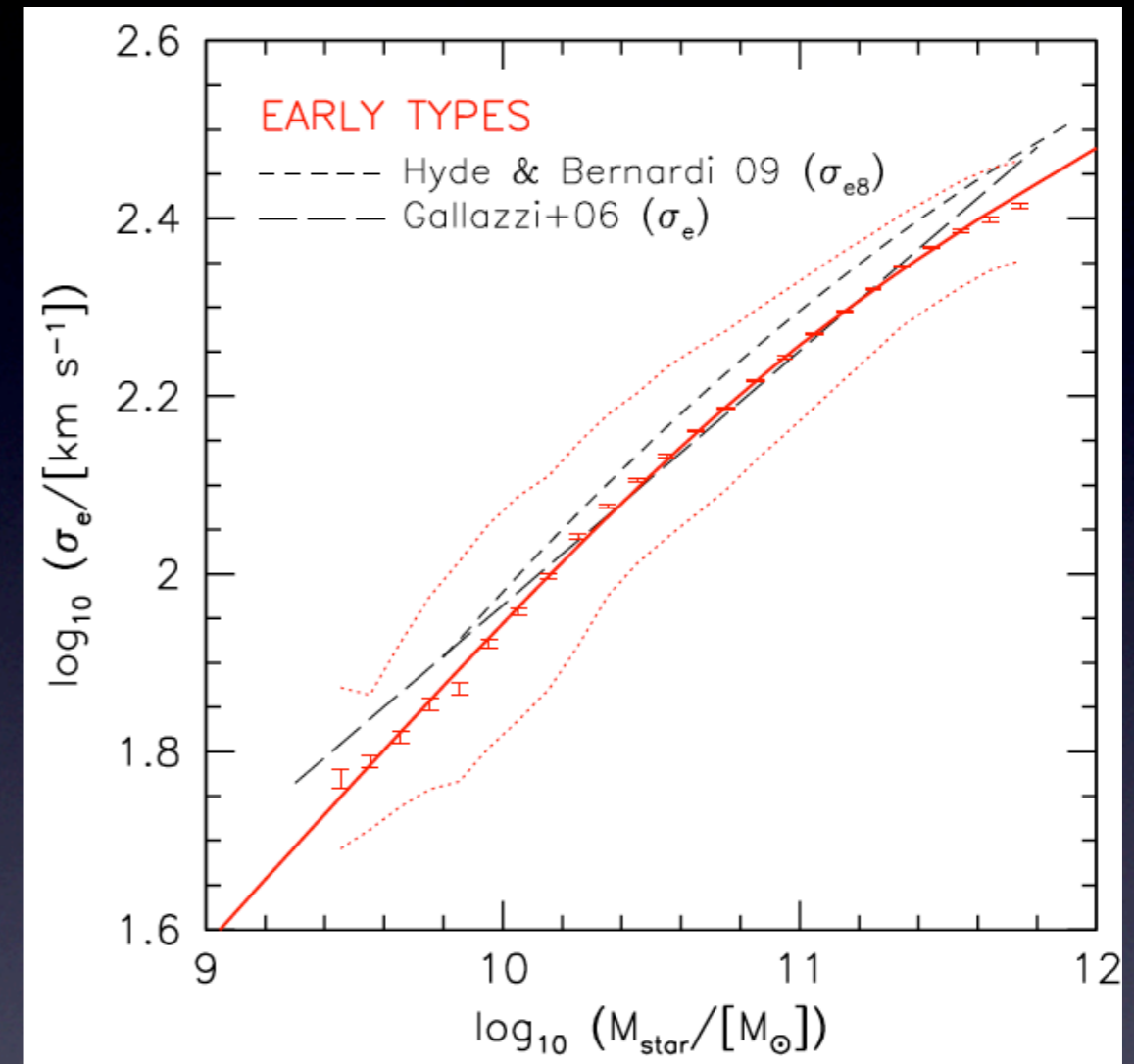
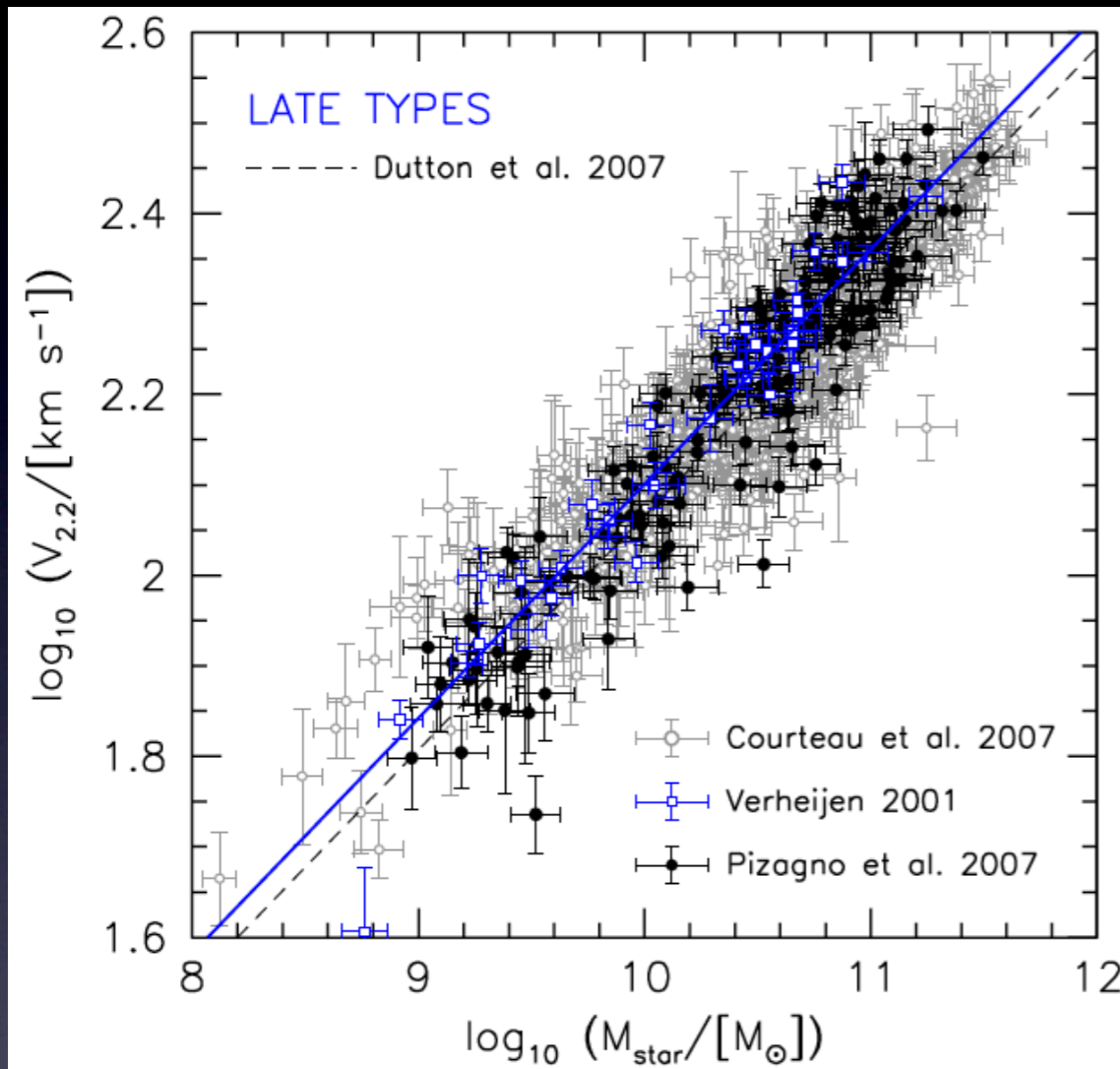
$$M_* \equiv M_d + M_b$$

## Cold Gas Disk

Modelled as thin exponential disk.  
Specified by two free parameters:  $M_g, R_g$



# Tully-Fisher and Faber-Jackson Relations

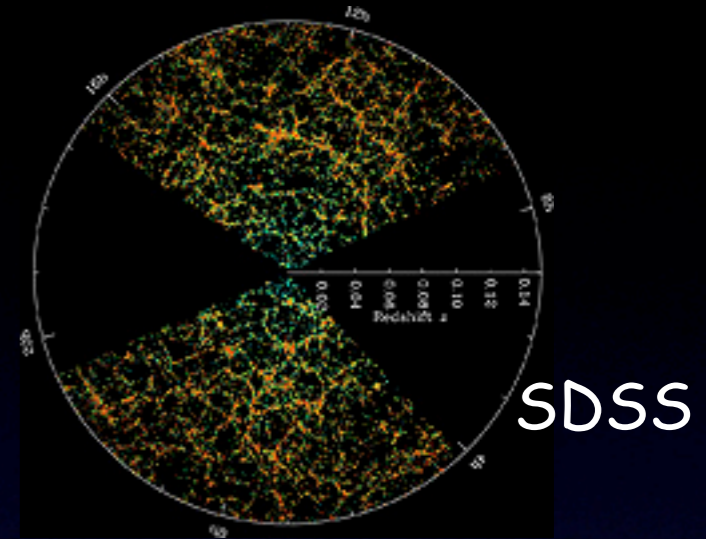


We use these relations as constraints for the models

# Methodology

## Observed Scaling Relations

$M_h$  vs.  $M_*$        $R_d$  vs.  $M_*$        $B/D$  vs.  $M_*$   
 $M_g$  vs.  $M_*$        $R_b$  vs.  $M_*$        $R_g$  vs.  $R_d$



## Model Parameters

$M_h, M_d, M_b, M_g$   
 $R_d, R_b, R_g$   
 $\Delta_{IMF}$     $\nu$

## Rotation Curve

$$V_c(r) = \sqrt{V_h^2 + V_d^2 + V_b^2 + V_g^2}$$

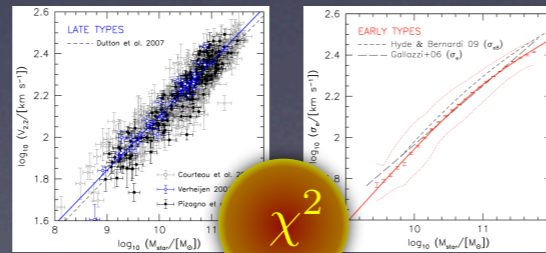
$$V_c(r_e)/\sigma_e$$

$V_{2.2}$  or  $\sigma_e$

Sampling of  $M_h$

Constrain

$\Delta_{IMF}$  &  $\nu$



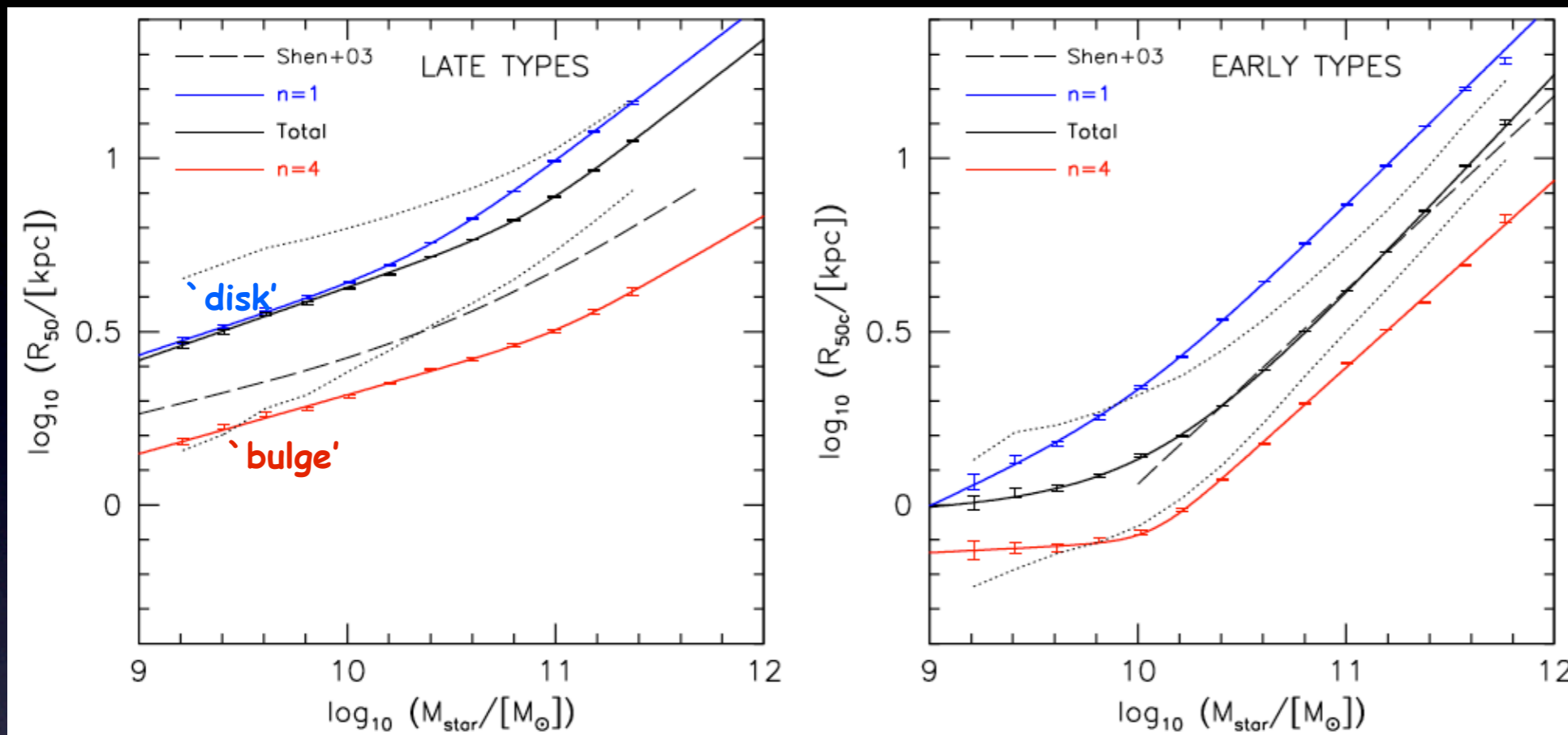
compare to data

TF & FJ relations

$\chi^2$



# Galaxy Sizes and B/D Ratios



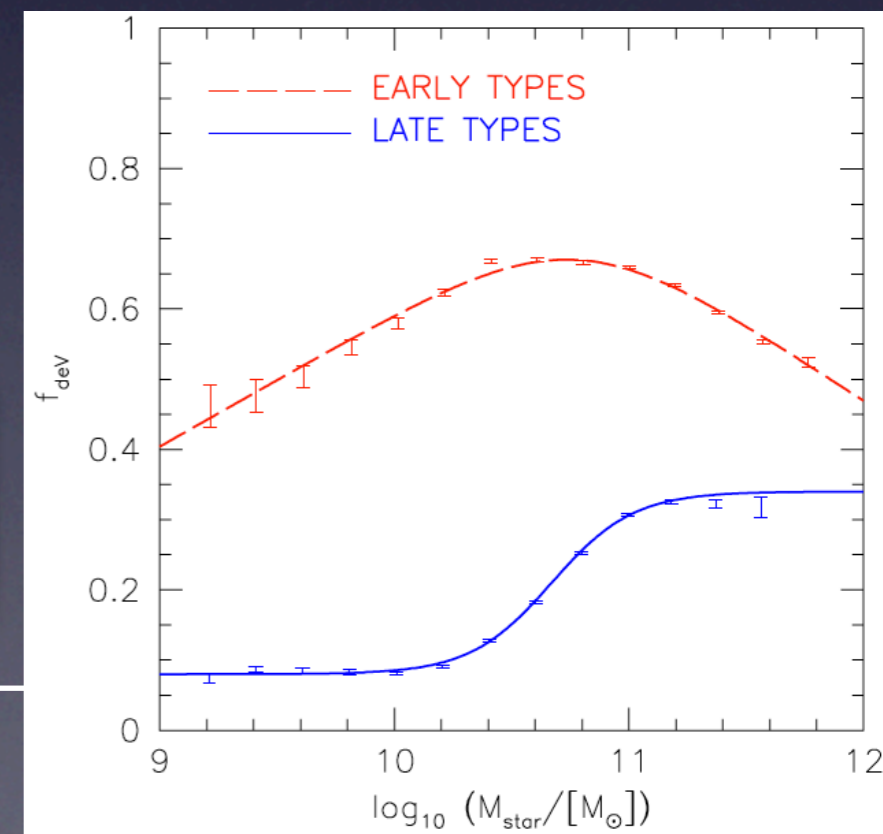
Sizes and B/D ratios obtained from GIM2D photometric analysis of  $\sim 270,000$  SDSS galaxies.

Stellar masses obtained from SDSS  $ugriz$ -SED by MPA/JHU group, assuming a Chabrier IMF.

We can rescale these stellar masses to another IMF by adding  $\Delta_{\text{IMF}}$  to  $\log(M_*)$

Chabrier:  $\Delta_{\text{IMF}} = 0.0$

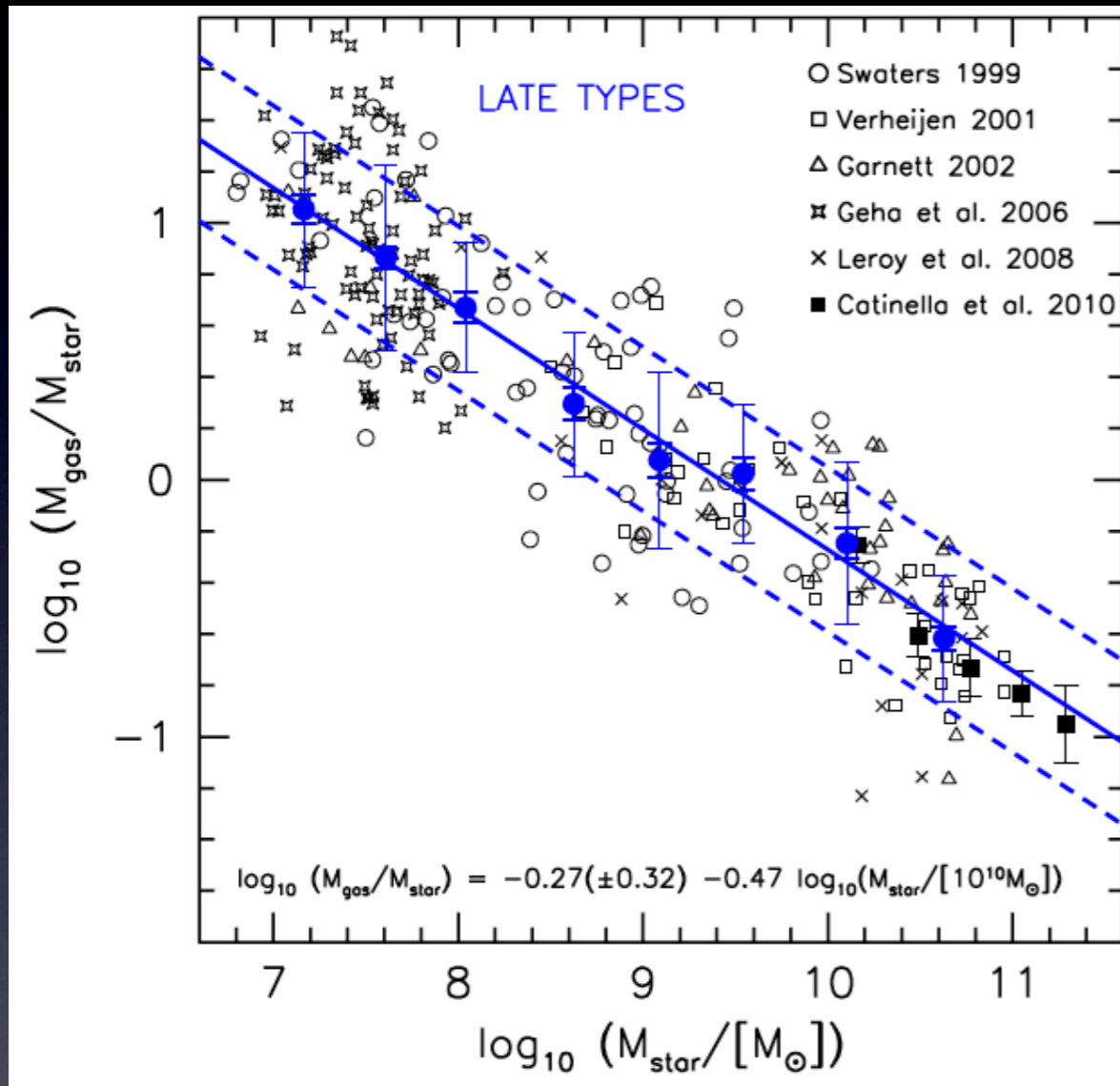
Salpeter:  $\Delta_{\text{IMF}} = +0.24$



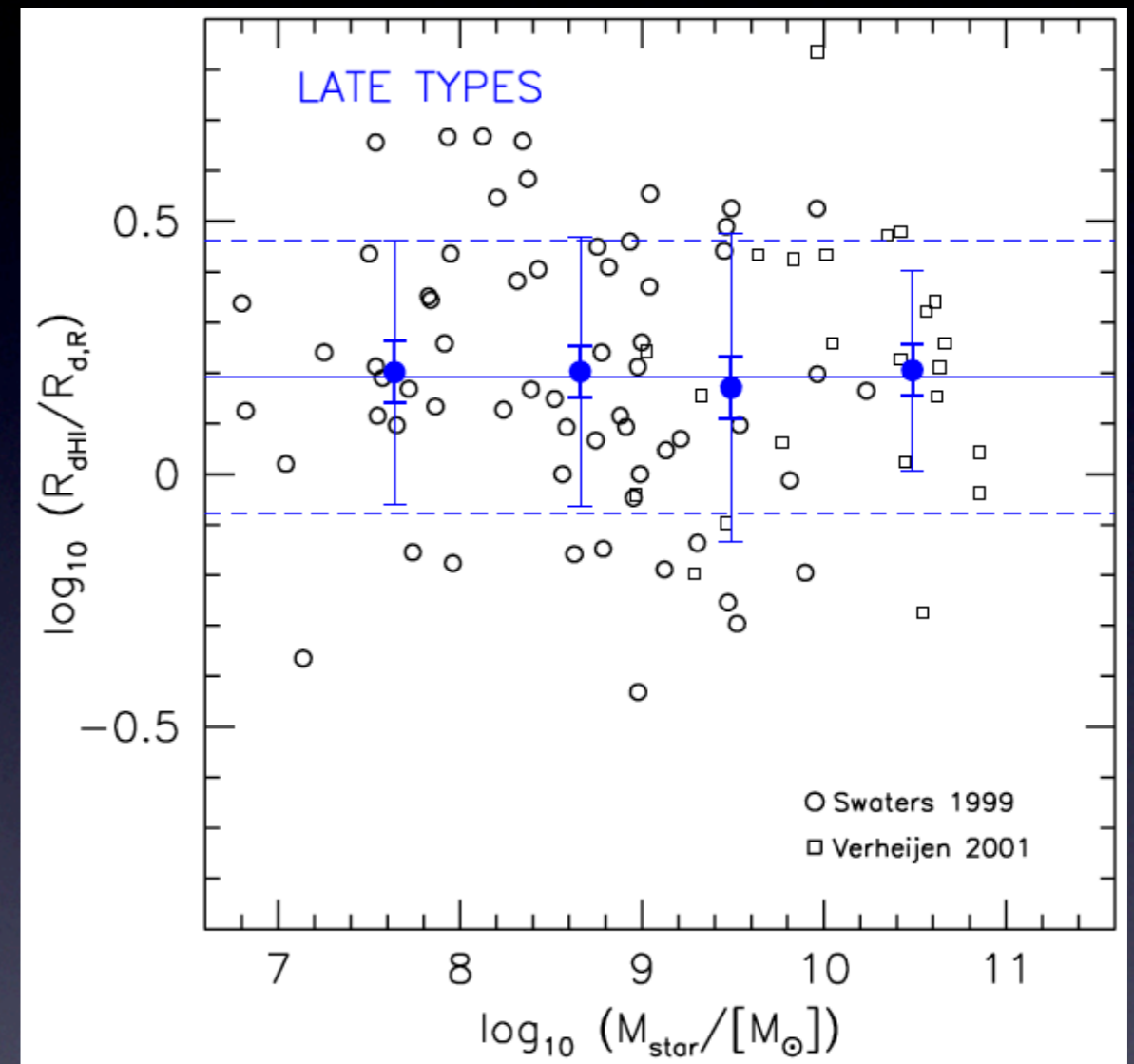
Note: Our sizes for late-types are larger than those of Shen et al. (2003); This is due to fact that Shen et al used circular aperture photometry.

# Properties of Cold Gas in Late-Type Galaxies

## Gas Mass Fractions



## Gas Scale Lengths

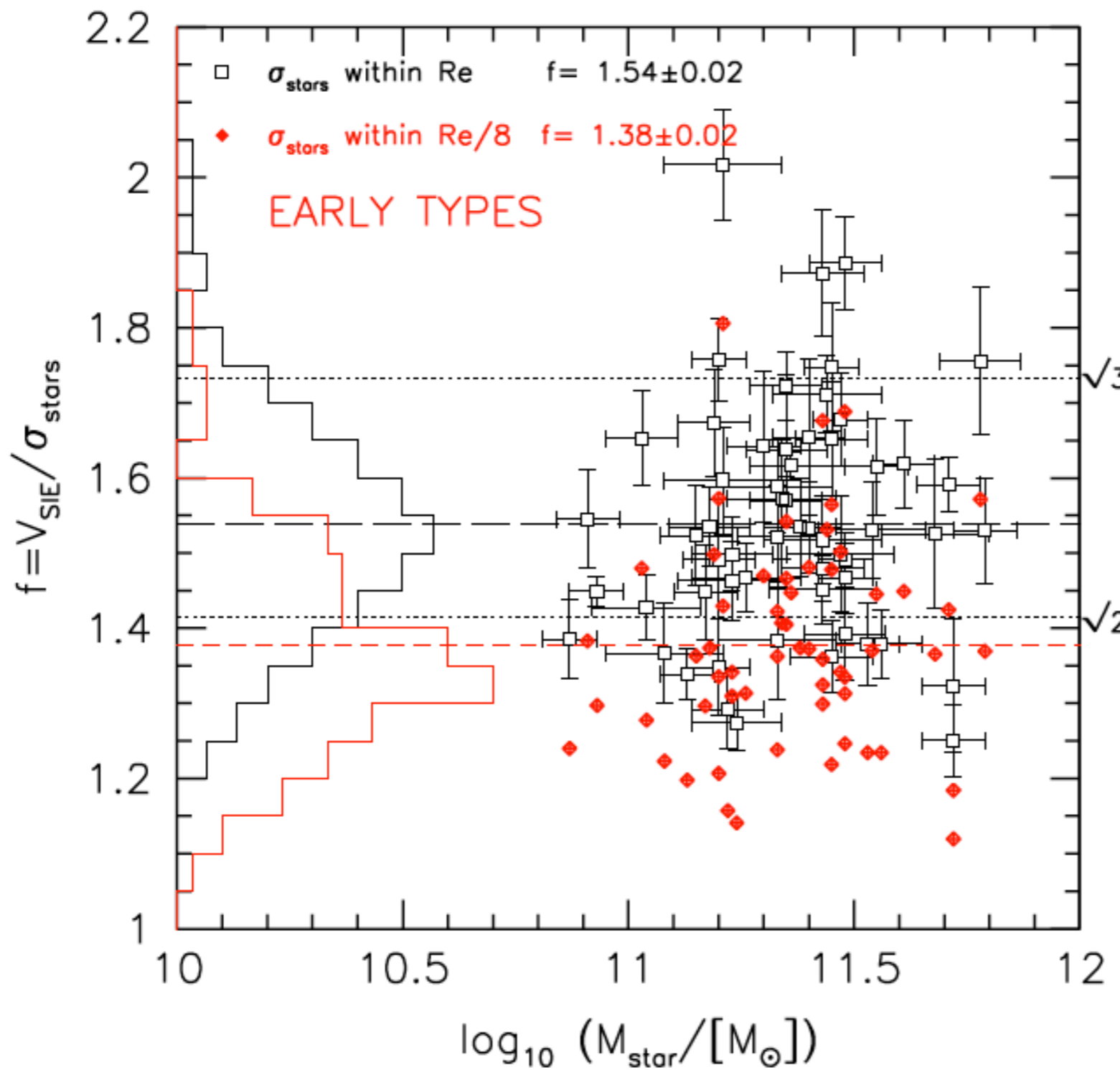


$$\log \left( \frac{M_g}{M_*} \right) = -0.27 - 0.47 \log \left( \frac{M_*}{10^{10} M_{\odot}} \right)$$

$$\log \left( \frac{R_d}{R_g} \right) = 0.19$$

These two relations define the gas properties of late-types.

# How to convert from $V(r)$ to $\sigma_e$ ?



Data from SLACS survey (strong gravitational lensing sample). Taken from Auger et al. (2009)

Based on strong lensing data we infer that

$$\frac{V_c(R_e)}{\sigma_e} = 1.54$$

which is the value we adopt throughout.

Previous studies:

Padmanabhan et al. (2004)

$$\frac{V_c(R_e)}{\sigma_e} = 1.65$$

Cappellari et al. (2006)

$$\frac{V_c(R_e)}{\sigma_e} = 1.44$$

We adopt uncertainty of 0.03 dex

# Satellite Kinematics

We use satellite kinematics in the SDSS to probe the relation between stellar mass and halo mass. Using virial equilibrium and spherical collapse:

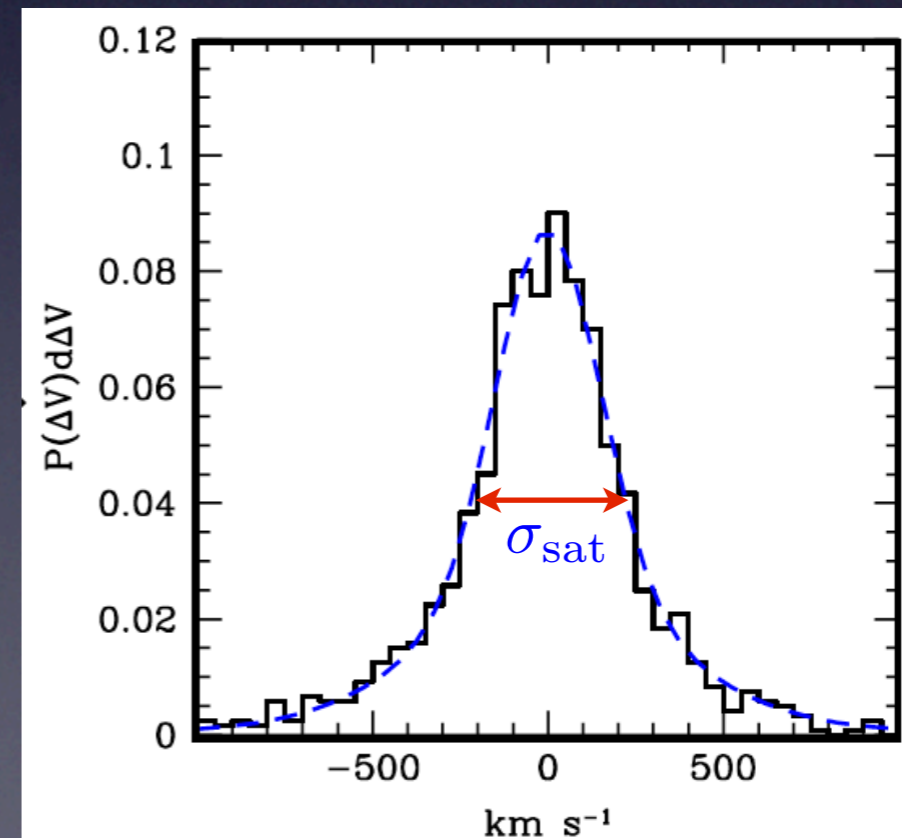
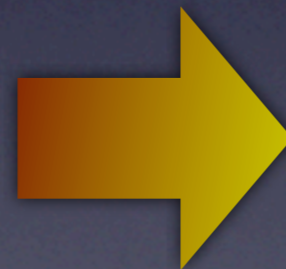
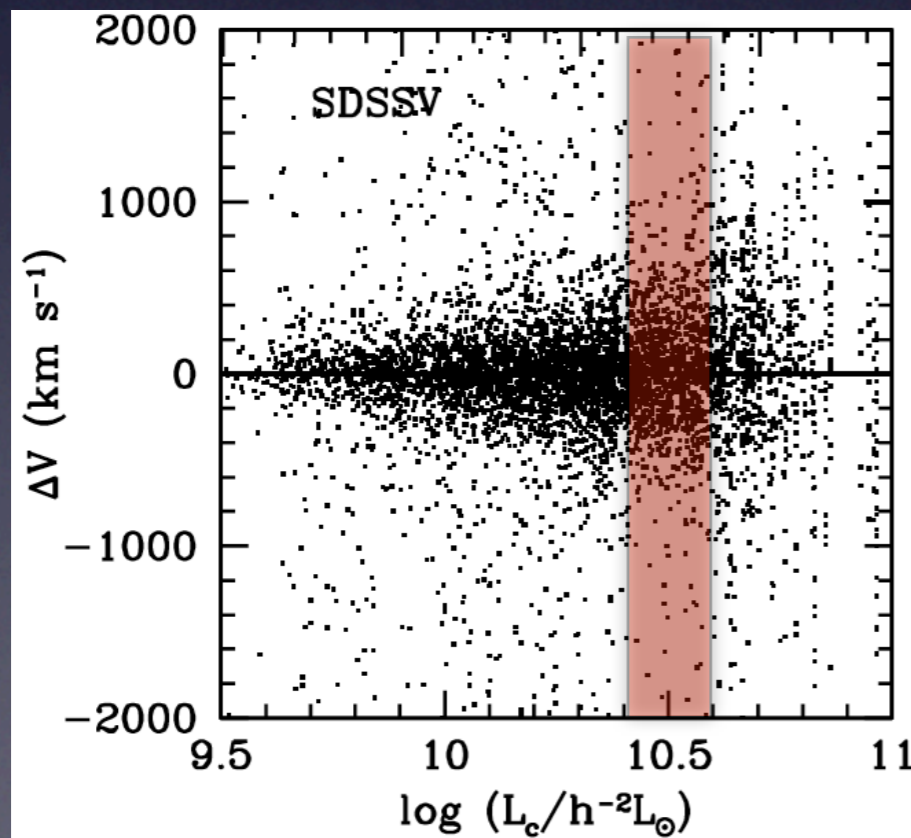
$$\sigma^2 \propto \frac{GM_h}{r_h}$$

$$M_h \propto r_h^3$$

$$\sigma \propto M_h^{1/3}$$

On average, only  $\sim 2$  satellites per central:  $\longrightarrow$  **stacking**

- select centrals and satellites from SDSS
- using redshifts, measure  $\Delta V = V_{\text{sat}} - V_{\text{cen}}$  as function of  $M_*$



# Satellite Kinematics

Unless  $P(M_h|M_*)$  is a Dirac Delta function, stacking implies combining haloes of different masses. Consequently, distinguish two schemes:

**satellite weighting:**

$$\sigma_{\text{sw}}^2(M_*) = \frac{\int P(M_h|M_*) \langle N_s|M_h \rangle \sigma_{\text{sat}}^2(M_h) dM_h}{\int P(M_h|M_*) \langle N_s|M_h \rangle dM_h}$$

**host weighting:**

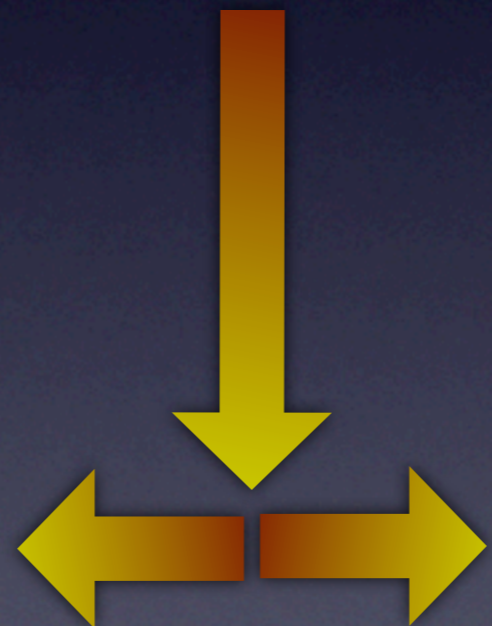
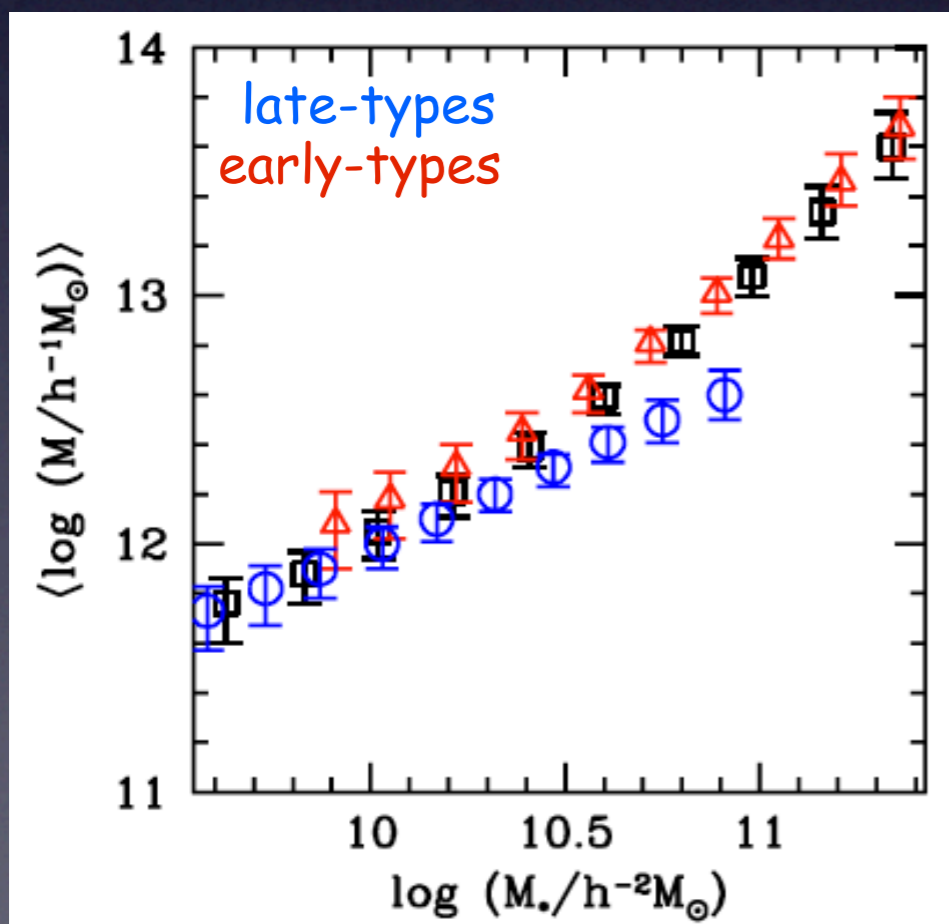
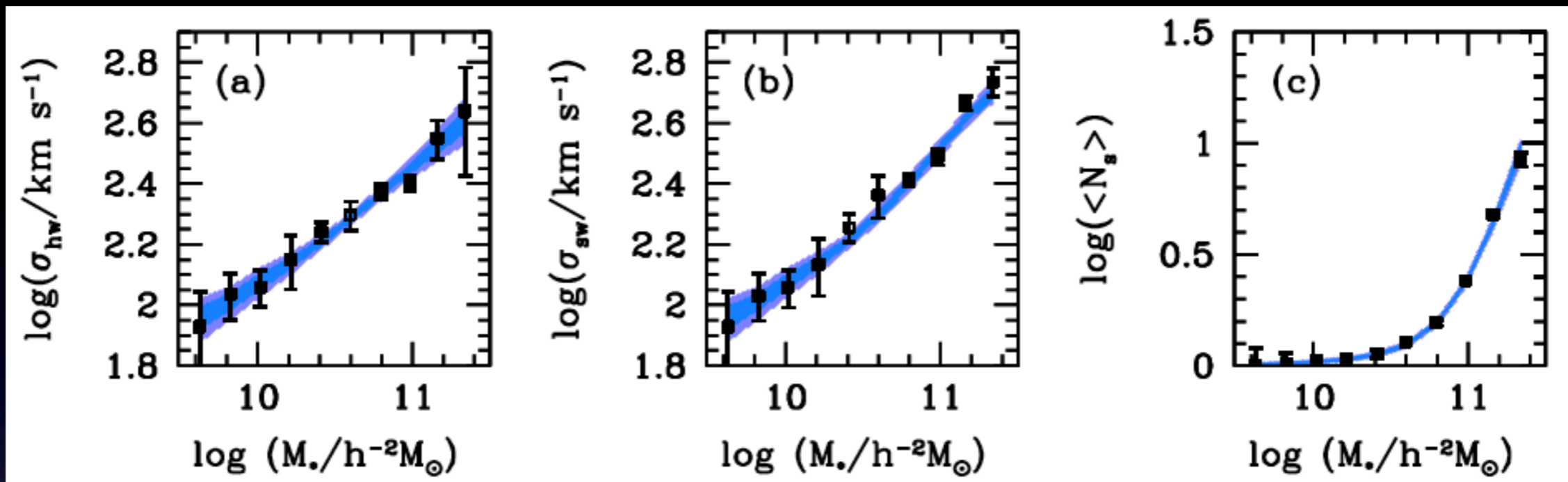
$$\sigma_{\text{hw}}^2(M_*) = \frac{\int P(M_h|M_*) \sigma_{\text{sat}}^2(M_h) dM_h}{\int P(M_h|M_*) dM_h}$$

**satellites per host:**

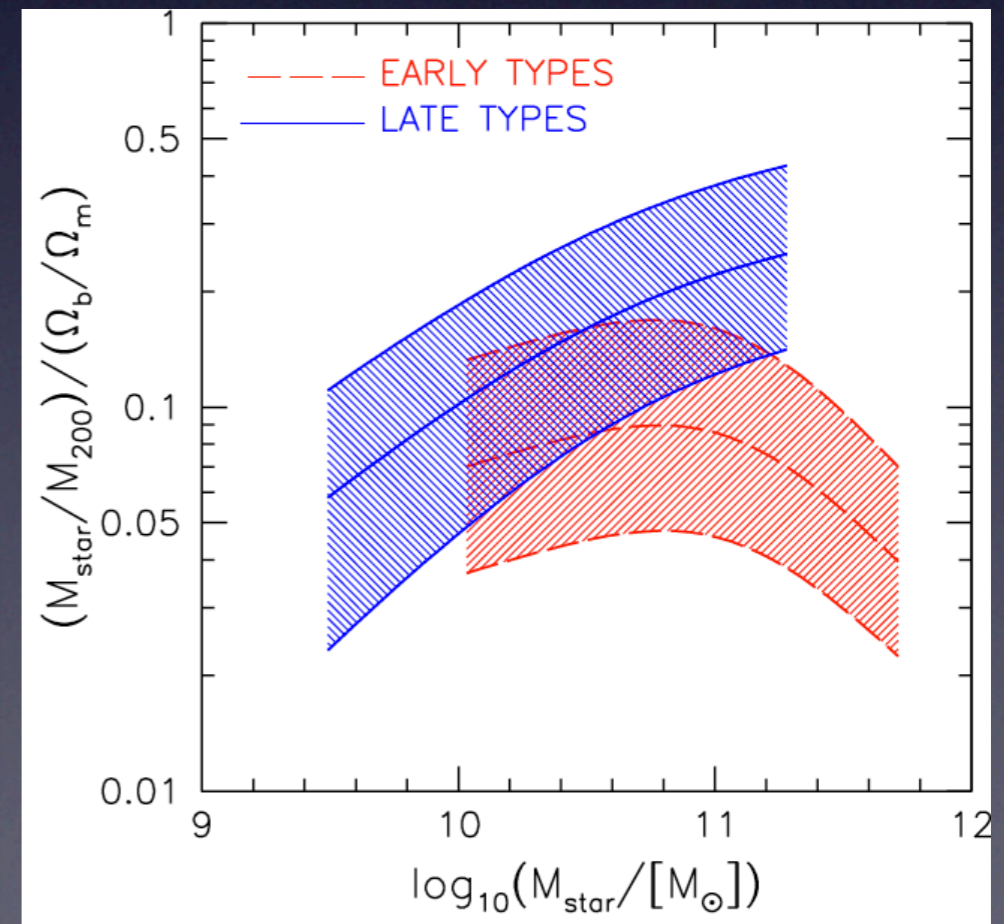
$$\langle N_{\text{sat}} \rangle(M_*) = \frac{\int P(M_h|M_*) \langle N_s|M_h \rangle dM_h}{\int P(M_h|M_*) dM_h}$$

From the measurements of  $\sigma_{\text{sw}}^2(M_*)$ ,  $\sigma_{\text{hw}}^2(M_*)$ , and  $\langle N_{\text{sat}} \rangle(M_*)$  one can determine  $P(M_h|M_*)$ .

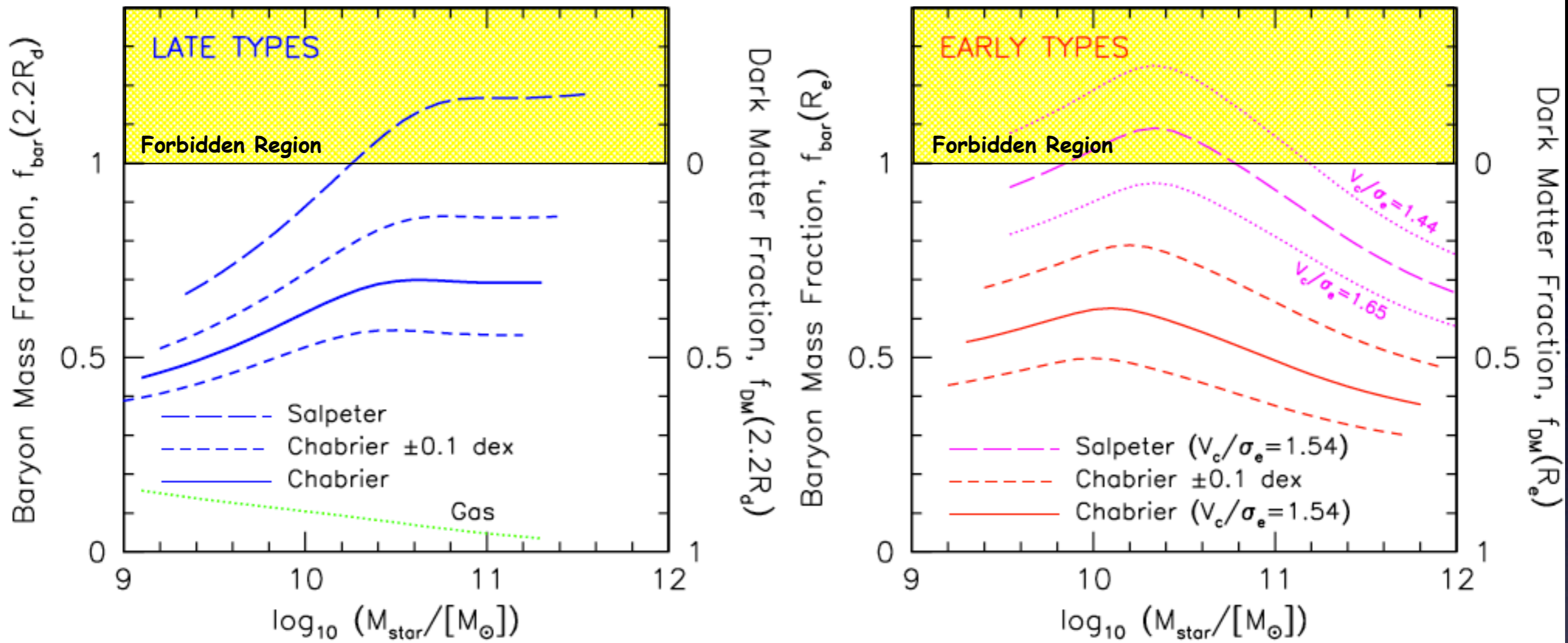
# Satellite Kinematics: results



based on ~6300 satellites around ~3800 centrals  
 [More et al. 2011]

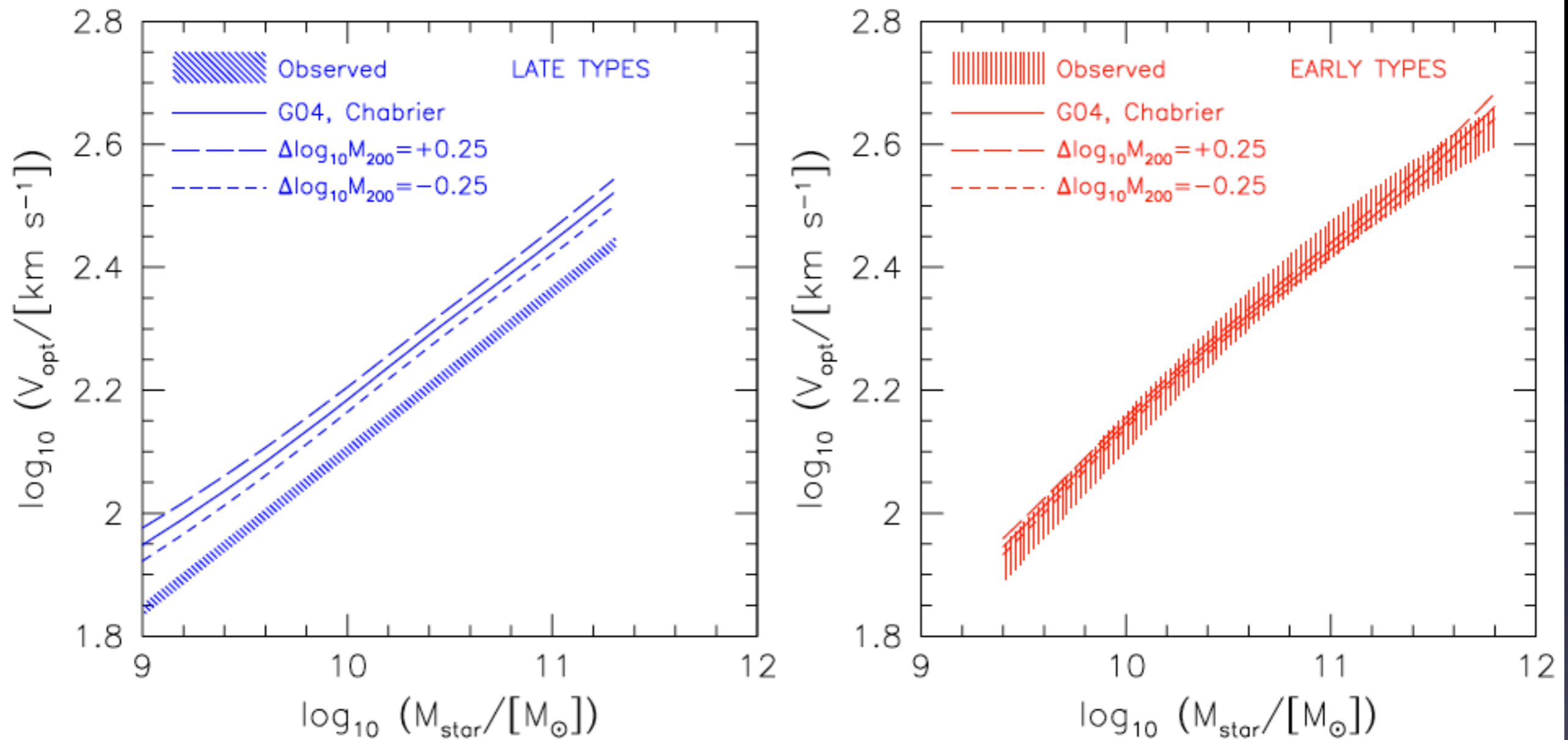


# Baryonic Mass Fractions



Chabrier IMF consistent with all galaxies....  
Salpeter IMF ruled out for massive late-types  
and for low mass early-types

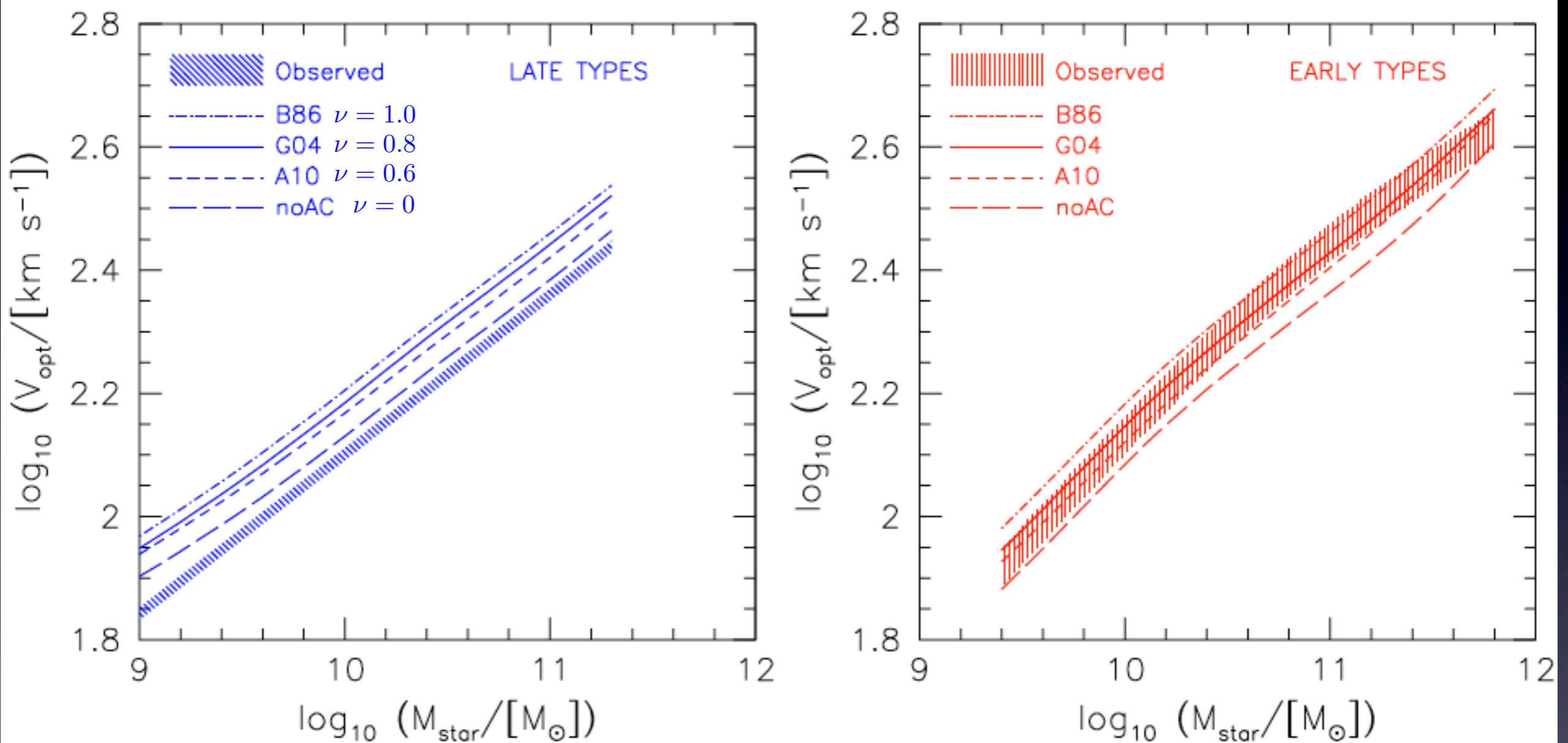
# Results



A model with Chabrier IMF ( $\Delta_{\text{IMF}} = 0.0$ ) and Gnedin contraction ( $\nu = 0.8$ ) is in agreement with the FJ relation, but yields a TF zeropoint that is too high (too much rotation for given stellar mass).

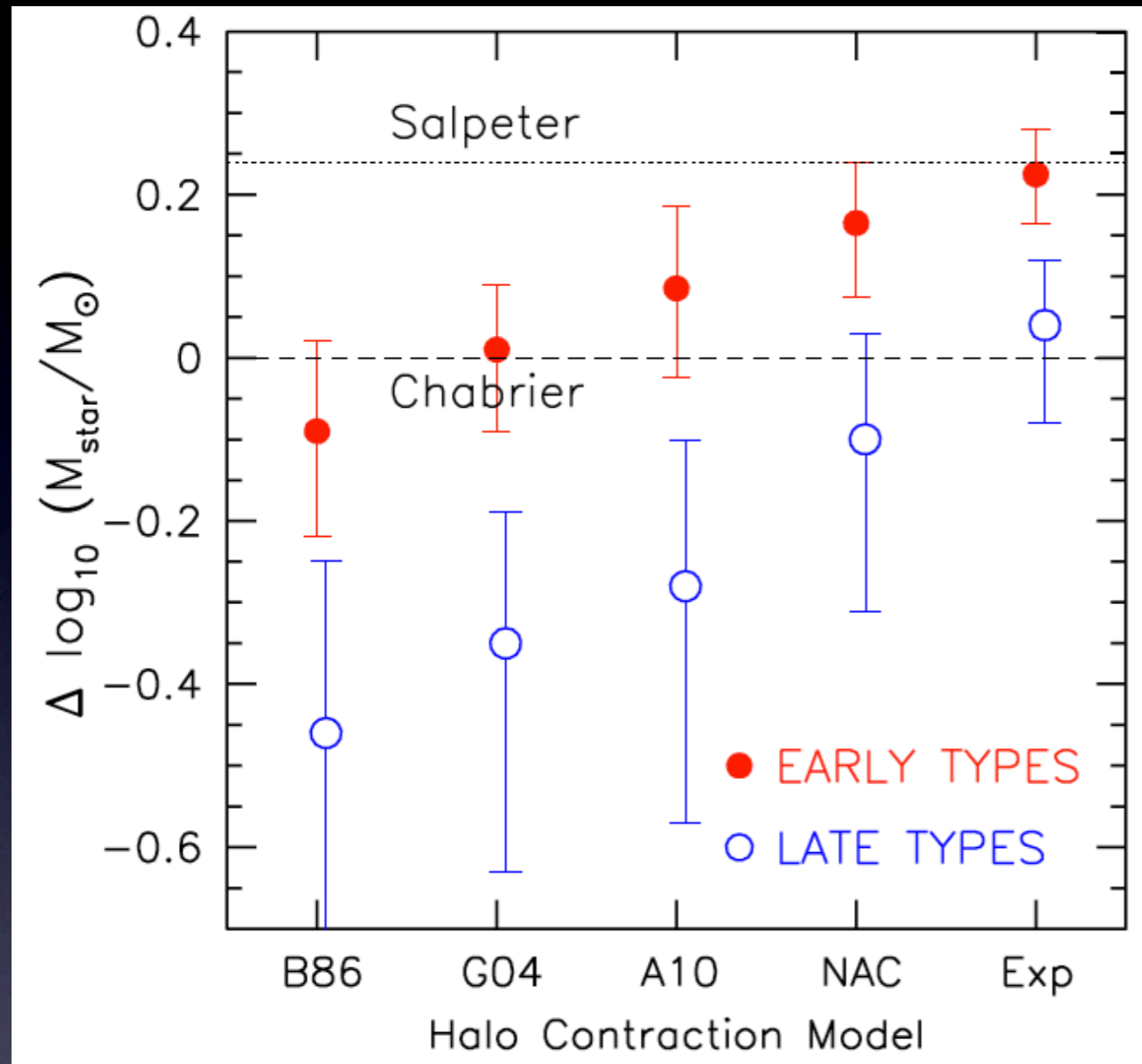


# Results



For a Chabrier IMF ( $\Delta_{\text{IMF}} = 0.0$ ), the zero-point of the TF relation requires halo expansion ( $\nu < 0$ ). However, for the same IMF, the zero-point of the FJ relation requires contraction with  $\nu = 0.8$ .

# Summary of Results



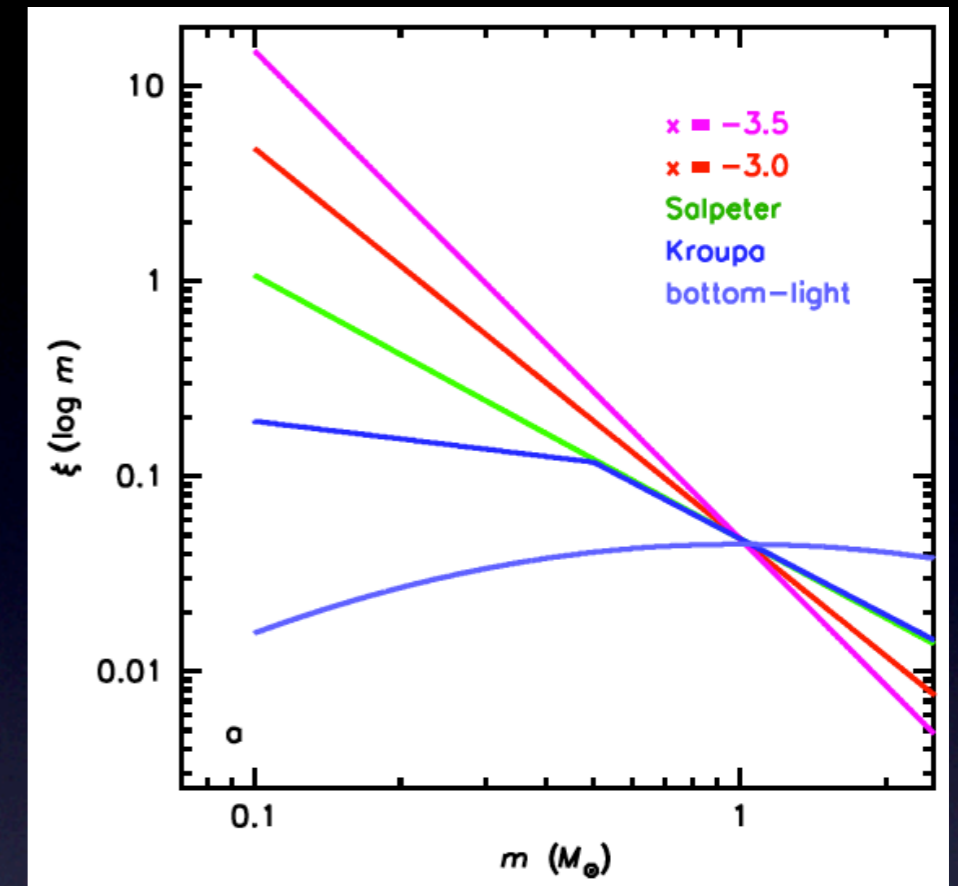
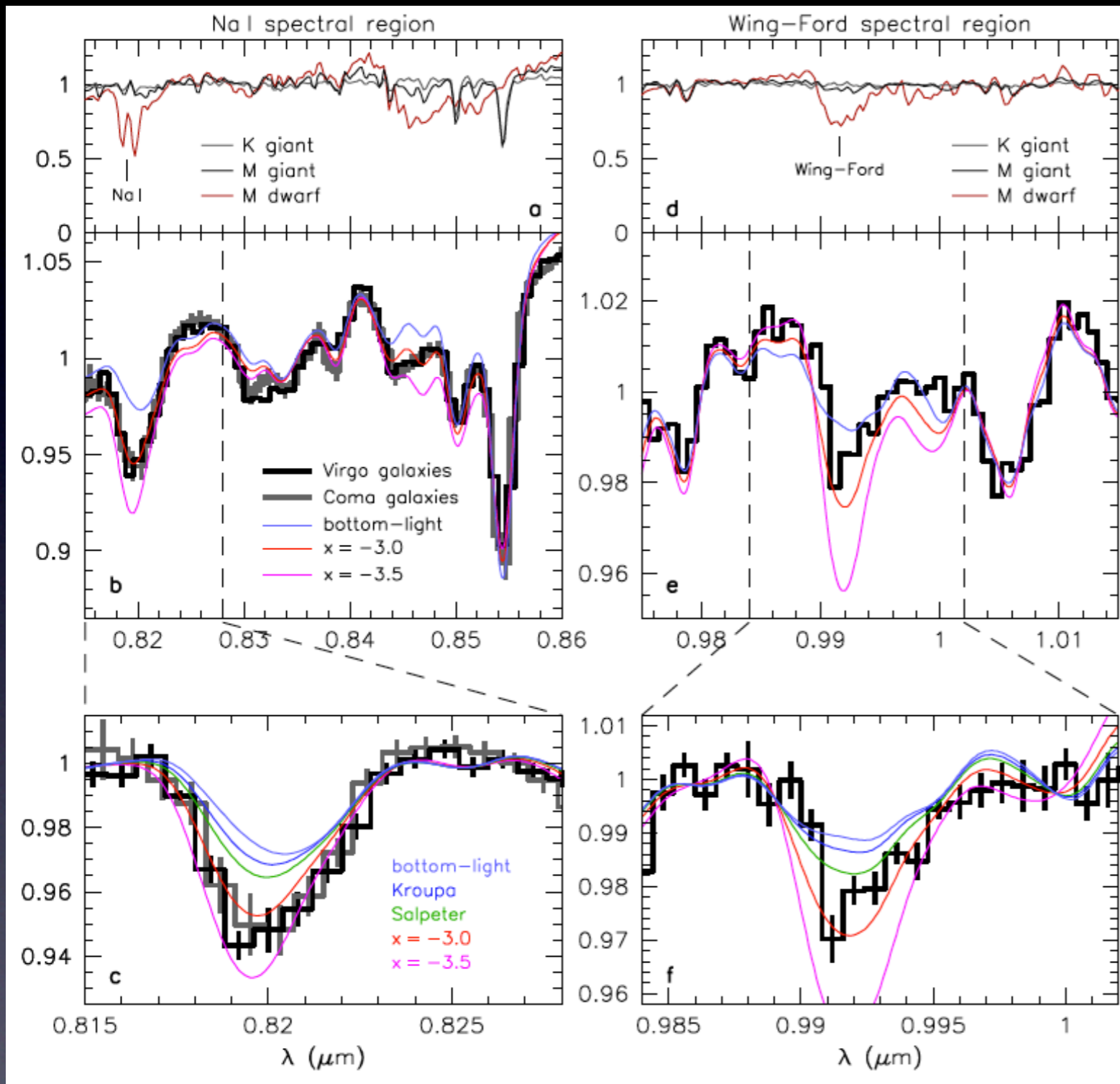
Early- and Late-type galaxies cannot have same IMF and have experienced the same amount of halo contraction!

In case of universal IMF, early-types must have experienced more halo contraction than late types.

In case of universal contraction, early-types must have IMF that is less top-heavy than in case of late-types.

IMF is power-law which turns over at low mass. Turn-over mass set by Jeans mass at formation, which is expected to increase with redshift due to  $T_{\text{CMB}}$  (Larson 1998). Early-types have older stellar populations, yielding IMF that is more top-heavy.

# A Bottom-Heavy IMF in Massive Ellipticals?

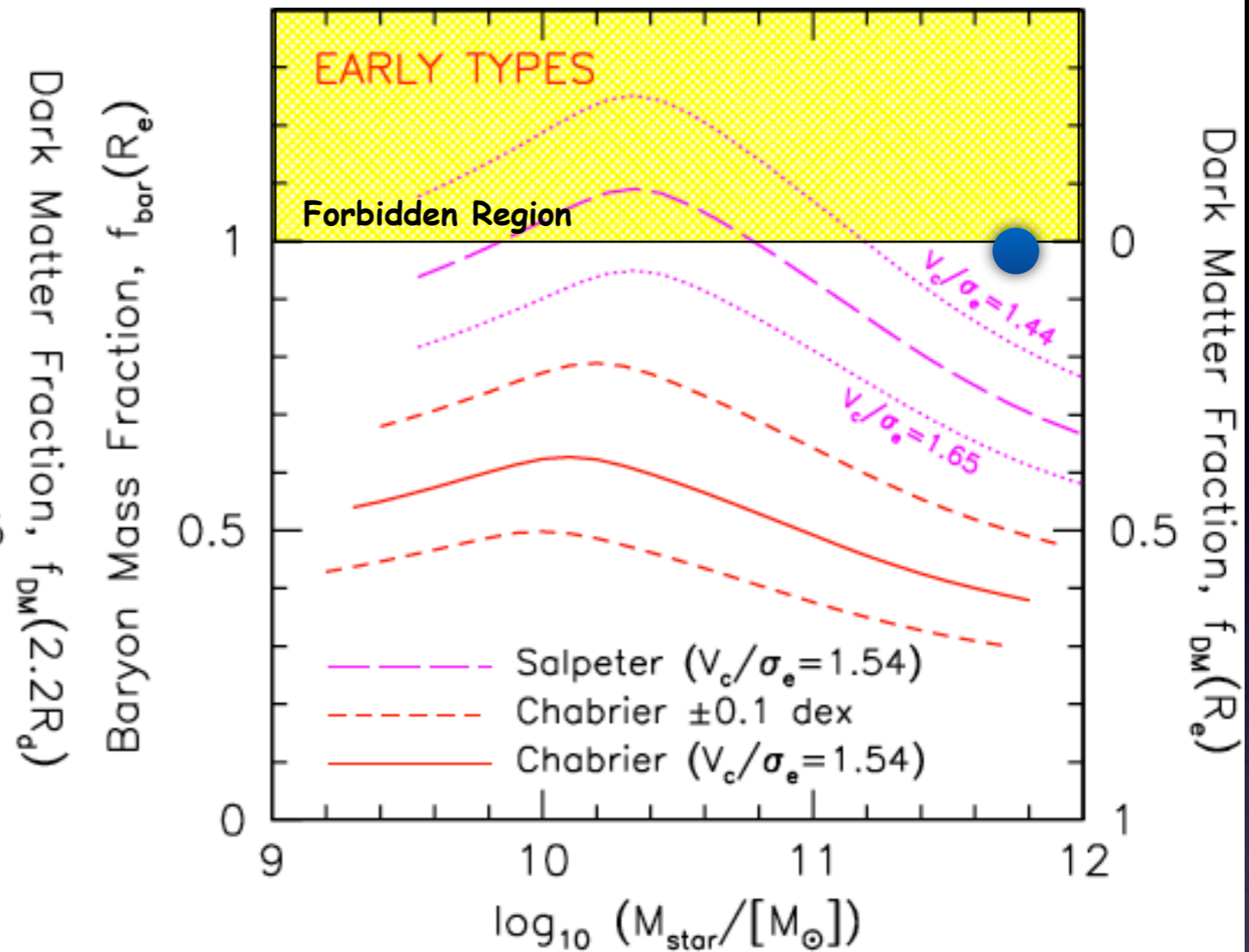
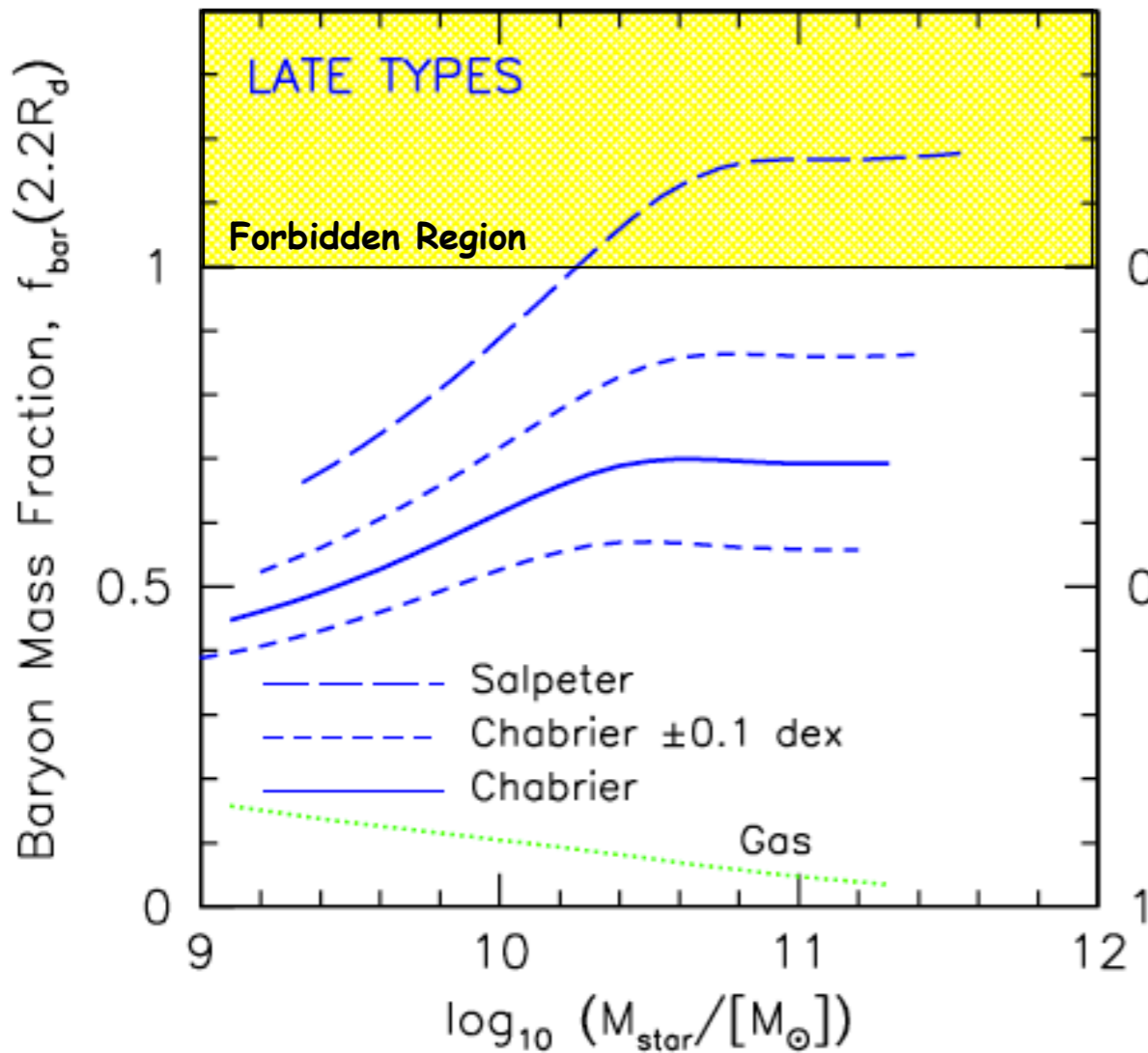


Sodium line and Wing-Ford band in spectra of nuclei of massive ellipticals reveal large population of low-mass stars; this suggests IMF that is more bottom-heavy than a Salpeter...

[van Dokkum & Conroy 2010]

Similar data of M31 globulars, which have similar age and metallicity, are consistent with Salpeter/Kroupa IMF [van Dokkum & Conroy 2011]

# Baryonic Mass Fractions



Bottom-heavy IMF of Conroy & van Dokkum CANNOT be present in lower mass early-types!