Star Formation Theory: Connecting the Local to the Extra-Galactic

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Frontiers in Star Formation Conference Yale, October 27, 2012

# SF Laws on Galactic Scales



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#### SF Laws on Sub-Galactic Scales



# Metallicity-Dependence





## Phase-Dependence



# The Theoretical Challenge

- Which laws are the fundamental ones, the local or the galactic-scale? Both? Neither?
- Can we unify the different sets of laws (at different scales, for different phases) within a single theoretical framework?

#### SF Laws: the Top-Down Approach



The idea in a nutshell: the SFR is set by *galactic-scale* regulation, independent of the local SF law. The local law is to be explained separately.

## **Q-Based Models**



Basic idea: SFR is a function of Toomre Q in galaxy

# Feedback Models



Also see Tasker (2011), E. Ostriker's talk

Mechanisms that regulate SF rate: supernovae, radiation pressure, ionized gas pressure, FUV heating

#### Characteristics of Top-Down Models



Changing the small-scale SF law does not change the SFR in the galaxy, but it does change the gas density distribution

# **Top-Down Model Limitations**



- Results depend strongly on subgrid feedback model (e.g. radiative trapping, SFE inside unresolved GMCs, UV heating per unit)
- No independent prediction for local SF laws

# Metallicity in Top-Down Models



Top-down models most naturally predict SF laws that do not depend on metallicity or phase, strongly inconsistent with observations

#### SF Laws: the Bottom-Up Approach



The idea in a nutshell: the SFR is set by a *local* SF law, plus a galactic-scale distribution of gas.

## The "Dense Gas" Model



Basic idea: SFR = M(> $\rho_{dense}$ ) /  $t_{dense}$ , with  $\rho_{dense}$ ,  $t_{dense}$  = const Problems: no physical basis for values of  $\rho_{dense}$ ,  $t_{dense}$ ; evidence for threshold mixed

# **Observed Local SF Law**



Local SF law: ~1% of gas mass goes into stars per free-fall time, independent of density or presence of massive stars

## Why is $\epsilon_{\rm ff}$ Low?

(Original model: Krumholz & McKee 2005; updates by Padoan & Nordlund 2011, Hopkins 2012, Federrath & Klessen 2012)

- Properties of GMC turbulence:  $\alpha_{vir} \sim 1$ , density PDF lognormal, LWS relation  $\sigma_v \sim \ell^{1/2}$
- Scaling: M ~ l<sup>3</sup>, PE ~ l<sup>5</sup>, KE ~ l<sup>4</sup>, so PE << KE, typical region unbound
- Only over-dense regions bound; integrating over lognormal PDF gives ε<sub>ff</sub> ~ 0.01



# Building a Galactic SF Law from a Local One

- Need to estimate characteristic density
- In MW-like galaxies, GMCs have  $\Sigma_{GMC} \sim 100$  $M_{\odot} pc^{-2}$ ,  $M_{GMC} \sim \sigma^4 / G^2 \Sigma_{gal}$ ; this gives

 $\rho_{\rm GMC} \sim G(\Sigma_{\rm GMC}^3 \Sigma_{\rm gal})^{1/4} / \sigma^2$ 

- In SB / high-z galaxies, Toomre stability gives  $\rho_{\rm T}\sim \Omega^2/GQ^2$
- Ansatz:  $\rho = max(\rho_T, \rho_{GMC})$

# **Combined Local-Galactic Law**



Krumholz, Dekel, & McKee 2012

#### Metallicity / Phase-Dependence



# **Chemical and Thermal Balance**

 ${
m H_{2}}$  formation  ${
m H_{1}}$  n  ${
m R}$  =  $n_{{
m H_{2}}} \int d\Omega \int d
u \, \sigma_{{
m H_{2}}} f_{{
m diss}} I_{
u}/(h
u)$  $\hat{e} \cdot \nabla I_{\nu} = -(n_{\mathrm{H}_2}\sigma_{\mathrm{H}_2} + n\sigma_{\mathrm{d}})I_{\nu}$ Absorption Decrease in by dust, H<sub>2</sub> rad. intensity

Line cooling  $n^2\Lambda = n \int d\Omega \int d
u \, \sigma_d E_{
m PE} I_
u/(h
u)$ 

 $\hat{e} \cdot \nabla I_{\nu} = -n\sigma_d I_{\nu}$ 

rad. intensity dust

Decrease in Absorption by

Caveat: this is assumes equilibrium, which may not hold

## Calculating Molecular Fractions

To good approximation, solution only depends on two numbers:

$$egin{array}{rll} au_{
m R} &=& n\sigma_{
m d}R \ \chi &=& rac{f_{
m diss}\sigma_{
m d}E_0^*}{n\mathcal{R}} \end{array}$$

An approximate analytic solution can be given from these parameters.



Analytic solution for location of HI /  $H_2$  transition vs. exact numerical result

# Calculating $f_{H_2}$



Qualitative effect:  $f_{H_2}$  goes from ~o to ~1 when  $\Sigma Z$  ~ 10  $M_{\odot}~pc^{-2}$ 

# Why Does SF Follow H<sub>2</sub>?





# The Local HI – H<sub>2</sub> Transition



Lee+ 2012

#### **Extra-Galactic Phase Dependence**



# The Future: Mapping out the Space Between Local and Galactic



# Extragalactic SF Laws at High Resolution





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#### Comparison to Model



#### **Comparison to Model**



# SF Laws in Many Lines



#### **Comparison to Model**



# Summary

- Can local and extra-galactic laws be unified? Depends on whether SF regulation is topdown or bottom-up
- Can laws for different phases / metallicities be unified with other laws? Yes, but this only happens naturally in a bottom-up framework.
- Promising approach: measure and predict SF laws at intermediate scales and densities