PROPERTIES OF THE DISTANT KUIPER BELT: RESULTS FROM THE PALOMAR DISTANT SOLAR SYSTEM SURVEY

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ABSTRACT

We present the results of a wide-field survey using the 1.2 m Samuel Oschin Telescope at Palomar Observatory. This survey was designed to find the most distant members of the Kuiper Belt and beyond. We searched $\sim 12,000 \text{ deg}^2$ down to a mean limiting magnitude of 21.3 in *R*. A total number of 52 Kuiper Belt objects and Centaurs have been detected, 25 of which were discovered in this survey. Except for the redetection of Sedna, no additional Sedna-like bodies with perihelia greater than 45 AU were detected despite sensitivity out to distances of 1000 AU. We discuss the implications for a distant Sedna-like population beyond the Kuiper Belt, focusing on the constraints we can place on the embedded stellar cluster environment the early Sun may be have been born in, where the location and distribution of Sedna-like orbits sculpted by multiple stellar encounters is indicative of the birth cluster size. We also report our observed latitude distribution and implications for the size of the plutino population.

Key words: Kuiper Belt: general – Oort Cloud

Online-only material: color figure, machine-readable table

1. INTRODUCTION

With the advent of wide-field CCD cameras in the past decade, there has been an explosion in observational programs searching for Kuiper Belt objects (KBOs; Jewitt & Luu 1995; Jewitt et al. 1996, 1998; Sheppard et al. 2000; Larsen et al. 2001, 2007; Trujillo et al. 2001; Trujillo & Brown 2003; Elliot et al. 2005; Brown 2008; Kavelaars et al. 2009). Now there are over 1000 KBOs known, with about half having secure orbits. The majority of these surveys search for distant solar system bodies using images taken on a single night over a span of a few hours, probing out to distances of ~100 AU. Most of these surveys have focused on observing within 10° of the ecliptic with the majority only imaging within just a few degrees.

The discovery of Sedna (Brown et al. 2004) on a highly eccentric orbit far outside the Kuiper Belt challenges our understanding of the solar system. With a perihelion of 76 AU, Sedna is well beyond the reach of the gas giants and could not be scattered into its highly eccentric orbit from interactions with Neptune alone (Emel'yanenko et al. 2003; Gomes et al. 2005a). Sedna's aphelion at 1000 AU is too far from the edge of the solar system to feel the perturbing effects of passing stars or galactic tides in the present-day solar neighborhood (Duncan et al. 1987; Fernandez 1997). Sedna is dynamically distinct from the rest of the Kuiper Belt, and its unexpected discovery alludes to a population of icy bodies residing past the Kuiper Belt with perihelia greater than 45 AU and semimajor axes greater than \sim 200 AU, beyond which Neptune is unable to raise the perihelia of scattered disk KBOs through resonant perturbations (Gomes et al. 2005a).

Sedna is the only body known to reside in this region. Sedna was found near perihelion at a distance of \sim 88 AU, at the motion limit, and brightness limit of its discovery survey (Brown et al 2008). With one night imaging, previous KBOs surveys were likely insensitive to the objects in the Sedna region. To date, surveys (Larsen et al. 2007; Brown 2008; Parker & Kavelaars 2010) have been unsuccessful in finding additional

Sedna-like bodies. In order to find the largest and brightest members of the Sedna population, we have been engaged in an observational campaign to survey the northern sky. We present the results of our search for distant solar system bodies covering $\sim 12,000 \text{ deg}^2$ within 30° of the ecliptic. Rather than searching over a single night, we use a two-night baseline to distinguish the extremely slow motions of these distant bodies from background stars. We are sensitive to motions out to a distance of $\sim 1000 \text{ AU}$ ($\sim 0'.2 \text{ hr}^{-1}$).

In this paper, we discuss the implications for a distant Sednalike population beyond the Kuiper Belt and provide constraints on the cluster birth Sedna formation scenario (Brasser et al. 2006). The survey was specifically designed to find the select brightest members of a distant Sedna population but was also sensitive to the dynamically excited off ecliptic populations of the Kuiper Belt including the hot classicals, resonant, scattered disk, and detached Kuiper Belt populations. We present our observed latitude distribution and implications for the plutino population.

2. OBSERVATIONS

Observations were taken nightly using the robotic 1.2 m Samuel Oschin Telescope located at Palomar Observatory and the QUEST large-area CCD camera. The QUEST camera has an effective field of view of 8.3 deg² with a pixel scale of 0''.87 (Baltay et al. 2007). The 161 megapixel camera is arranged in four columns or "fingers" along the east–west direction each equipped with 28 2400 ×600 CCDs in the north–south direction (see Figure 1). The gap between CCDs in the north–south direction is ~1'.2 and the spacing between adjacent fingers along the east–west direction is ~25'. The four fingers are labeled (A–D) and the CCDs are numbered sequentially (1–28) from north to south. We will refer to the CCDs by finger and position along the finger (i.e., C14, D28).

Observations were taken from 2007 May 8–2008 September 27. We have surveyed in total 11,786 deg² within $\pm 30^{\circ}$ of the

Table 1	
Summary of Field Positions	s

Pointing	R.A.	Decl.		Night 1		Night 2			
	(J2000)	(J2000)	MJD Obs1	MJD Obs 2	Mag. Limit	MJD Obs 1	MJD Obs 2	Mag Limit	
1	13 53 27.599	-18 15 59.80	54228.327	54228.333	20.9	54229.189	54229.237	21.4	
2	13 55 33.959	-18 15 59.80	54228.330	54228.336	21.1	54229.192	54229.240	21.5	
3	13 22 04.440	-134328.20	54228.313	54228.320	20.6	54229.163	54229.209	20.9	
4	13 38 45.960	-13 43 28.60	54228.260	54228.266	21.4	54229.169	54229.216	21.3	
5	13 40 49.440	-13 43 27.50	54228.263	54228.269	21.4	54229.172	54229.219	21.4	
6	13 55 27.841	-13 43 27.80	54228.205	54228.211	21.2	54229.176	54229.222	21.3	
7	12 51 16.560	-09 10 55.60	54228.273	54228.279	21.0	54229.183	54229.230	21.4	
8	12 53 18.240	-09 10 55.90	54228.276	54228.283	21.1	54229.186	54229.233	21.4	
9	13 07 40.440	-09 10 55.90	54228.219	54228.226	21.3	54229.196	54229.243	21.5	

Notes. The center coordinates for all pointings searched for KBOs and used in the analysis presented in this paper. The table includes pointing number, the right ascension and declination of the mosaic center CCD (B15), MJD dates of all four observations of the field and limiting magnitudes for each night the field was observed.

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)



Figure 1. Scale drawing of the focal plane of the QUEST camera, depicting the layout of the 112 CCDs. The gap between CCDs in the north–south direction is \sim 1/2 and the spacing between adjacent fingers along the east–west direction is \sim 25'.

ecliptic to a mean depth of *R* magnitude 21.3. Our sky coverage is shown in Figure 2. Field centers are compiled in Table 1. A forest fire on Palomar Mountain prevented observations in 2007 September and camera malfunctions ceased operations from 2008 February–2008 May leading to gaps in longitudinal coverage. After 2008 May normal observations resumed until the QUEST camera ceased operations on the Oschin telescope at the end of 2008 September.

Target fields were observed over a two-night baseline in order to search for solar system objects out to distances of ~ 1000 AU (moving at speeds as low as 0.2 hr⁻¹). All exposures were taken

through the broadband red RG610 filter (IIIaF filter from the POSS-II survey) with a wavelength range of $\lambda = 610-690$ nm (Reid et al. 1991). For each field, a pair of 240 s exposures was taken separated by ~ 1 hr on each of the two nights. The second night of observations was typically the next day or at most four nights later. Observations were in varying photometric conditions and lunations. To check the photometric quality of each nightly pair of observations, magnitudes of the detected sources from both images were histogram binned with a bin size of 0.2 mag, and the peak value of the histogram was selected as an indicator of image depth. If the median value of the five best CCDs (B11, C19, D09, D12, D13) was less than 20.4 mag (19.0 mag for crowded fields with greater than 4000 detected sources), then the observation was rejected as poor quality, and the target field was rescheduled for new observations the next night. If a target field could not be successfully imaged within four nights of the first pair of observations, the field was reset and scheduled for another two nights of observations.

All target fields were observed within 42° of opposition, and to avoid high star densities, fields less than 15° from the galactic plane were avoided. The camera R.A. CCD gap was covered by adjacent pointings, but the ~1/2 declination gap remains mostly uncovered in our survey observations. When all opposition fields within $\pm 30^{\circ}$ of the ecliptic for a month's lunation were completed, overlap pointings were then targeted to reduce holes in our sky coverage due to the camera's declination gap and defective CCDs. From the beginning of the survey to 2007 November 12, instead of performing overlapping coverage, fields with ecliptic latitudes greater than 30° were instead targeted once all available opposition fields within 30° of the ecliptic were completed.

3. DATA ANALYSIS AND OBJECT DETECTION

3.1. Moving Object Detection

Observations were processed nightly though an automated reduction pipeline using the Interactive Data Language (IDL) Software package. Each CCD on the detector was reduced and searched for moving objects independently from the other CCDs on the mosaic. All images were bias-subtracted and flat-field corrected. A row-by-row median of the overscan region was used for the bias subtraction. A master flat-field image for each CCD was constructed from a 3σ clipped median of the night's science images. Some of the camera CCDs had a significant



Figure 2. Sky coverage of the Palomar survey plotted on the J2000 sky. The observed fields are plotted to scale. The plane of the Milky Way is denoted as a dashed line, and the ecliptic is denoted as a solid line. Holes are due to galactic plane avoidance, bad weather, forest fires, and hardware malfunctions.

fraction of hot or defective pixels. These pixels were identified as those where the flat-field image value deviated by more than 0.7% from the value of the 3×3 median boxcar filtered flat-field image. To mask the effects of these hot pixels, those regions of the science image were replaced by the median value of a 3×3 pixel box centered on the bad pixel. If hot/bad pixels constituted more than 20% of the image than a 3×3 median boxcar smoothed image was substituted for analysis.

SExtractor (Bertin & Arnouts 1996) was run on each image to compile a list of sources. SExtractor was tuned such that source detection constituted four or more contiguous pixels (DETECT_MINAREA parameter) above the detection threshold (DETECT_THRESH parameter) of 1.2σ above the sky background. Chips C14, C04, and D26 had significant image defects and higher SExtractor detection thresholds were used for these three CCDs (DETECT_MINAREA = 5 and DETECT_THRESH = 2.3) SExtractor performed circularaperture photometry using a 5 pixel radius aperture. Each source was characterized by its position, flux, and shape. The best of the four images was selected as the master template whose astrometric solution was found by matching image stars to the USNO A2.0 catalog (Monet 1998). The other three images were then aligned relative to the stars in the template image. Even if the absolute astrometry failed, the relative astronomy between the images was still sufficient to search for distant solar system bodies. The median absolute astrometric error for the entire survey was 0'.'4. The median relative astrometric error between survey images was 0''.076.

Once astrometric solutions had been found, the images were searched for moving objects. Because our observations were taken at or near opposition, slow-moving solar system objects were identified by their retrograde motion due to the parallax caused by the Earth's orbital motion. Distant planetesimals may move too slowly to show apparent motion over the nightly 1 hr baselines and appear stationary on individual nights. To ensure the detection of objects out to distances of ~ 1000 AU, we only required motion to be identified over the two-night baseline. The detection catalogs from all four

images were compared to identify and eliminate the stationary sources in each image. Sources on one image that had a counterpart within a 4" radius on either of the second night's observations were removed as background stars. To further cull the object lists of stars that were above the SExtractor thresholds on one night but below the detection limit on the other, we generated SExtractor source catalogs with more sensitive detection parameters (DETECT_MINAREA = 3 and DETECT_THRESH = 1.1), and compared these deep catalogs to our detection lists. Image sources from one night that appeared on the other night's deep detection catalogs were deemed stationary and rejected as well. Saturated stars and extended sources whose peak flux was more than 3 pixels from the source center measured by SExtractor were also removed from the object catalogs.

Potential moving candidates were identified from the remaining unmatched sources. The nightly images were searched for moving object pairs with motions less than $14^{\prime\prime}_{...4}$ hr⁻¹, the velocity of bodies at distances of 10 AU. Moving object pairs from the first night and pairs from the second night separated by more than 4".38 with retrograde motion consistent with opposition were linked. To eliminate stationary image sources that had been linked between the two nights, candidates with average nightly magnitudes differing by more than 1 mag were eliminated. Remaining candidates whose nightly motions differ by less than twice the first night's on-sky velocity were kept to create the list of moving object candidates. Candidates were filtered via the orbit-fitting package described in Bernstein & Khushalani (2000). Those candidates with successful orbit fits which produced a χ^2 less than 25 and barycentric distance between 15 and 1000 AU were identified as moving objects and added to the final list of candidates to be screened by eye. 100×100 pixel subimages for each of the final moving object candidates were created from the discovery images. These snapshots were aligned and blinked by eye. A total of 39,110 candidates (~200 a night) were visually inspected. Typical false positives included diffraction spikes, faint background stars, blended sources, and CCD imperfections.

3.2. Recovery Observations

At discovery, heliocentric distance and inclination can be identified from the parallax effect due to the Earth's motion, but other orbital parameters remain unconstrained. With only a two-night discovery arc, a distant Sedna-like body cannot be distinguished from a typical scattered disk KBO near aphelion. Even with follow-up observations a month after discovery, both families of orbits provide reasonable astrometric fits to the observations. The two orbital solutions diverge sufficiently a year after discovery, and a secure dynamical identification can only be made after these additional observations.

Recovery observations of new discoveries were taken at the Palomar 60 inch telescope, the Palomar 200 inch telescope, the 0.9 m telescope operated by the SMARTS consortium at Cerro Tololo Inter-American Observatory, the 42 inch John S. Hall Telescope located at Lowell Observatory, the 2.66 m Nordic Optical Telescope located at el Roque de los Muchachos Observatory, and the 8.2 m Subaru Telescope on Mauna Kea. Of our detected KBOs, 96% have multiopposition observations. All but two discoveries classified as KBOs by the Minor Planet Center (MPC; 2007 JF45 and 2007 PS45) were recovered during the survey. The two unrecovered objects were discovered during reprocessing of the data with more sensitive SExtractor source detection parameters and were discovered after they were no longer observable. Observations taken near 40° from opposition, contained contamination from asteroids near their stationary points that appeared to be moving at rates similar to distant KBOs. Some were identified with subsequent observations that confirmed these objects were on orbits with semimajor axes less than 5 AU. All other objects not successfully recovered have either been linked with other asteroid observations or have been classified on orbits well short of the Kuiper Belt by the MPC database⁴.

3.3. Calibration and Efficiency

3.3.1. Limiting Magnitude

The survey observations were taken during a wide variety of photometric, seeing, and weather conditions. Each CCD frame was independently photometrically calibrated. A photometric zero-point offset to our instrumental magnitudes was derived relative to the USNO A2.0 catalog (Monet 1998) red magnitude. The photometric uncertainty of the USNO catalog is nonnegligible. For magnitudes greater than 17, the uncertainty is 0.3 mag (Monet 1998). We likely have several tenths of magnitude uncertainty in our discovery magnitudes. We have not precisely calibrated the survey depth with calibration observations. Limiting magnitudes were computed based on the USNO catalog. We found that the faintest magnitude with a 5σ (10 σ for C2 A19, C14, C04, D26; CCDs with larger numbers of hot pixels) uncertainty as reported by SExtractor represented an accurate measure of the source detection limit of our images, and we used these values in the work presented in this paper. The limiting magnitude for each nightly pair of field observations was taken as the depth of the shallower of the two images. The mean limiting magnitude of the survey based on the USNO catalog is 21.3 in R.

3.3.2. Survey Efficiency

Because our survey has covered a wide swath of sky detecting multiple previously known KBOs, we have an alternative be detected and no visible moving source was identifiable. We define the survey efficiency function as

bad due to poor telescope tracking, or the KBO was too faint to

$$\varepsilon = \frac{\varepsilon_{\max}}{2} \left(1 - \tanh\left(\frac{m - m^*}{g}\right) \right), \tag{1}$$

where ε is the efficiency with which KBOs of magnitude m are detected in our survey, ε_{\max} is the maximum efficiency, m^* is the magnitude at which $\frac{\varepsilon_{\text{max}}}{2}$, and g is the half width. We fit for the efficiency by computing the cumulative distribution for all known KBOs scaling for the probability of detection and compare to the observed cumulative distribution. To find the optimal parameters, we minimize the χ^2 between the observed and calculated cumulative distributions. We find $\varepsilon_{\text{max}} = 0.66$, $m^* = 21.5$, and g = 0.05. The efficiency drops by 50% at 21.5 V mag, consistent with our median image limiting magnitude. Figure 3 plots the best-fit efficiency function and plots the binned detection efficiency for the known sources located on all four field images in 0.5 mag bins. We estimate the uncertainty in our survey efficiency using the number of known KBOs found with magnitudes less than or equal to 21st magnitude, well before the dropoff in the best-fit efficiency function. We found 13 of 19 known KBOs brighter than or equal to 21st magnitude, giving an efficiency of 68%, consistent with our bestfit efficiency function, and assuming Poisson counting statistics, the 1σ confidence level ranges from 51% to 89%.

⁴ http://www.cfa.harvard.edu/iau/Ephemerides/Distant/index.html

method of determining the limiting magnitude of our survey. Of our detections, 27 are previously discovered KBOs and Centaurs in the MPC database. The absolute magnitudes recorded in the MPC are based upon the apparent magnitudes measured from the discovery or follow-up observations, like our survey, which are often taken in non-standard filters and observed without precise photometric calibrations. Romanishin & Tegler (2005) find the absolute magnitudes recorded in the MPC are systematically 0.3 mag brighter than those magnitudes accurately measured for their sample of 90 KBOs and Centaurs. We can still use the known population of bright KBOs to estimate a crude efficiency for the survey. We obtained the positions and visual apparent magnitudes computed by JPL Horizons⁵ for known KBOs. As of 2010 January 20, there were 64 previously known multiopposition KBOs with visual magnitudes brighter than 22nd magnitude (excluding discoveries found in this survey and objects with a < 30) with predicted positions located on our survey images that could have been detected by our detection pipeline. We only considered KBOs positioned on the same CCD for all four field observations, not accounting for masked regions of the CCDs. Masked bad pixel regions account for $\sim 8\%$ of the QUEST camera's observable area, but likely the loss due to bad pixels is much smaller than this value. A KBO positioned on a bad pixel may not necessarily be lost, SExtractor interpolates values for masked pixels from neighboring good pixels before source detection. For every object not detected in the survey, we examined the images to determine if a moving source was visible. No known KBO was missed during the visual inspection of moving object candidates. The majority of the missed KBOs were not found because the KBO's psf overlapped with a neighboring star and was missed by SExtractor, the KBO was on a bad or masked off region of the CCD, image quality was

⁵ http://ssd.jpl.nasa.gov/horizons.cgi



Figure 3. Survey efficiency based on the previously known multiopposition KBO population. Solid line plots the best-fit efficiency function. Diamonds plot the binned detection efficiency in 0.5 mag bins with 1σ Poissonian error bars. The dashed line with triangles is the number of previously known multiopposition KBOs (a > 30 AU) in each magnitude bin with predicted positions located on all four survey images.

3.3.3. Geometric Losses

The gap between the QUEST camera's CCDs in the north-south direction is $\sim 1'_2$. Along the east-west direction, the separation between CCDs is $\sim 25'$. At the distances our survey is sensitive to, a KBO located in the declination gap would remain in the gap between CCDs over the two-night baseline. This was the case for Eris, and Eris was not detected in our survey. For some areas of the sky, we do have overlap pointings to try and cover the declination gap but only after all opposition target fields were observed. The losses due to the CCD gaps is accounted for in our sky coverage estimates, but we do not include the loss due to masked regions.

KBOs that moved off the edge of the CCD into the CCD gaps were missed by our automated detection pipeline. Nonfunctioning CCDs and longitudinal losses are accounted for in our latitudinal sky coverage estimates, but to measure our geometric losses from those KBOs moving off the CCDs or lost in the CCD gaps, we generated $\sim 10^6$ random circular orbits assuming a uniform inclination distribution $(0^{\circ}-180^{\circ})$ for a range of semimajor axes. Neglecting the effect of masked CCD regions, we calculated the fraction of simulated KBOs positioned on all four survey images as a function of ecliptic latitude. Figure 4 compares our survey sky coverage to the fractional coverage of the simulated circular orbits at 30, 50, and 100 AU. The greatest losses occur at the ecliptic, and we find this effect is at most $\sim 10\%$. Closer orbits are moving at faster on-sky velocities and are more likely to move off the CCD over the two-night baseline than objects at further distances, but we find the difference in losses by objects at 30 and at 100 AU is small, and that all objects in the Kuiper Belt have similar geometric losses in our survey.

3.3.4. Pipeline Detection Efficiency of Sedna-like Bodies

Any comparison of the Sedna population requires that we also understand whether these bodies would be detected in our survey. Many of the mechanisms proposed for the formation of Sedna (Kenyon & Bromley 2004; Morbidelli & Levison 2004;

Brasser et al. 2006, 2007; Kaib & Quinn 2008) produce many highly eccentric and even retrograde orbits. To test whether Sedna-like orbits would pass through our orbit-fitting filter, we created artificial orbits with a uniform semimajor axis ranging from 100 to 1100 AU and uniform eccentricity and inclination distribution including retrograde orbits. For those 781,763 artificial orbits whose positions land on our images, have barycentric distances less than 1000 AU, and have perihelia greater than 50 AU, we add absolute and relative positional offsets characteristic of the survey's astrometric errors. All four images of a field observation have the same absolute astrometric error but random relative positional errors. We add normally distributed random absolute and relative astrometric errors using the 3σ clipped median and standard deviation of the survey astrometric uncertainties. As shown in Figure 5, the efficiency is the fraction of synthetic orbits fit with the Bernstein & Khushalani (2000) software that pass our selection criteria in each semimajor axis bin compared to the number of objects in the 100 AU bin. Five percent of the simulated orbits would not have made it through to visual inspection with the majority of failures due to the best-fit orbit placing the object on an asteroidlike orbit. We are confident that Sedna-like bodies present in our images detected by SExtractor would be identified by our automated detection scheme.

4. DETECTIONS

A total of 52 KBOs and Centaurs have been detected of which 25 are new discoveries from this survey. Fifty of our discovered objects have multiopposition orbits. Table 2 lists the orbital information for objects detected in the survey. The orbital and radial distribution is plotted in Figures 6 and 7, respectively. With the detection of no cold classical belt objects, our overall survey probes the orbital properties of the hot classical, scattered disk, detached, and resonant populations. The survey was specifically designed to probe the Sedna region, but except for Sedna, no additional objects with perihelion greater than 45 AU were detected despite sensitivity out to distances of 1000 AU.



Figure 4. Effect of geometric losses on the sky coverage of the survey. The fraction of simulated orbits found on all four CCDs as a function of latitude binned in 2° bins. Main effects are due to KBOs that are not located on all field observations and move off the CCD or objects positioned in the gaps between the CCDs.



Figure 5. Efficiency of our orbit-fit detection filter. Fraction of synthetic orbits with barycentric distances between 15 and 1000 AU that are successfully identified as outer solar system bodies found on all four survey images vs. semimajor axis binned in 100 AU bins.

We do detect several Centaurs with semimajor axes less than 30 AU in our survey, but to constrain the number of false detections by inner solar system objects we placed a minimum distance threshold in our moving object detection scheme. Candidates with barycentric distances less than 15 AU as calculated from initial orbits fit by the Bernstein & Khushalani (2000) method were ignored. Our survey is limited to detecting only the most distant of the Centaurs, and we therefore will not address the Centaur population in this paper.

5. SEDNA POPULATION

With a perihelion of 76 AU and an aphelion of \sim 1000 AU Sedna is dynamically distinct from the rest of the Kuiper Belt.

Its extreme orbit suggests the presence of a population of icy bodies residing past the Kuiper Belt. The study of this Sedna population provides a unique new window into the history of the early solar system. Some other mechanism no longer active in the solar system today is required to emplace Sedna on its highly eccentric orbit. Several possible scenarios have been offered to explain Sedna's extreme orbit, including interactions with planet-sized bodies (Gladman & Chan 2006; Gomes et al. 2006; Lykawka & Mukai 2008; Gomes & Soares 2010), stellar encounters (Morbidelli & Levison 2004), multiple stellar fly-bys in a stellar birth cluster (Morbidelli & Levison 2004; Brasser et al. 2006, 2007; Kaib & Quinn 2008), interstellar capture (Kenyon & Bromley 2004; Morbidelli & Levison 2004), and perturbations from a wide-binary solar companion (Matese et al.



Figure 6. Eccentricity vs. semimajor axis and inclination vs. semimajor axis of multiopposition objects found in the Palomar survey. Sedna has been excluded for better resolution. 1σ errors from Bernstein & Khushalani (2000) orbit fit are plotted. The error bars are typically smaller than the size of the symbol.

2005). Each of the various Sedna formation models leaves a distinctive imprint on the members of this class of distant objects and has profound consequences for our understanding of the solar system. These planetesimals in the Sedna region are dynamically frozen and the relics of their formation process. The orbital distribution and number density of Sedna-like bodies will distinguish between the formation scenarios.

In Schwamb et al. (2009), before recovery observations were complete, we compared the expected number of detections from a theoretical population on orbits with the same semimajor axis and eccentricity as Sedna to our survey results, the redetection of Sedna. Our best-fit value gives 40 bodies residing on Sedna's orbit that are brighter than or equal to Sedna. At the 1σ confidence level we ruled out a population larger than 92 and smaller than 15 Sedna-sized or bigger objects on orbits similar to Sedna's. Our previous work had been limited to examining a model population of bodies residing specifically on Sedna's orbit. Any realistic Sedna population likely occupies a much larger region of orbital space, possibly including objects with sufficiently high perihelia that they would never or rarely become bright enough to see. With secure orbital classifications for survey objects, we can now test more sophisticated orbital distributions.

5.1. Constraints on a Cluster Birth

No new Sedna-like bodies with perihelia beyond 45 AU were found in the survey despite a sensitivity out to distances of ~ 1000 AU. Although we cannot differentiate between the Sedna origin scenarios with a single detection, we can place constraints on the cluster birth model where the location and distribution of Sedna-like orbits is indicative of the Sun's birth cluster size. Most stars are born in dense gas-rich embedded



Figure 7. Inclination vs. barycentric distance at discovery for objects detected in the Palomar survey. 1σ errors from Bernstein & Khushalani (2000) orbit fit are plotted. The error bars are typically smaller than the size of the symbol.

clusters (Lada et al. 1991; Carpenter 2000; Porras et al. 2003; Lada & Lada 2003; Allen et al. 2007), and it is likely that the Sun spent several million years in such an environment. The presence of short-lived radioactive nuclides in primitive meteorites may provide circumstantial evidence that the Sun was in relatively close proximity to a supernovae early on in the solar system's formation (Chaussidon & Gounelle 2007; Brennecka et al. 2009, and references therein) and therefore in a much denser environment than the present-day solar neighborhood. In the dense stellar nursery, encounters between nearby solar neighbors and the Sun would occur at a much higher frequency than in the present solar environment (Adams & Laughlin 2001; Laughlin & Adams 1998; Proszkow & Adams 2009; Adams 2010). Close fly-bys of passing stars would perturb objects in the Sun's planetesimal disk onto highly eccentric Sedna-like orbits (Morbidelli & Levison 2004; Brasser et al. 2006, 2007; Kaib & Quinn 2008).

Brasser et al. (2006) successfully produce objects on orbits similar to Sedna's in simulations of embedded cluster environments. The gravitational effects of both stars and gas in the cluster are included in their integrations. If the mean density of the material the Sun encounters while residing in the embedded cluster was $\sim 10^3 M_{\odot} \text{ pc}^{-3}$ (central cluster densities of $10^4 M_{\odot} \text{ pc}^{-3}$) or denser, Sedna's orbit is recreated and a distribution of Sedna-like bodies with semimajor axes less than 10,000 AU is formed. Brasser et al. (2006) find that the central density of the stellar cluster (directly correlated to the amount of material the Sun encounters in the cluster) determines the orbital distribution of Sedna-like bodies generated. The denser the cluster environment, the smaller semimajor axis at which the Sedna population begins. For this paper, we focus specifically on the Brasser et al. (2006) results for the 10^4 , 10^5 , and $10^6 M_{\odot} \text{ pc}^{-3}$ embedded cluster integrations ($10^3 M_{\odot} \text{ pc}^{-3}$ did not produce Sedna). We refer the reader to their paper for details of the orbital integrations and the review of embedded clusters by Lada & Lada (2003). Figure 8 shows the orbital distributions from the embedded cluster numerical simulations used in this work.

Our survey observations probe the Sedna population today after 4.5 Gyr of evolution. The distribution of orbits presented by Brasser et al. (2006) is what remains after 3 Myr when the integrations end and the Sun is expected to have left the birth cluster. Once the Sun exits the cluster, the Galaxy becomes the dominant gravitational potential. The gravitational perturbations from galactic tides over the age of the solar system have not been accounted for in the Brasser et al. (2006) integrations. Sedna's orbit is protected from the effects of passing stars and galactic tides in the current solar environment, but objects with higher semimajor axes than Sedna may be perturbed onto comet-like orbits (Duncan et al. 1987; Fernandez 1997). Kaib & Quinn (2009) examined the production of long period comets in the Sedna region and find that the production efficiency drops significantly for bodies with a <3000 AU compared to those with larger semimajor axes. Therefore, we expect that objects emplaced onto Sedna-like orbits with semimajor axes less than 3000 AU should remain to the present day, and we do not include any orbits from the cluster simulations with a \geq 3000 AU in comparisons to our observations.

The Nice model (Tsiganis et al. 2005; Gomes et al. 2005b) predicts that the giant planets were in a more compact configuration than in the present-day solar system. The orbits of the giant planets went unstable approximately 1 Gyr after the formation of the solar system causing the migration of the giant planets and scattering of planetesimal disk. Jupiter migrates inward, and the remaining giant planets move outward with Neptune migrating outward to 30 AU. The oldest embedded clusters are \sim 5 Myr old (Leisawitz et al. 1989; Lada & Lada 2003), Neptune migrates well after the Sun has left the birth cluster and the emplacement of the Sedna population. Brasser (2008) confirms this scenario can create a Sedna population and generate an Oort cloud population within the current estimates of the mass of the Oort cloud. Neptune's orbit became eccentric during migration and was later circularized via scattering of planetoids in the Kuiper Belt region. Current estimates have Neptune's eccentricity as high as ~ 0.3 corresponding to an aphelion of \sim 39 AU at the end of migration (Levison et al. 2008). The sculpting of the Sedna population due to Neptune's migration outward has not been accounted for in the Brasser et al. (2006) simulation results. The cluster models do create orbits with perihelia in the range of 30-50 AU, which may not exist in the

Table 2
Orbital Information for Objects Detected in the Survey

Designation	а	е	i	R	Oppositions	Night 1	Night 2	Н	MMR
	(AU)		(deg)	(AU)		Avg Mag	Avg Mag		
(26181) 1996 GO21	93.01	0.588	13.4	40.87	11	21.0	20.6	5.2	11:2
(26308) 1998 SM165	47.99	0.375	13.5	36.99	12	21.4	21.4	5.8	2:1 Kozai
(19521) 1998 WH24	45.74	0.103	12.0	41.84	11	21.9	21.9	4.8	
(40314) 1999 KR16	48.83	0.306	24.8	36.27	6	20.6	20.7	5.8	
(38628) 2000 EB173	39.44	0.277	15.5	28.93	7	19.3	19.4	4.7	3:2 Kozai
(47932) 2000 GN171	39.36	0.281	10.8	28.34	9	20.3	20.4	6.0	3.2
(20000) 2000 WR 106	42.85	0.056	17.2	43 39	13	19.9	19.7	3.6	0.2
(82075) 2000 YW134	57.61	0.287	19.8	43.81	6	21.0	21.1	4.9	8.3
(83982) 2002 GO9	19.45	0.277	12.8	15.00	6	21.0	21.1	91	0.0
(50000) 2002 LM60	43.47	0.039	8.0	43.27	16	19.3	19.4	2.5	
(55636) 2002 TX300	43 46	0.126	25.8	41 29	12	19.8	19.7	33	
(55638) 2002 VE95	39.37	0.290	16.3	28.24	10	20.1	20.0	53	3.2
(119979) 2002 WC19	47.80	0.250	9.2	42.95	7	20.1	20.0	5.0	2.1
(174567) 2002 WC19 (174567) 2003 MW12	47.80	0.144	21.5	47.95	12	20.6	20.5	3.6	2.1
(120178) 2003 OP32	43.67	0.108	21.5	41.36	6	10.0	10.0	1 1	
(120178) 2003 UR292	32 49	0.100	27.1	26.87	6	21.4	21.5	7.0	
2003 UZ117	14 29	0.133	2.7	39.46	6	22.0	21.5	53	
(00377) 2003 VB12	510.00	0.155	11.0	88.31	8	22.0	21.7	1.6	
(30377) 2003 VB12 (136204) 2003 WI 7	20.17	0.850	11.9	15 21	6	20.6	21.0	8.7	
(130204) 2003 WL7 (175113) 2004 DE115	20.17	0.239	11.2	13.21	6	20.0	20.0	47	
2004 PC115	02.08	0.002	16.3	36.65	5	20.5	20.3	5.0	
(120247) 2004 SP60	42.08	0.005	22.0	42.80	10	20.8	20.9	4.2	
(120347) 2004 SB00	42.27	0.105	23.9	43.89	10	20.4	20.3	4.2	
2003 CD/9 (145451) 2005 DM42	45.15	0.140	20.7	40.10	0	20.4	20.5	5.0	
(145451) 2005 RNI45 (145452) 2005 RNI42	91.37	0.010	20.0	40.72	12	19.9	19.9	4.4	
(145452) 2005 KN45 (145480) 2005 TD100	41.77	0.028	19.2 26.4	40.72	13	20.0	20.0	5.9	
(145460) 2005 1D190	70.38	0.397	20.4	40.43	1	20.9	20.8	4.7	
2000 3A308	22.20	0.405	50.5 15 1	12.44	4	20.5	20.5	9.5	2.2
2007 JF45	39.41 44.60	0.165	10.6	29.43	4	20.9	20.8	5.2	5.2
2007 JF45	44.09	0.147	10.0	36.12	10 2	21.5	21.4	0.0	
2007 JJ45 2007 JV42	48.22	0.100	12.0	41.90	3	20.8	20.7	4.9	
2007 JK45	40.55	0.492	44.9	25.95	3	20.8	21.1	7.0 0.6	
2007 NC7	50.00	0.507	0.5	20.37	3	21.4	21.0	8.0 5.7	
2007 OC 10 (225088) 2007 OB 10	50.09	0.292	21.7	55.40 95.27	5	20.8	20.8	5.7	
(223088) 2007 OK10	42 75	0.300	18.0	83.37 20.80	/	21.5	21.4	1.9	
2007 PS45	45.75	0.090	10.9	39.80 19.70	10 2	21.5	21.1	5.0	
2007 RG283	19.98	0.233	28.8	18.70	3	21.5	21.0	8.8	
2007 RH285	15.90	0.339	21.4	17.48	8	21.4	21.2	8.4	2.2
2007 KI15	39.61	0.234	12.9	30.90	3	21.0	21.5	0.9	3:2
2007 KW 10 (2207(2) 2007 LIV 12(30.40	0.303	36.0	26.24	/	21.3	21.1	0.5	
(229/62) 2007 UK126	/3.52	0.488	23.4	45.96	9	20.4	20.3	3.4	
2007 XV50	46.02	0.073	22.9	46.19	3	21.2	21.3	5.0	
2008 AP129	41.66	0.138	27.4	37.39	5	20.6	20.7	5.3	5.0
2008 CS190	42.08	0.153	16.0	36.17	2	21.6	21.6	6.4	5:3
2008 CT 190	52.47	0.339	38.9	34.77	2	21.0	21.4	5.5	7:3
2008 LP17	88.04	0.660	14.1	30.26	2	21.0	20.9	6.6	
2008 NW4	45.58	0.203	23.1	36.92	2	21.2	21.0	6.0	
2008 OG19	67.37	0.428	13.1	38.74	2	21.6	21.3	4.9	
2008 QB43	43.36	0.219	26.3	38.79	3	21.6	21.4	5.6	
2008 QY40	63.09	0.418	25.1	38.11	2	20.9	20.9	5.3	
2008 SO266	39.64	0.247	18.8	31.58	2	21.5	21.4	6.9	3:2
2008 SP266	41.21	0.124	19.5	36.18	2	21.2	21.2	5.7	
2008 ST291	106.00	0.607	20.7	56.68	2	21.8	21.3	4.4	

Notes. Orbital elements reported by the Minor Planet Center of Centaurs and KBOs detected in the Palomar survey: semimajor axis (a), eccentricity (e), inclination (i), barycentric distance (R), oppositions observed (in years except where days noted by d), nightly discovery magnitudes, absolute magnitude (H), and mean motion resonance (MMR) if applicable. All 2007 and 2008 classified objects were new discoveries found by this work

current solar system due to Neptune ejecting these Sednas or scattering them onto KBO-like orbits during its eccentric phase. We chose a conservative minimum perihelia threshold of 50 AU (which would require Neptune to have an eccentricity of ~ 0.7 to reach 50 AU at aphelion) to compare the cluster distributions to our survey results.

5.2. Survey Simulator

We developed a survey simulator to compare the expected number of detections from the theoretical cluster Sedna populations to our survey results. The simulator draws synthetic objects from a model orbital and absolute magnitude distribution and for



Figure 8. Plot of perihelion (q) vs. semimajor axis (a) and plot of inclination (i) vs. perihelion (q) for Sedna-like bodies produced at the end of the Brasser et al. (2006) embedded cluster simulations used in this work. We limit the population to orbits q > 50 and a < 3000 AU. The diamond (red in the online version) denotes Sedna's orbit.

(A color version of this figure is available in the online journal.)

every image computes the positions and brightnesses of these objects on the sky. For all three cluster environments, we model a population of 3,000,000 bodies on cluster-created orbits randomly drawing the semimajor axis, eccentricity, and inclination for each particle from those produced in the cluster numerical integrations. Brasser et al. (2006) obtain a value of \sim 2 Gyr for the precession frequency of Sedna and other Sedna-like objects, therefore we assume that the orbits have been randomized due to planetary effects, and randomize over all other orbital angles. The positions of the artificial objects are computed for the survey period; those synthetic cluster objects that land on our images are identified neglecting the effects of masked regions of the CCDs. For each of the three cluster environments, approximately a third of the synthetic cluster-created orbits are located on our images.

A brightness distribution is then applied to the synthetic population. Due to the large uncertainties in the albedo distribution of such a distant population, we assign absolute magnitudes to our synthetic bodies instead of diameters. We assume a single power-law brightness distribution similar to the Kuiper Belt where the number of objects brighter than a given absolute magnitude, H_{max} , is described by

$$N(H \leqslant H_{\text{max}}) = N_{H \leqslant 1.6} 10^{\alpha(H_{\text{max}} - 1.6)}.$$
 (2)

The brightness distribution is scaled to $N_{H \leq 1.6}$, the number of bodies with an absolute magnitude brighter than or equal to Sedna (H = 1.6). A typical value of α measured for the asteroid belt is 0.3 (Jedicke & Metcalfe 1998). The best-fit single power laws for the hot (inclinations $> 5^{\circ}$) and cold (inclinations $<5^{\circ}$) Kuiper Belt populations are $\alpha = 0.35$ and $\alpha = 0.82$, respectively, measured by Fraser et al (2010), but it is unclear if the Sedna population should have an α value similar to the Kuiper Belt. The Sedna population may have very different surface characteristics than typical KBOs. Barucci et al. (2005) find methane and a tentative detection of nitrogen on Sedna's surface. Schaller & Brown (2007) model of volatile loss on KBO surfaces predicts that moderate-sized Sedna-like bodies on high perihelia orbits should retain methane and nitrogen ices on their surfaces. Most KBOs on the other hand, are either too small or too hot to hold on to their primordial abundance of volatiles. Distant Sednas never sublimate a significant amount of ices to renew their surfaces in a frost/thaw cycle. Instead the surfaces of the Sedna population would be subject to constant photoprocessing of methane by solar irradiation steadily darkening their surfaces. Sedna is one of the reddest KBOs with a $\langle V - R \rangle = 0.78$ with thermal measurements constraining Sedna's V albedo to be between 0.16 and 0.30 (Brown 2008; Stansberry et al. 2008). We choose to explore the extremes of the brightness distribution and model

the likely range of power-law distributions for α ranging from 0.2 to 0.8 including the best-fit value for the hot and cold KBOs measured by Fraser et al (2010).

For a given value of α and $N_{H \leq 1.6}$, absolute magnitudes are randomly assigned to our simulated Sednas. A single instance of the brightness distribution can be thought of as a separate survey. Those synthetic objects that lie within our sky coverage with an apparent magnitude above both nights' limiting magnitudes (as determined in Section 3.3.1) are deemed valid survey detections. We assume a 100% efficiency out to the limiting magnitude where then the efficiency immediately drops to zero. We require that the object must be located on all four field images to be considered "discovered" in the simulated survey, and we do not require the object have Sedna's perihelia of 76 AU. Bodies with $H \leq 4.3$ residing at 50 AU would be visible within our survey, and an object of Sedna's size and albedo would have been detected up to a distance of \sim 93 AU. Objects have multiple detection opportunities due to repeat sky coverage over subsequent years and overlapping fields. We do not count duplicate detections in our tallies.

5.3. Could Sedna Have Been Formed in a Cluster Environment?

We did not find any distant objects with perihelia greater than 45 AU with the exception of Sedna. To determine whether the orbital distributions produced in the various cluster environments are consistent with our redetection of Sedna, we must compare the orbital distributions of single detections produced by the survey simulator to Sedna. We employ our 3,000,000 synthetic Sedna population for each cluster environment to generate single detections. For each given value of α , absolute magnitudes are randomly assigned to our simulated Sednas for the range of possible values of $N_{H \leq 1.6}$ to create 10,000 single detections.

Each simulated detection is characterized by a semimajor axis, eccentricity, and inclination (a, e, i). We test a, e, i because these three parameters are directly affected by the impulses from the stellar encounters and gravitational effects from the embedded gas and stars, and these are the most independent set of orbital parameters. We choose to exclude the H distribution in our analysis because of the uncertainty of our limiting magnitudes. To determine whether Sedna and the clusterproduced single detections could be drawn from the same parent population for varying slopes and scaling of the brightness distribution, we employ a variant of a three-dimensional (3D) Kolmogorov–Smirnov (K-S) test adapted from Peacock (1983) and Press et al. (1992) which simultaneously compares the a, e, i orbital distributions to Sedna. The fraction of data points in each of the eight quadrants in a, e, i space, where the origin is defined by Sedna's orbital parameters (a = 519 AU, e = 0.853, i = 11.9 deg), is computed. In order to determine if Sedna's orbit is extreme compared to the cluster-produced detections, the D statistic in this case is defined as the difference of the maximum and minimum fraction calculated. The significance of the computed D statistic is found by performing our 3D K-S test again, selecting each of the 10,000 simulated single detections as the new origin, counting the fraction where the computed D statistic was higher than the D statistic for Sedna's orbit. We reject the cluster-produced population if the 3D K-S test does reject at a 95% or greater significance the null hypothesis, that the simulated survey single detections and our sole detection of Sedna are drawn from the same distribution.

We performed the 3D K-S test for all ranges of $N_{H \leq 1.6}$ that produced single detections and possible values for α (0.2–0.82)

 Table 3

 3D K-S Test Results for the Brasser et al. (2006) Cluster-produced Single Detections Compared to Sedna's Orbit

Cluster Central Density	α							
$(M_{\odot} \mathrm{pc}^{-3})$	0.2	0.35	0.4	0.6	0.82			
104	60	54	48	40	47			
10^{5}	99	98	99	98	97			
106	100	100	100	100	100			

Note. We report the confidence level at which we can reject the two distributions as drawn from the same parent population.

for all three cluster environments. The orbital distribution of single detections produced at smaller $N_{H \leq 1.6}$, is different from those at large $N_{H \leq 1.6}$, and the entire range of possible values $N_{H \leq 1.6}$ must be tested. At small values of $N_{H \leq 1.6}$ there are fewer bright H objects available to fill detectable orbits, biasing the single detections to slightly lower perihelia orbits than for larger values of $N_{H \leq 1.6}$ where there is an ample supply of bright bodies to fill detectable orbits. We find that the 3D K-S test confidence levels calculated for the 10⁶ and 10⁵ M_{\odot} pc⁻³cluster distribution for varying values of α are independent of $N_{H \leq 1.6}$. For the 10⁴ cluster and any value of α , $N_{H \leq 1.6} = 1$ has the highest probability of rejection and then decreases to a flat value as $N_{H \leq 1.6}$ increases. For the 10⁴ cluster, $N_{H \leq 1.6} = 1$ represents an upper limit on the rejection confidence level of the orbital distribution. Therefore, we report the confidence level calculated for each cluster distribution and brightness distribution for values of $N_{H \leq 1.6} = 1$ in Table 3. For the two densest cluster environments 10^6 and $10^5 M_{\odot} \text{ pc}^{-3}$ producing Sedna as the sole detection is an extremely low probability event. The bulk of the 10⁶ and 10⁵ M_{\odot} pc⁻³ cluster-created single detections had orbits with semimajor axes less than Sedna's. The simulations produce many more objects with lower perihelia than Sedna that should have been found but were not detected in our survey. We can rule out 10^6 and the $10^5 M_{\odot} \text{ pc}^{-3}$ cluster population at confidence levels greater than 95% for all ranges of α and possible values of $N_{H \leq 1.6}$. Therefore, we reject the 10⁶ and $10^5 M_{\odot} \text{ pc}^{-3}$ clusters as the source of the Sedna population. We cannot reject the $10^4 M_{\odot} \text{ pc}^{-3}$ cluster environments to a confidence level greater than 60% for all combinations of α and $N_{H \leq 1.6}$ tested; we are unable to rule this population out with statistical significance. The $10^4 M_{\odot} \text{ pc}^{-3}$ orbital distribution is consistent with our redetection of Sedna. These results assumed that every object that lands on a CCD brighter than the image limiting magnitude would be detected. Our detection efficiency is not 100%, but including a flat detection efficiency curve that drops to zero at the image limiting magnitude does not change the results presented. Including a detection efficiency produces the same types of orbits for single detections, just the absolute number of single detections decreases. Since we are only looking at single detections, the 3D K-S test results are the same for any efficiency value.

If Sedna's orbit is the result of multiple stellar encounters when the nascent Sun resided in an embedded cluster, our work rules out central densities for the cluster greater than or equal to $10^5 M_{\odot}$ pc⁻³ for the environment of the early solar system, and Brasser et al. (2006) require central densities higher than $10^3 M_{\odot}$ pc⁻³ to reproduce Sedna's orbit. In terms of the mean density of the material the Sun would have interacted with in the cluster environment, the Sun would have had to have encountered a mean density greater than 10³ and less than ~10⁴ M_{\odot} pc⁻³ to be consistent with our survey observations. Gutermuth et al. (2005) map the volume density of three young embedded cluster regions (GGD 12–15, IRAS 20050+2720, NGC 7129). The peak densities of these regions were on the order of ~10⁵ M_{\odot} pc⁻³. For GGD 12–15 and IRAS 20050+2720, 72% and 91% of the member stars reside in locations with densities upward of 10⁴ M_{\odot} pc⁻³, and are unlikely to produce the observed Sedna population. For NGC 7129, less than 24% of the stars in the core of the cluster experience densities greater than 10⁴ M_{\odot} pc⁻³. Lada & Lada (1995) estimate the central stellar density of the 0.1 pc central regions of IC 348, NGC 2024, and Trapezium clusters to range from ~10³ to 10⁴ M_{\odot} pc⁻³ at the minimum central density required to form Sedna's orbit. These environments and NGC 7129 could produce the observed Sedna population.

5.4. Population Estimate

Now that we have found the $10^4 M_{\odot} \text{ pc}^{-3}$ cluster population is the only cluster environment capable of emplacing Sedna on its orbit, we can place constraints on the size of the produced population. To estimate the size of the Sedna population, we use the value of α measured by Fraser et al (2010) for the hot and cold populations of the Kuiper Belt ($\alpha = 0.35$ and 0.82, respectively) as limits for our brightness distribution. For each given value of α , absolute magnitudes are randomly assigned to our survey simulator created 3,000,000 Sednas 50,000 times, for every value of $N_{H \leq 1.6}$. A single instance of the brightness distribution can be thought of as a separate survey. For each $N_{H \le 1.6}$ tested, the number of synthetic "surveys" in which, like the real survey, one object on a Sedna-like body is detected is tallied. Valid detections are only those in which the object is located on the same CCD and in all four field observations. We do not require that the object have Sedna's absolute magnitude (H = 1.6), only that the apparent magnitude of the object is above the SExtractor calculated limiting magnitudes of all four frames the object is "discovered" on.

The best-fit values for the number of objects brighter than or equal to Sedna with 95% errors are 393^{+1286}_{-264} and 74^{+279}_{-47} for the hot and cold brightness distributions, respectively. The lower and upper 95% confidence levels' limits reported are onesided statistics found by computing the interval over which the integrated probability distribution 0.95, respectively, of the total area. The survey simulator assumes all simulated Sednas that land on our images and are above the image limiting magnitude would be detected in the survey. The effect of a less than 100% survey detection efficiency is non-negligible. The reported size estimates represent a lower bound on the size of the Sedna population. Assuming a uniform detection efficiency which drops to zero at the image limiting magnitude, the best-fit value and 95% limits for $N_{H \leq 1.6}$ are scaled by the inverse of the survey efficiency. For our nominal detection efficiency of 0.66, the best-fit values for the number of objects brighter than or equal to Sedna are 595^{+1949}_{-400} and 112^{+423}_{-71} , respectively, for the hot and cold brightness distributions. Figure 9 plots the fraction of simulated surveys that produced a single Sedna detection as a function of $N_{H\leqslant 1.6}$ the 10⁴ M_{\odot} pc⁻³ cluster environment for our nominal survey detection efficiency.

For the $10^4 M_{\odot} \text{ pc}^{-3}$ cluster environment, the range is quite large but there could be on the order of hundreds to thousands of planetoids brighter than Sedna present beyond the Kuiper Belt. For comparison, the total number of Sedna-sized or larger bodies in the Kuiper Belt is ~5–8 (Brown 2008); there may be an order of magnitude or two more mass residing in the Sedna region than exists in the present Kuiper Belt. The expected number of objects with $H \leq 1.6$ varies significantly with the slope of the brightness distribution. Choosing a steeper power law for the brightness distribution decreases the likelihood of detecting only one Sedna because of the larger number of bright objects populating detectable orbits and decreases the best-fit number of objects brighter than Sedna. Selecting a smaller value of α , a shallower brightness distribution, increases the likelihood of detecting only one object on Sedna's orbit by decreasing the number of synthetic surveys with multiple detections.

We excluded orbits with semimajor axes greater than 3000 AU from our analysis. If we had included higher semimajor axis orbits, the best-fit number of Sedna-like bodies brighter than or equal to Sedna would increase due to the larger population of orbits being included, but our overall conclusions would not change. Those orbits that are contributing most to being Sedna detections are those with semimajor axes much smaller than 3000 AU. The $10^4 M_{\odot} \text{ pc}^{-3}$ cluster results are the most sensitive to this cut. We examined the single detections produced in the best-fit simulations for the range of α parameters. Orbits with semimajor axes less than 1000 AU contribute $\sim 80\%$ –90% of the Sedna single Sedna detections. The number is even greater from the 10^6 and $10^5 M_{\odot}$ pc⁻³ clusters. We make a conservative perihelia cut at 50 AU to compare the clusterproduced Sedna-like orbits to our observed Sedna population. Our simulations were rerun, including orbits with perihelia greater than 45 AU and our conclusions remain the same. The 10⁶ and 10⁵ M_{\odot} pc⁻³ cluster will be ruled out with a higher confidence level because of the increase in low perihelia orbits that should have been detected in our survey. For this analysis, we used the SExtractor computed limiting magnitudes to determine whether our simulated Sedna population was observable on our images.

5.5. Comparison to Occultation Surveys

Wang et al. (2009) place upper limits on the number of small bodies in the Sedna region due to the lack of occultations from distant solar system bodies in the TAOS survey. We can estimate whether our upper limits for the Sedna population are consistent with Wang et al.'s reported upper limits on the number density of objects larger than 1 km. We find the fraction of our $10^4 M_{\odot} \text{ pc}^{-3}$ cluster survey simulator created 3,000,000 Sednas that are within 3° of the ecliptic (TAOS's ecliptic latitude range) and at 100 and 1000 AU. Assuming no break in the size distribution, we extrapolate the number of bodies larger than 1 km. The albedo distribution is uncertain, Sedna's V albedo is measured to be between 0.16 and 0.30 (Brown 2008; Stansberry et al. 2008), but to give an extreme upper limit we chose an albedo for 0.04 and assume no break in the size distribution in order to estimate the fraction of bodies that would be observable by TAOS. TAOS is sensitive to bodies brighter than H = 19.1.

Within 3° of the ecliptic, 0.05% of the $10^4 M_{\odot}$ pc⁻³ cluster-produced Sedna population are located between 50 and 150 AU and 0.07% reside at 900–1100 AU. For the flat size distribution value ($\alpha = .35$), we expect there to be no more than 780 Sednas deg⁻² on the ecliptic at 100 AU and 10^4 Sednas deg⁻² at 1000 AU assuming a 66% detection efficiency. Our 95% confidence level estimates for a flat size distribution are well below TAOS's ecliptic number density of 1 km or larger bodies at 100 (~10⁷ Sednas deg⁻²) and 1000 AU (~10⁹ Sednas deg⁻²) even without a break in the size distribution. The TAOS observations do not rule out a large Sedna population with thousands of Sedna-sized or larger bodies



Figure 9. Results of the $10^4 M_{\odot}$ pc⁻³ cluster analysis for the $\alpha = 0.35$ (hot) and $\alpha = 0.82$ (cold) Kuiper Belt population size distributions. Fraction of synthetic surveys with one detectable Sedna-like body as a function of the number of bodies bigger and brighter than Sedna assuming our nominal 66% detection efficiency.

residing far from the Sun for a flat brightness distribution. For the steep (cold population) size distribution, $\alpha = .82$, and a 66% magnitude detection efficiency, at 100 AU we expect no more than 2.8 × 10¹⁰ objects deg⁻², approximately 2 orders of magnitude larger than TAOS's 3σ upper limit. We find that even our 95% lower limit at 100 AU is an order of magnitude larger than the TAOS limit. Our expected number density at 1000 AU at our 95% upper confidence level, on the other hand, is $3.70 \times$ 10¹¹ objects deg⁻² below TAOS's limit of ~10¹² objects deg⁻².

The occultation results do not necessarily rule out a steep size distribution for the Sedna population. In the Kuiper Belt at small sizes (\sim 50–150 km), the distribution is observed to break to a shallower slope (Bernstein et al. 2004; Fuentes et al. 2009; Fraser & Kavelaars 2009). Brasser et al.'s model did not include gas in the solar nebula and therefore did not include the effects of gas dynamics in their simulations. Sedna is \sim 1500 km in size and would not be effected by gas drag, but smaller sized objects would be. Brasser et al. (2007) investigated the effect of gas drag on the size distribution of objects deposited into the Sedna region. They find a size-sorting effect in the clusterproduced Sedna population. Bodies smaller than \sim 20–60 km would be circularized onto orbits beyond Jupiter and Saturn and not available to be scattered into the Sedna region. Far fewer small-sized objects would be deposited into the Sedna region. Our survey is sensitive to objects much larger than those that would be effected by gas drag or the break in the brightness distribution. The combination of a broken power-law size distribution and a size-sorting effect could reconcile the observations, causing very few small objects that TAOS would have been able to detect to be present in the Sedna region.

5.6. Open Cluster Environments

The majority of stars are birthed in embedded clusters, but 4%-7% of stars form in smaller loose conglomerations with little or no gas known as open clusters (Lada 2004). Open clusters, like the Pleiades, have ages of a few tens to hundreds of Myr (Lada 2004). Although embedded clusters are more prevalent, it is postulated that $\sim 5\%$ of the embedded clusters



Figure 10. Folded latitudinal distribution of objects with semimajor axis > 30 AU found in this work. The lower dashed line with diamonds shows the number of actual KBO detections in 2° bins. The dashed line shows the fractional ecliptic latitude completeness. The solid line shows the expected number of KBOs brighter than 21.3 corrected for sky coverage with 1σ Poisson error bars computed for the unfolded distribution added in quadrature.

may dissipate into loosely bound open clusters (Lada & Lada 2003). Kaib & Quinn (2008) are able to produce objects on Sedna-like orbits in various open cluster environments. Interactions between the planetesimals disks of the cluster members are not included in their simulations. Their numerical integrations produce similar wedge-like orbital distributions to the Brasser et al. (2006) embedded clusters models, but Kaib & Quinn (2008) find no relationship between the size of the birth cluster and the orbital distribution of Sednas. The open cluster integrations are nondeterministic with Sedna's orbit being produced in only 5 of their 16 cluster simulations of varying cluster size. For those integrations that do produce Sedna and other Sedna-like orbits, distributions similar to the 10^4 and $10^6 M_{\odot}$ pc⁻³ (Brasser et al. 2006) results are generated. This is not unsurprising since the dominant dynamics sculpting the Sedna region, stellar encounters, is the same in both environments. Our analysis above of the embedded cluster distributions also applies to Kaib & Quinn (2008) open cluster orbital distributions. Those distributions where Sedna is at the end of a distribution Sedna-like orbits with many lower semimajor axes and lower perihelia orbits similar to the 10^5 and $10^6 M_{\odot} \text{ pc}^{-3}$ embedded clusters are inconsistent with our observations.

5.7. Implications for the Kuiper Belt

Using the discovery of 2008 KV42, with an orbit essentially perpendicular to the ecliptic, Gladman et al. (2009) posit a metastable parent population with inclinations greater than ~ 50 AU with *a* in the hundreds of AU and q = 3545 AU. Such a population is produced in the 10^5 and $10^6 M_{\odot}$ pc⁻³ cluster environments but not present in the $10^4 M_{\odot}$ pc⁻³ embedded cluster (Brasser et al. 2006). Gladman et al. (2009) suggest 2008 KV42 may have been a high inclination counterpart to Sedna placed on a lower perihelia and semimajor axis that later diffused to its current orbit. Although for our analysis we removed such objects with perihelia less than 50 AU from our distribution, adding those objects would only rule out the 10^5 and

 $10^6 M_{\odot} \text{ pc}^{-3}$ cluster environments to even higher confidence because many more low *a* and low *q* objects single detections would be produced than detections with similar orbits to Sedna. With this region devoid of particles in the $10^4 M_{\odot} \text{ pc}^{-3}$ cluster integrations, this suggests that 2008 KV42 and Sedna are likely formed from two independent source populations.

6. LATITUDE DISTRIBUTION

Figure 10 plots the folded latitude distribution of all objects with a > 30 debiased for latitudinal coverage. We assume Poisson detection statistics (as computed by Kraft et al. 1991), with error bars representing the Poissonian 68% confidence limit on the detected number of objects in each latitude bin corrected for sky coverage. A noticeable spike occurs at $\sim 12^{\circ}$ from the ecliptic. Brown (2008) also finds these prominent peaks in the latitudinal distribution $\sim \pm 11^{\circ}$ ecliptic latitude. Brown finds that this peaked distribution cannot be generated by a simple inclination distribution of objects in random orbits. Brown (2008) suggests that resonant orbits are likely able to explain these high latitude concentrations. Resonators trapped in the Kozai resonance (such as Pluto) have their perihelia near their maximum excursion off the ecliptic (Morbidelli 1997) and the highest detection probability out of the ecliptic plane. The plutinos come to perihelia away from Neptune (Malhotra 1996, 1995) and are preferentially biased toward detection at certain longitudes. Without dynamical classification Brown (2008) could not verify the plutinos as the source of these peaked latitude distributions.

With secure orbits for our detections, we can address this issue. In order to classify which of the survey KBOs reside in mean motion resonances with Neptune, each KBO had 13 clones integrated for 10 Myr. One clone represents the best-fit orbit, and the rest are taken from a self-consistent spread of orbits covering the 3σ uncertainty of the KBOs best-fit orbital solution computed from the covariance matrix of orbital elements obtained from AstDys⁶ on 2009 December 1.

⁶ http://hamilton.dm.unipi.it/astdys/



Figure 11. Folded latitudinal distribution 2° bins of survey of multiopposition plutinos (top) and non-plutinos excluding confirmed Haumea family members (bottom) brighter than 21.3 corrected for sky coverage with 1σ Poisson error bars computed for the unfolded distribution added in quadrature. Filled circles show the number of actual KBO detections in 2° bins.

These objects were integrated using the *n*-body code SyMBA (Levison & Duncan 1994) using the integrator swift_rmvs3 based on the mapping by Wisdom & Holman (1991). The KBO clones were treated as massless particles. The four giant planets were included and their initial conditions were taken from JPL HORIZONS. The mass, position, and velocity of the terrestrial planets were combined with the Sun. The integration proceeded backward in time with 40 day time steps from epoch JD 2455200. After 10 Myr, the clones were examined for one or more librating resonant angles and as well as librating arguments of perihelion in order to identify Kozai resonators. We identified objects (listed in Table 2) as resonant if all the clones lie in the resonance at the end of the integrations.

The latitudinal distribution of detected plutinos found in the survey is plotted in Figure 11. Six plutinos were detected in our survey, only two reside at ecliptic latitudes less than 10° . The remaining four plutinos compose the majority of the 12° latitude spike. Of these four plutinos (Huya, 2007 RT15, 2002 VE95, and 2008 SO2006), two objects are Kozai resonators, Huya and 2007 RT15; the other three have perihelia off the ecliptic having possibly experienced temporary Kozai interactions. The remaining non-plutino distribution still exhibited a peak in the distribution at 12° including two members of the Haumea collisonal family. At least 7% of our detections are fragments of the Huamea collisional family (Brown et al. 2007; Ragozzine & Brown 2007; Schaller & Brown 2008; Snodgrass et al. 2010).



Figure 12. Cumulative number of expected KBOs within $\pm 30^{\circ}$ of the ecliptic assuming a flat latitude distribution (open diamonds) with 2σ Poisson error bars. Cumulative number of known multiopposition KBOs ($a \ge 30$) within $\pm 30^{\circ}$ ecliptic latitude (filled circles).

The identifier of the Haumea family is the characteristic deep near-infrared pure water ice absorption features on their surfaces (Brown et al. 2007; Schaller & Brown 2008). The water icerich bodies are thought to all have anomalously high albedos, like family member 2002 TX300 (Elliot et al. 2010), extremely biasing our survey toward detection of Haumea family members. Any clustering in the Haumea family members will severely bias our latitude distribution. Removing the spectroscopically confirmed family members from our survey, the non-plutino distribution is not peaked as shown in Figure 11.

Brown (2008) and this work are the only two wide-field surveys to probe significantly beyond the ecliptic. In order to test whether the plutino population observed by ecliptic surveys is representative of the entire plutino population, we compare our observed plutino latitude distribution to the CFEPS plutino model. The CFEPS survey (Kavelaars et al. 2009; Gladmanet al. 2010) orbital and brightness distribution is based on the sample of plutinos detected in observations covering ecliptic latitudes less than 2°. None of their detections are Kozai librators, thus only representing the non-Kozai plutino population. CFEPS is sensitive to an absolute magnitude range of $H_{g'} \sim 6-10.5$, fainter than the sources we are able to detect in our survey. In order to compare their model to our observed latitude distribution, we must extend the distribution to larger objects where the CFEPS survey does not measure directly and where the slope of their measured brightness distribution may not be applicable to the larger bodies that we detect. The H distribution is measured in g' and we observe in a broadband R filter. Fraser et al. (2008) find an average KBO value of $\langle g' - R \rangle = 0.95$, and we apply this as our constant offset to the g' magnitudes. We create a latitude distribution by shuffling the absolute distribution of the 10^5 model plutinos with $H_g > 10.5 \sim 10^5$ times. We tally the latitudes of all plutinos for all runs with magnitudes brighter than R = 22 that lie within our survey sky coverage in a folded latitude histogram binned in 2° latitude bins. To estimate the expected number of plutinos in the 12° bin, we scale CFEPS model latitude distribution to the value of our folded latitude distribution at 2°, the lowest latitude binned plutino detection in our survey. Assuming Poisson errors and using the quadrature

of the fractional errors, $6.7 \, {}^{+15.6}_{-6.3}$ (68% confidence level) times as many plutinos reside in 11° – 13° from the ecliptic than are predicted by the non-Kozai plutino CFEPS model. Although the range is quite high, our latitude distribution suggests that the plutino population, in particular the Kozai population, has been underestimated and may be much larger than previous KBO surveys have reported.

7. NUMBER OF BRIGHT OBJECTS

Our survey probes the bright end of the KBO size distribution. Assuming a uniform latitude distribution, we can crudely estimate the number of large observable KBOs. Using our nominal survey efficiency function from Section 3.3.2 and the effective area covered we compute the expected number of bright KBOs (a > 30) as a function of magnitude. We neglect the effects of masked CCD regions and other geometric effects. Our sky coverage drops significantly above latitudes of $\pm 30^{\circ}$ and therefore we only focus on detections and sky covered within $\pm 30^{\circ}$ of the ecliptic. Figure 12 plots the cumulative number of expected bright KBOs as a function of magnitude compared to known multiopposition KBOs.

8. CONCLUSIONS

Surveying $\sim 12,000 \text{ deg}^2$ within $\pm 30^\circ$ of the ecliptic to ~ 21.5 in *R* magnitude, we have searched for additional members of the Sedna population. Based on the 52 KBOs and Centaurs detected in our survey we conclude the following.

- We detected only one object on a Sedna-like orbit, Sedna, despite a sensitivity to motions of bodies out to ~1000 AU. With one detection, we cannot differentiate between the various proposed formation mechanisms proposed to emplace Sedna on its orbit.
- 2. For the embedded cluster Sedna formation model, we reject the 10^5 and $10^6 M_{\odot}$ pc⁻³ cluster environment-produced populations as consistent with our redetection of Sedna. We find the $10^4 M_{\odot}$ pc⁻³ cluster environment consistent with our observations, with a best-fit population of $N_{H \leq 1.6}$

3. The plutino population has a peaked distribution at $\sim \pm 12^{\circ}$ ecliptic latitude, likely due to Kozai resonators and current estimates of the size of the plutino population from onecliptic surveys insensitive to these high latitude plutinos likely underestimate the size of the true population

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