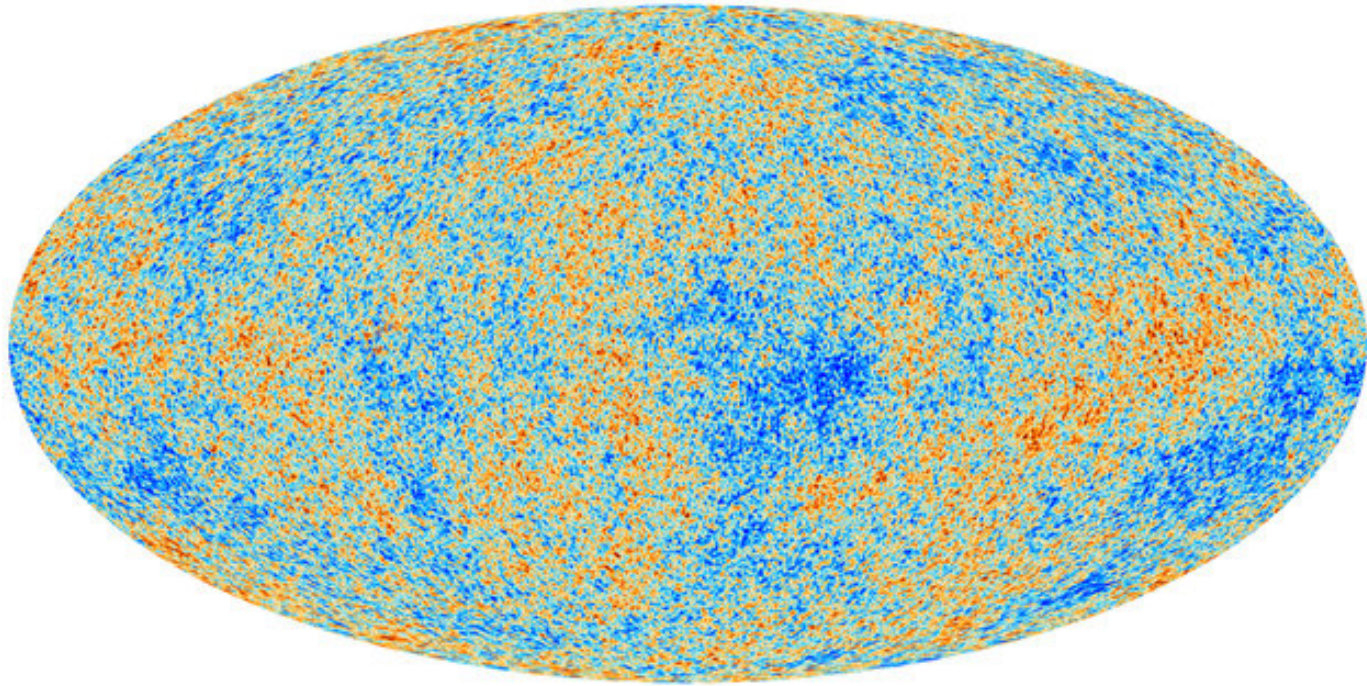


Astronomy 120



Little Bumps in the CMB & Curvature of Space

Class 23

(next to last...)

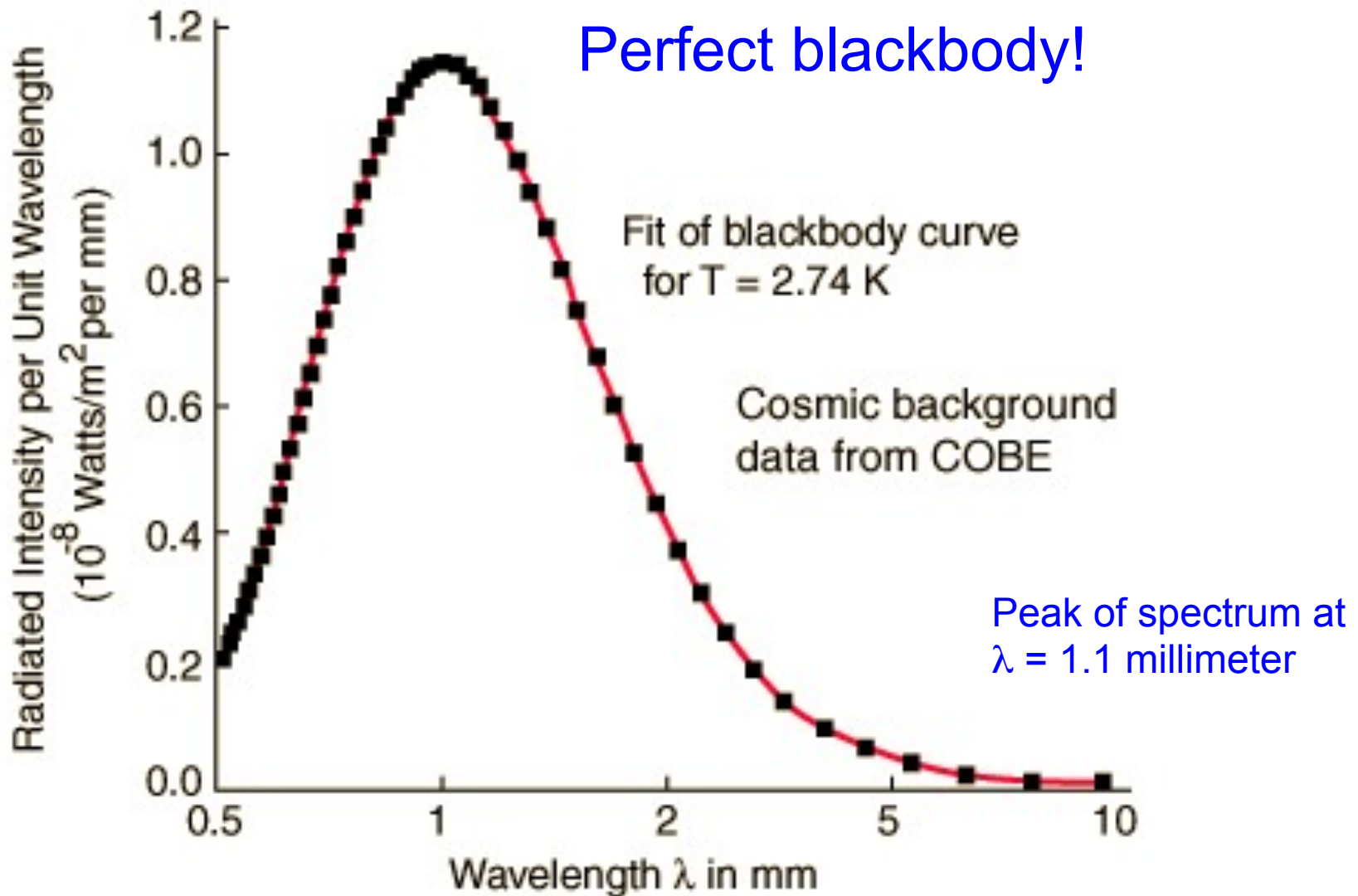
Prof J. Kenney

June 28, 2018

Homeworks

- all HWs must be handed in by tomorrow
Thursday June 28!
- so I can post solutions to help you prepare
for Final Exam on Friday

Spectrum of cosmic microwave background



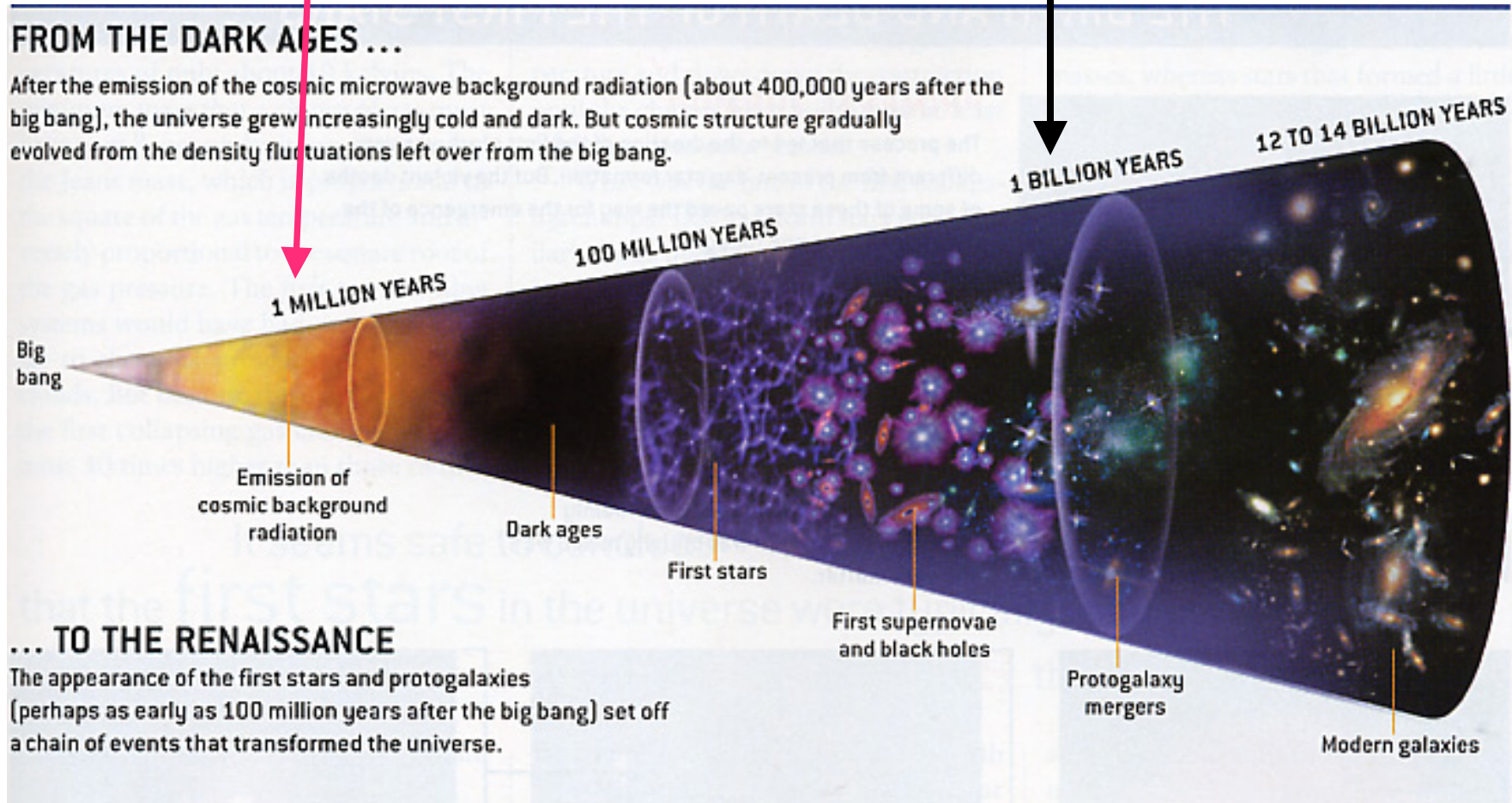
ISOTROPY OF THE COSMIC MICROWAVE BACKGROUND



Intensity of CMB radiation over whole sky:
Nearly the same in every direction!

Emission of cosmic background radiation (380,000 yrs ABB)

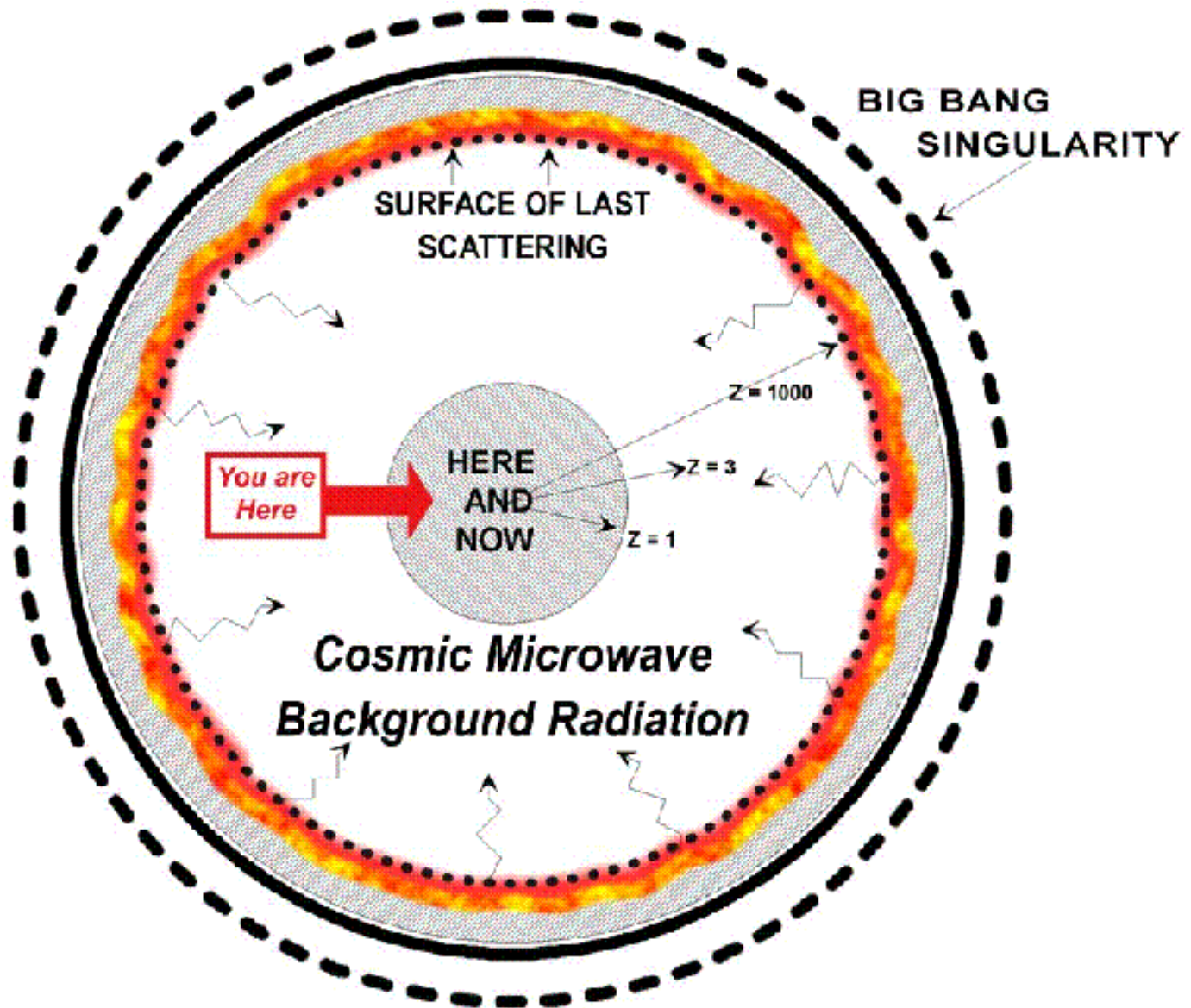
Era of Peak star, galaxy & black hole formation (~ 1-4 Byrs ABB)



BIG BANG

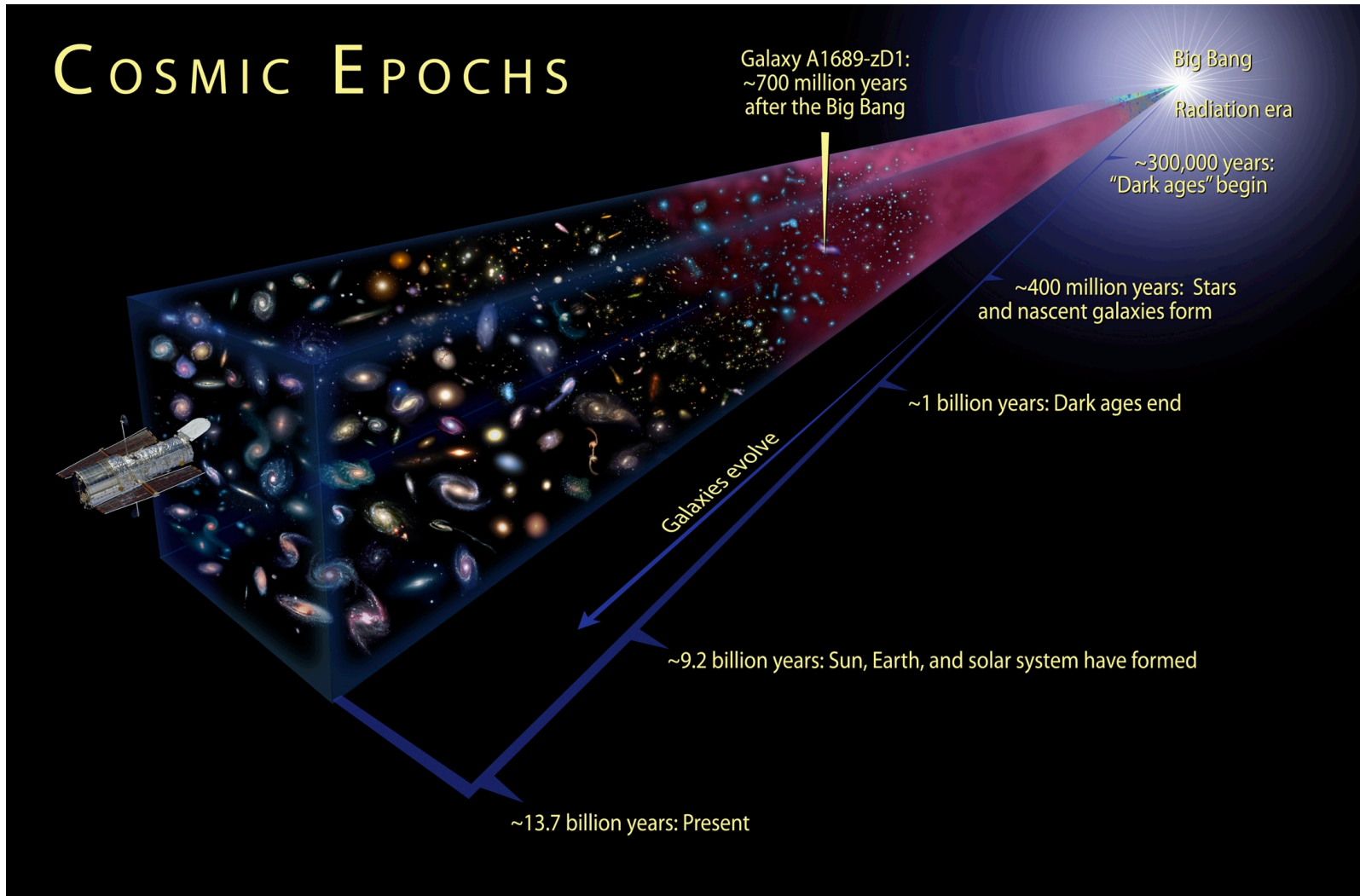
Cosmic Time

NOW



Things we learn from CMB

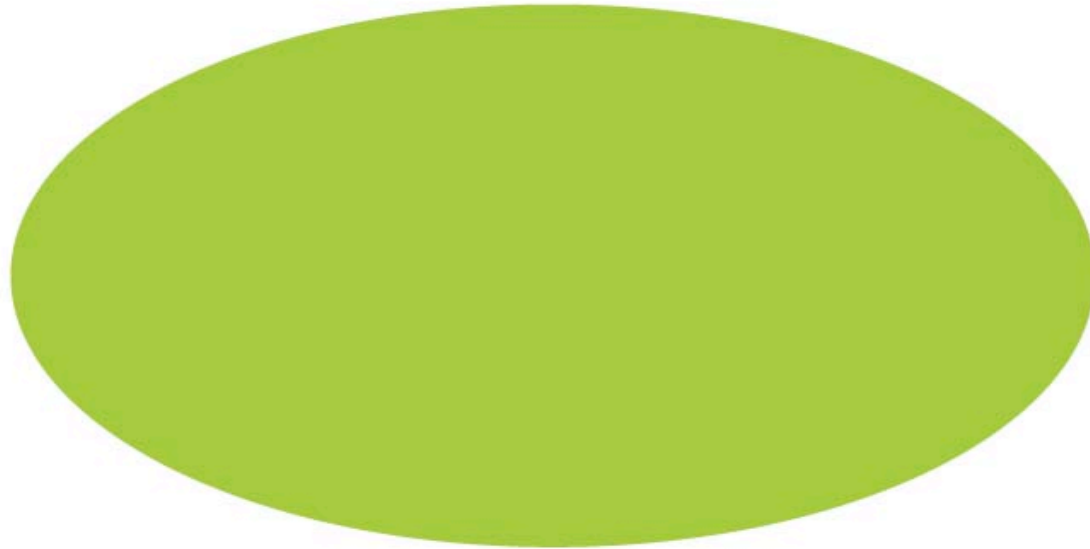
Universe was once much hotter and denser than now (evidence for BIG BANG)



Things we learn from CMB

We are not in special location in universe

**ISOTROPY OF THE COSMIC
MICROWAVE BACKGROUND**



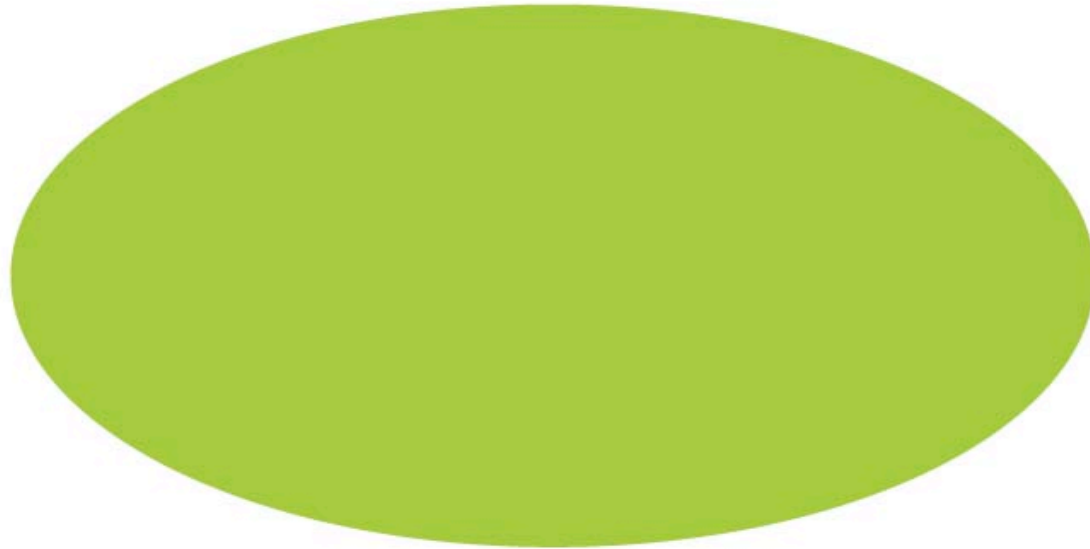
Where is the center???

NO CENTER of expansion at any one location in space -->
Big Bang occurred in all of space at the same time with
same intensity (what Einstein says in GR)

Things we learn from CMB

Universe was once much more uniform than now

ISOTROPY OF THE COSMIC MICROWAVE BACKGROUND

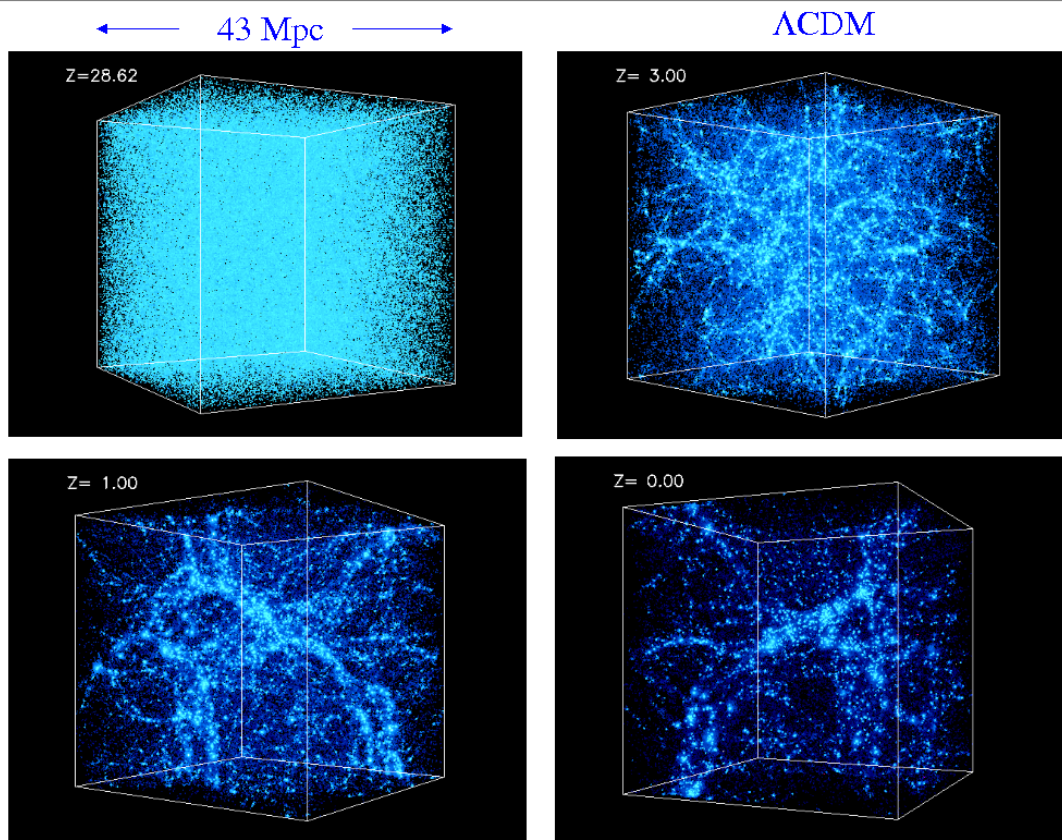


(almost) no substructure in universe at early times

Things we learn from CMB

Universe was once much more uniform than now.

So when did stars, planets, galaxies, clusters, black holes ("structure") begin to form?



Growth of structure (stars, galaxies, clusters...) in universe began in earnest only after decoupling (when CMB photons were made)

Things we learn from CMB

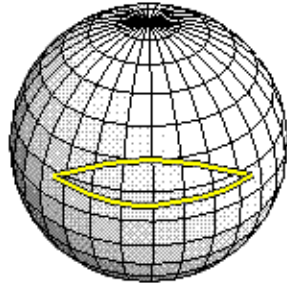
Evidence for dark energy & inflation



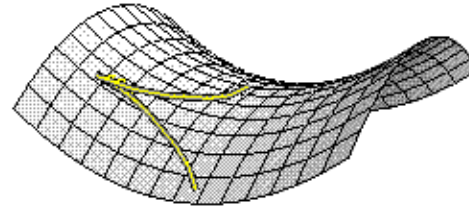
Things we learn from CMB

How space of universe is curved

Positive
(spherical)

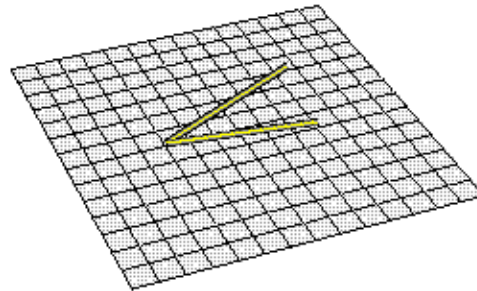


A *closed* universe curves “back on itself”. Lines that were diverging apart come back together. Density > critical density.



An *open* universe curves “away from itself”. Diverging lines curve at increasing angles away from each other. Density < critical density.

Negative
(saddle)



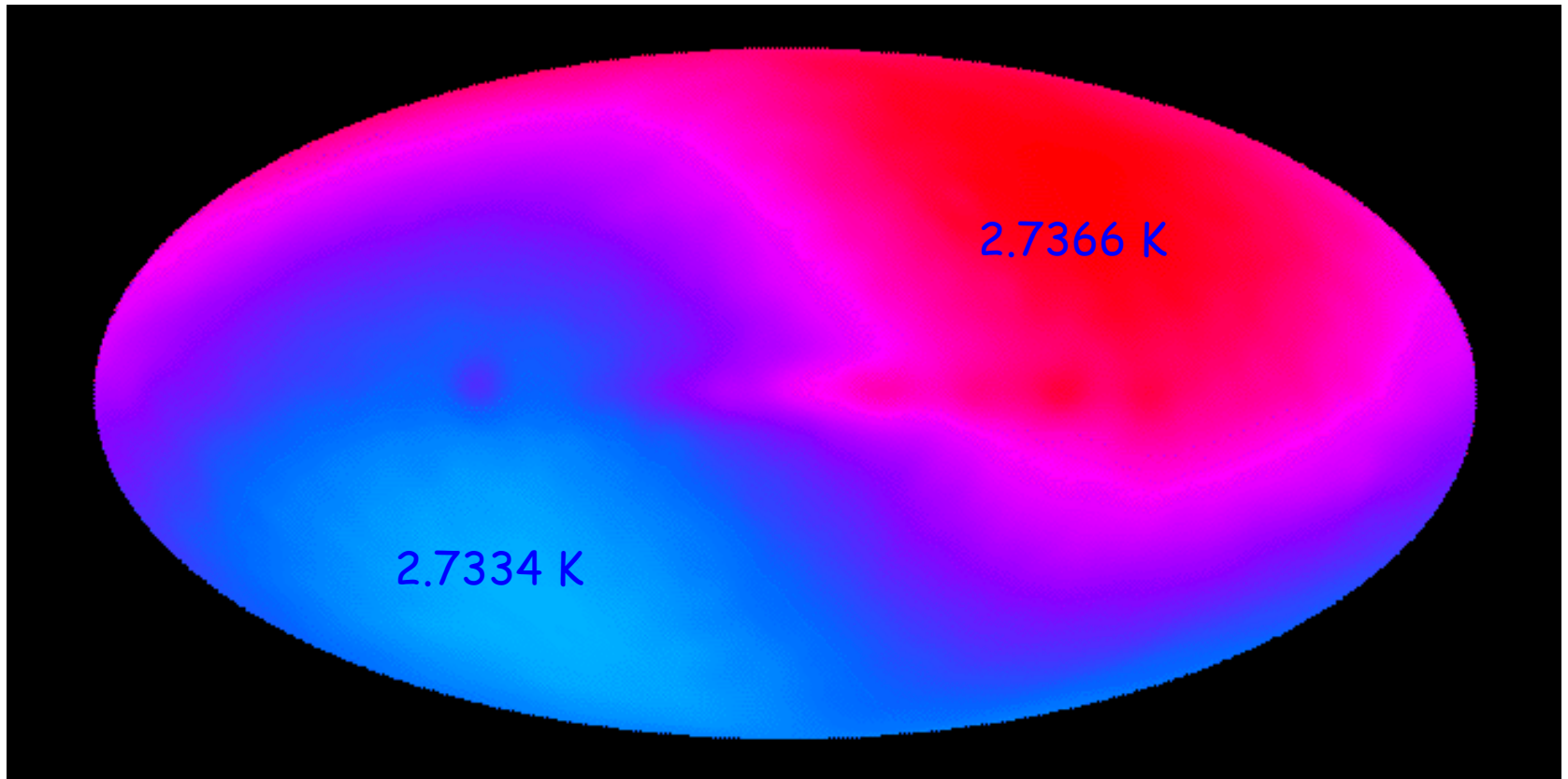
A *flat* universe has no curvature. Diverging lines remain at a constant angle with respect to each other. Density = critical density.

Zero curvature
(flat)

Types of possible curvatures for universe in General Relativity

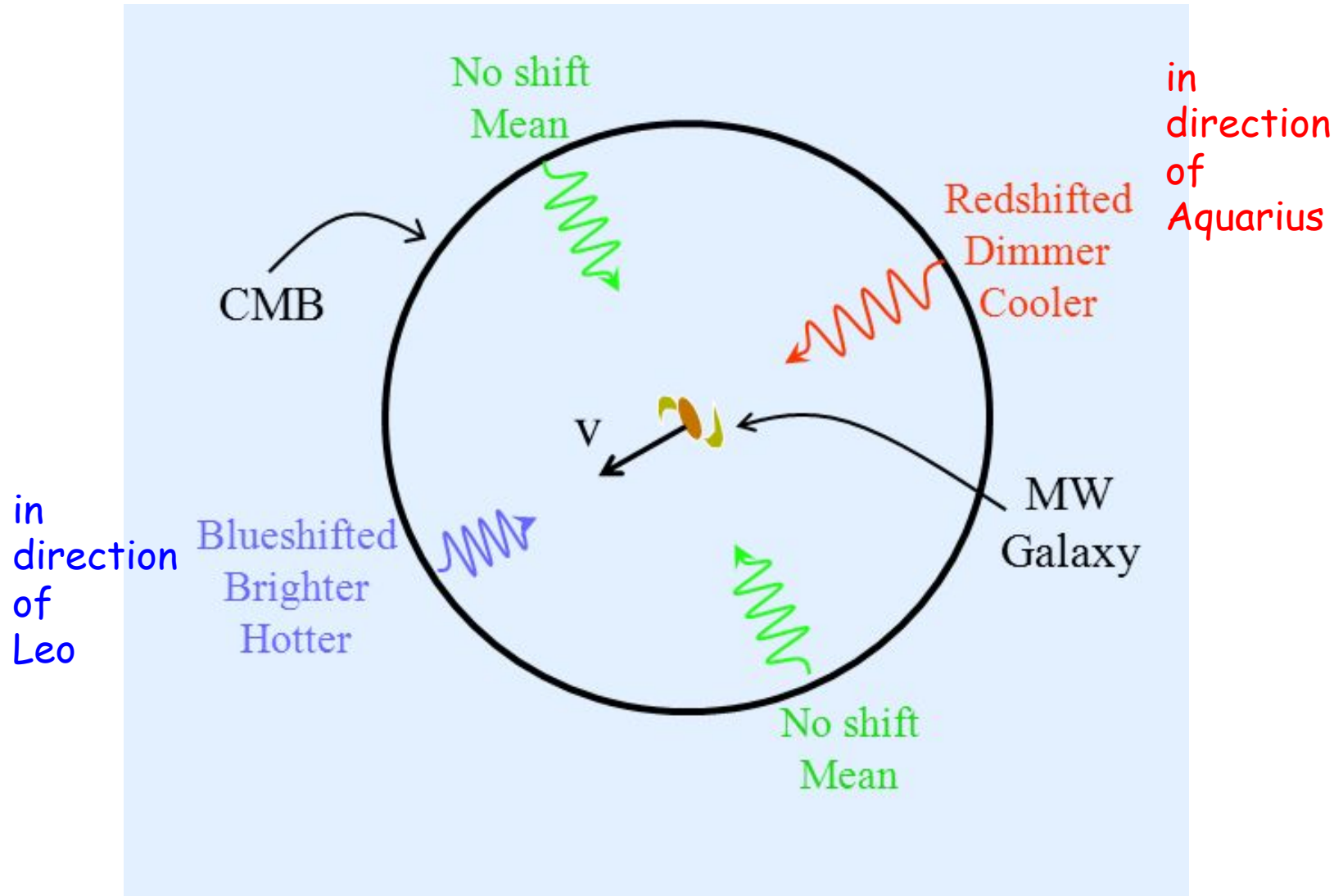
Things we learn from CMB

- Universe was once much hotter and denser than now (evidence for BIG BANG)
- Universe was once much more uniform than now
- When structure (stars, galaxies, clusters...) in universe began to form
- Evidence for dark energy
- Evidence for inflation
- We are not in special location in universe (BIG BANG occurred in all of space at same time)
- How space of universe is curved



99.9% of average signal removed
...a “Dipole” pattern remains!!
(all of sky shown)

Doppler shift origin of the dipole pattern in the CMB



Dipole Anisotropy in CMB

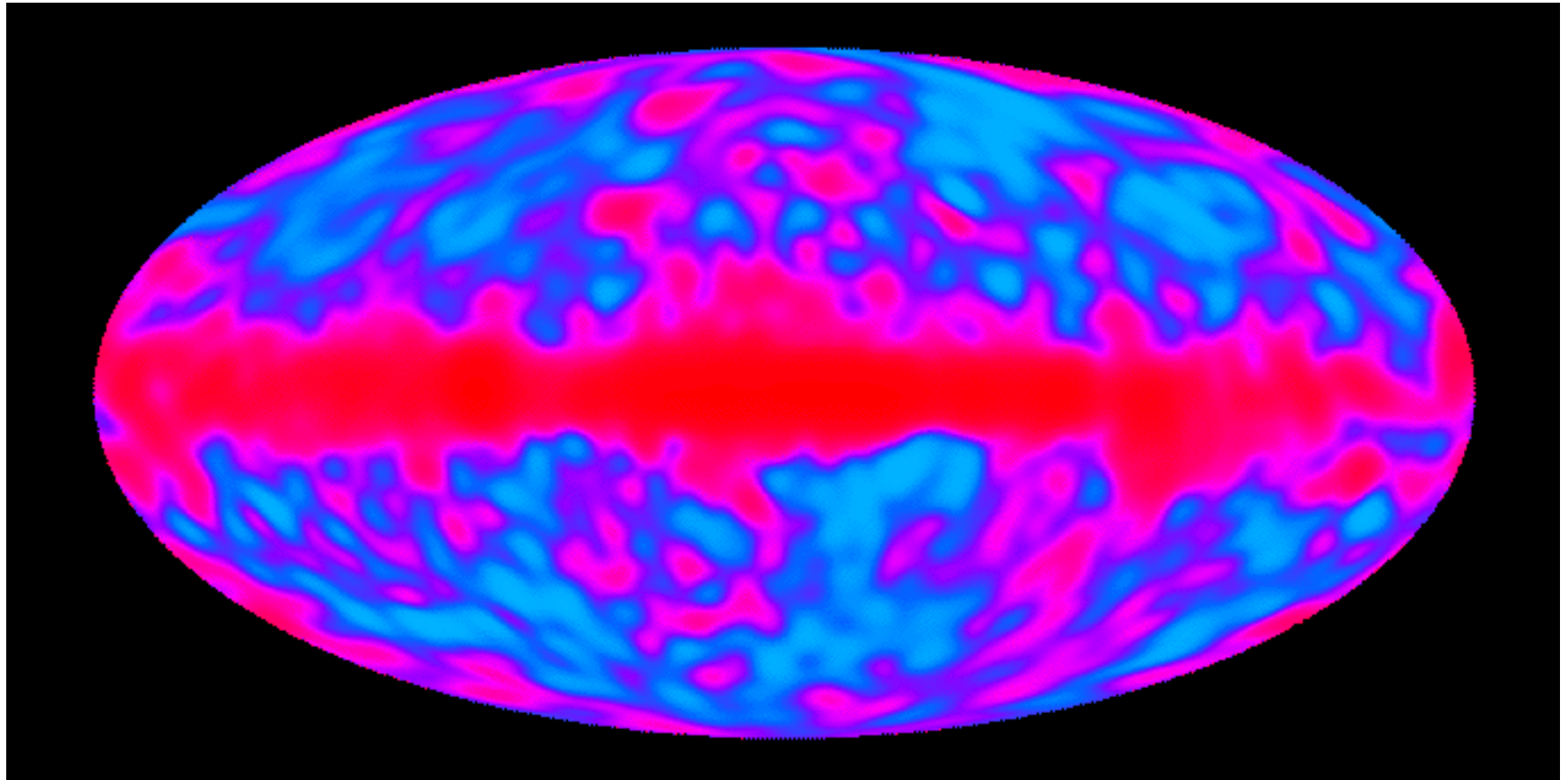
arises from earth's motion caused by gravitational pull of different objects

- Earth around sun 30 km/s
- Sun around center of MW 220 km/s
- MW toward Virgo cluster 350 km/s
- MW+VC toward Great Attractor 620 km/s

Pulls are in different directions so net motion is 370 km/s toward Leo (in between Virgo & Great Attractor)

Dipole Anisotropy in CMB

- Perfect “dipole” pattern (sinusoidal variation) across sky tells us this is due to our motion w.r.t. CMB
- Caused by our galaxy being pulled by gravity of nearby clusters & superclusters
- Provide us with a way to measure our motion with respect to the absolute frame of reference of expanding space itself

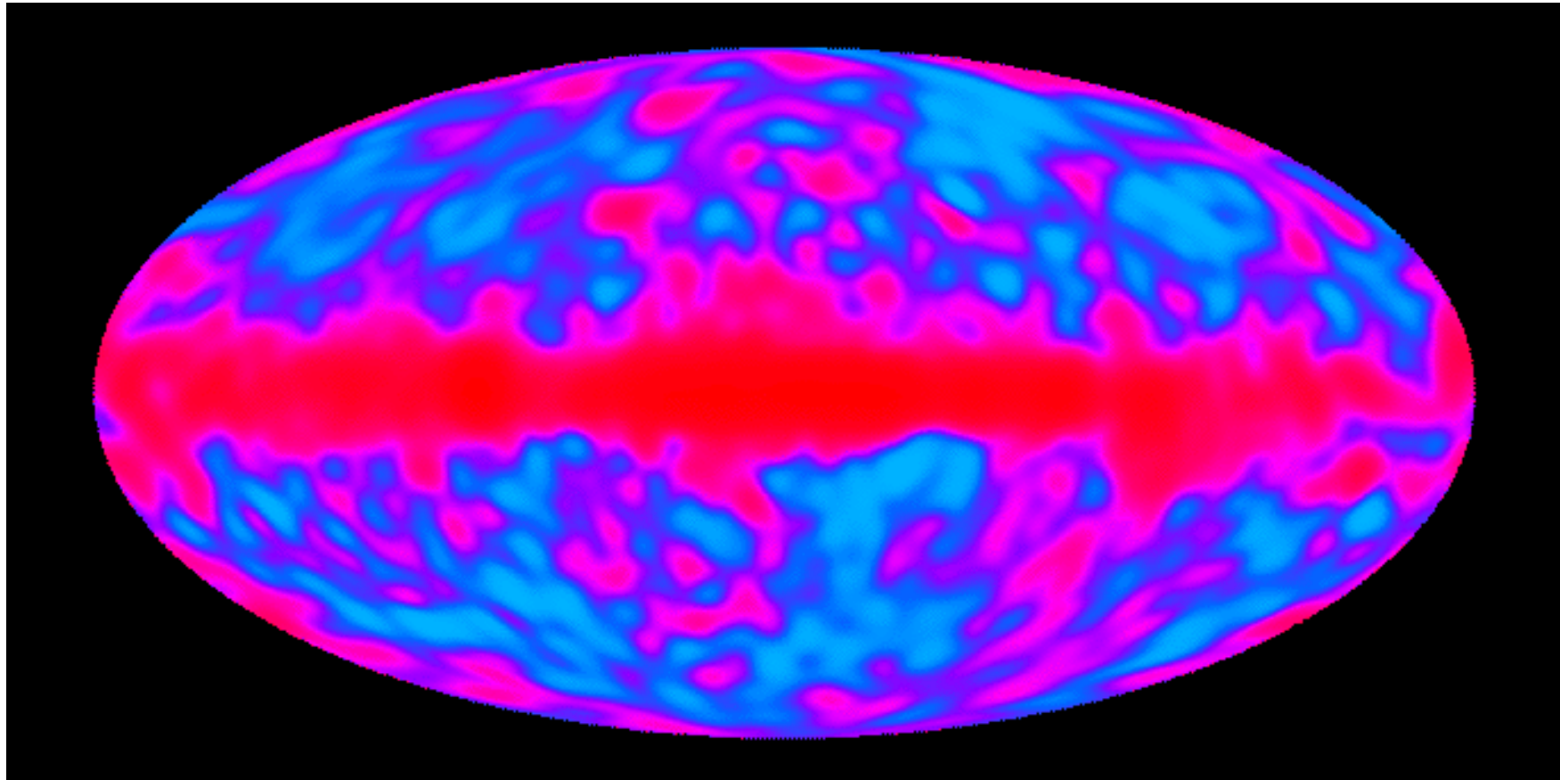


99.999% of average signal and
Dipole signal removed

DIRBE 1.25, 2.2, 3.5 μm Composite

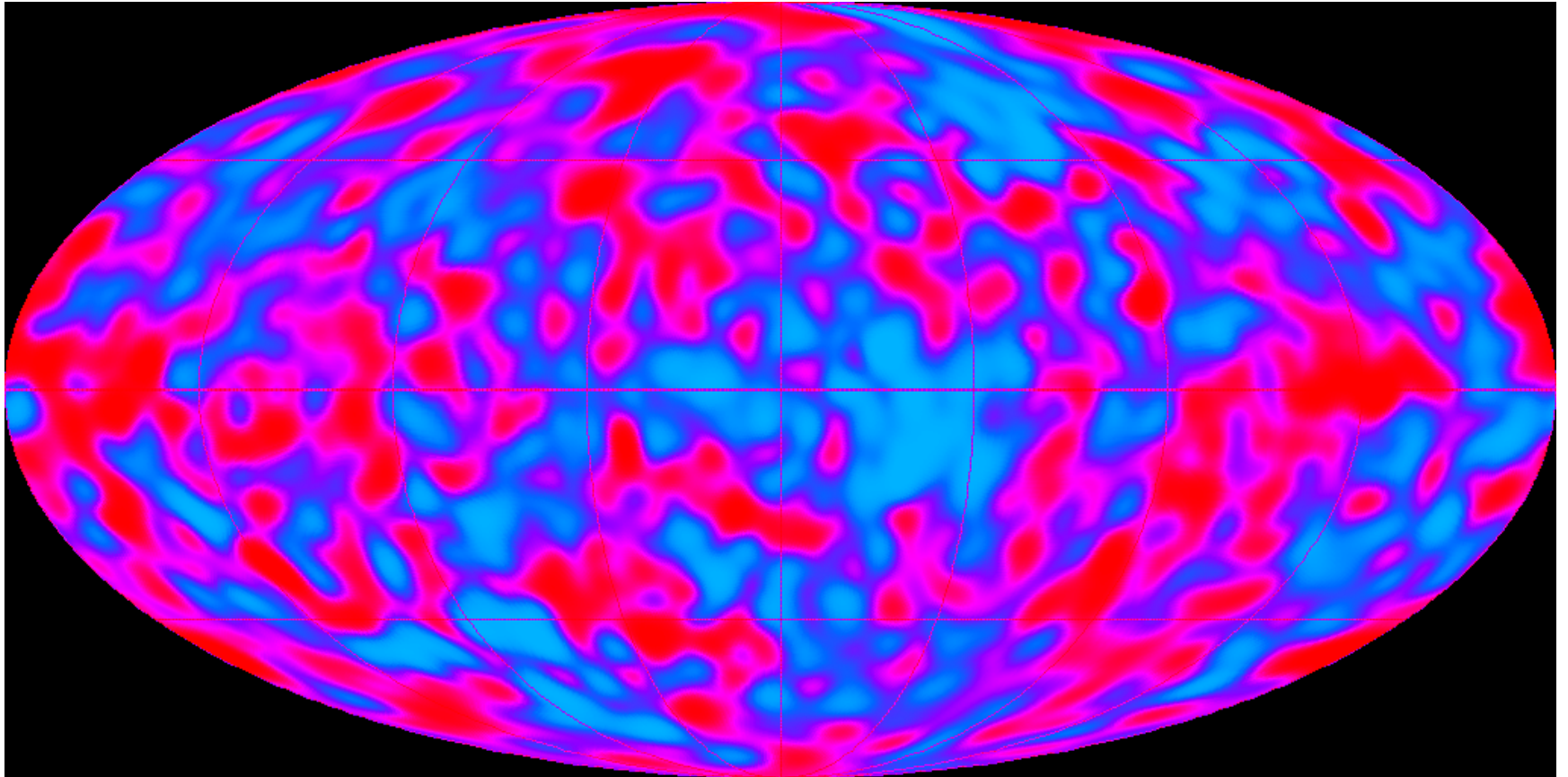


Our Milky Way Galaxy



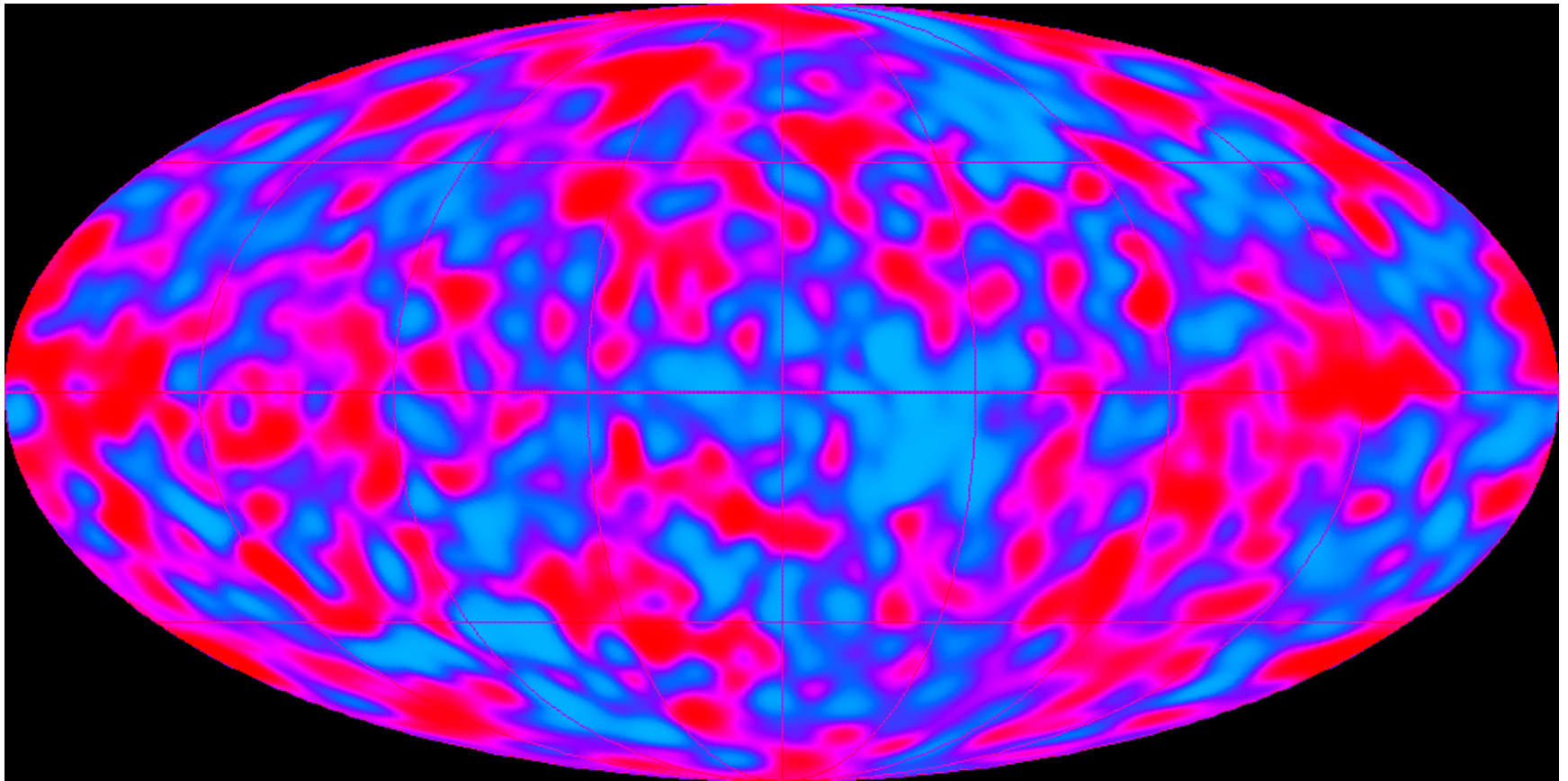
99.999% of average signal and
Dipole signal removed

COBE 1992



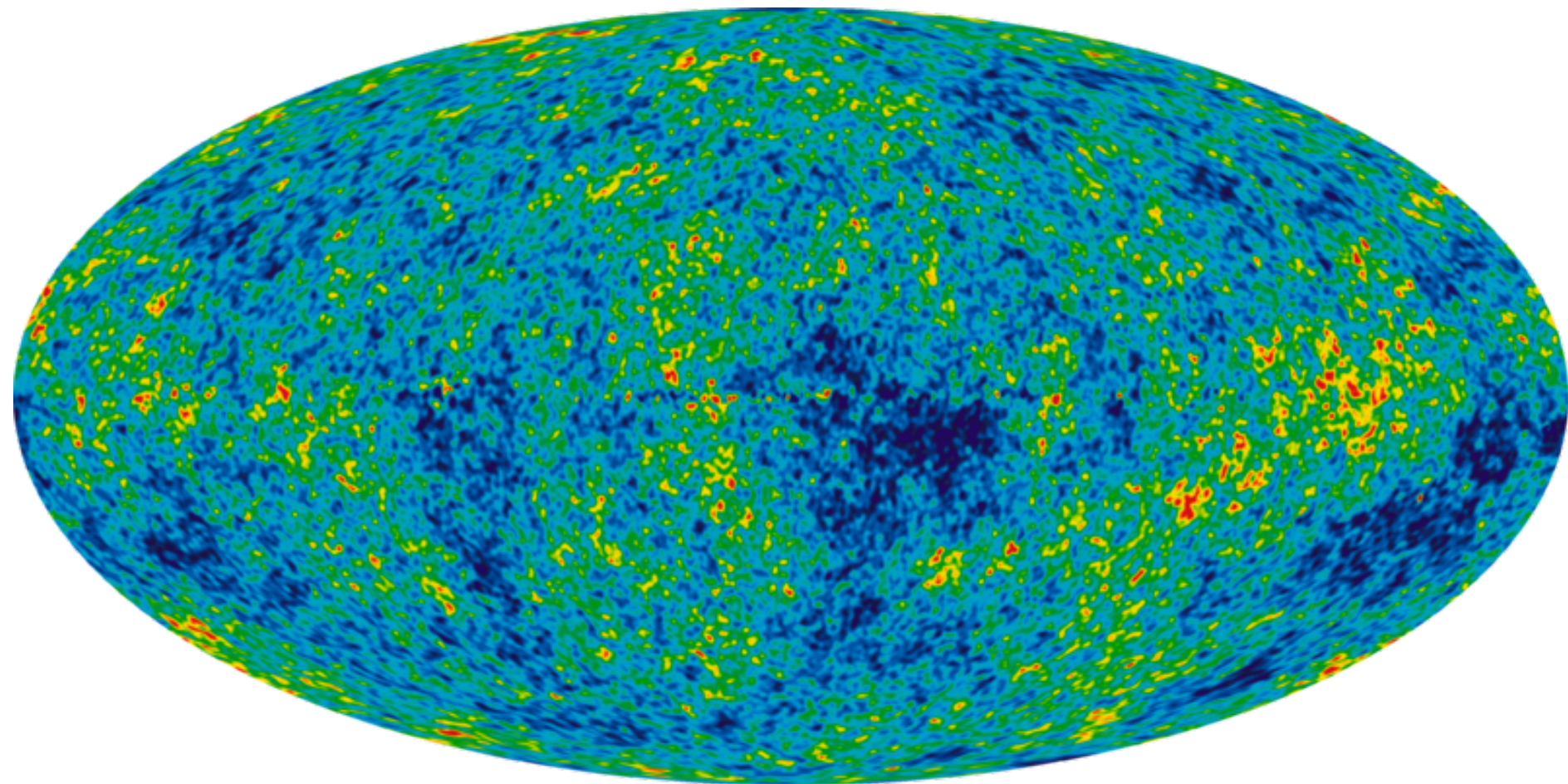
99.999% of average signal & Dipole pattern
& Milky Way signal removed

CMB Map from COBE Satellite 1992

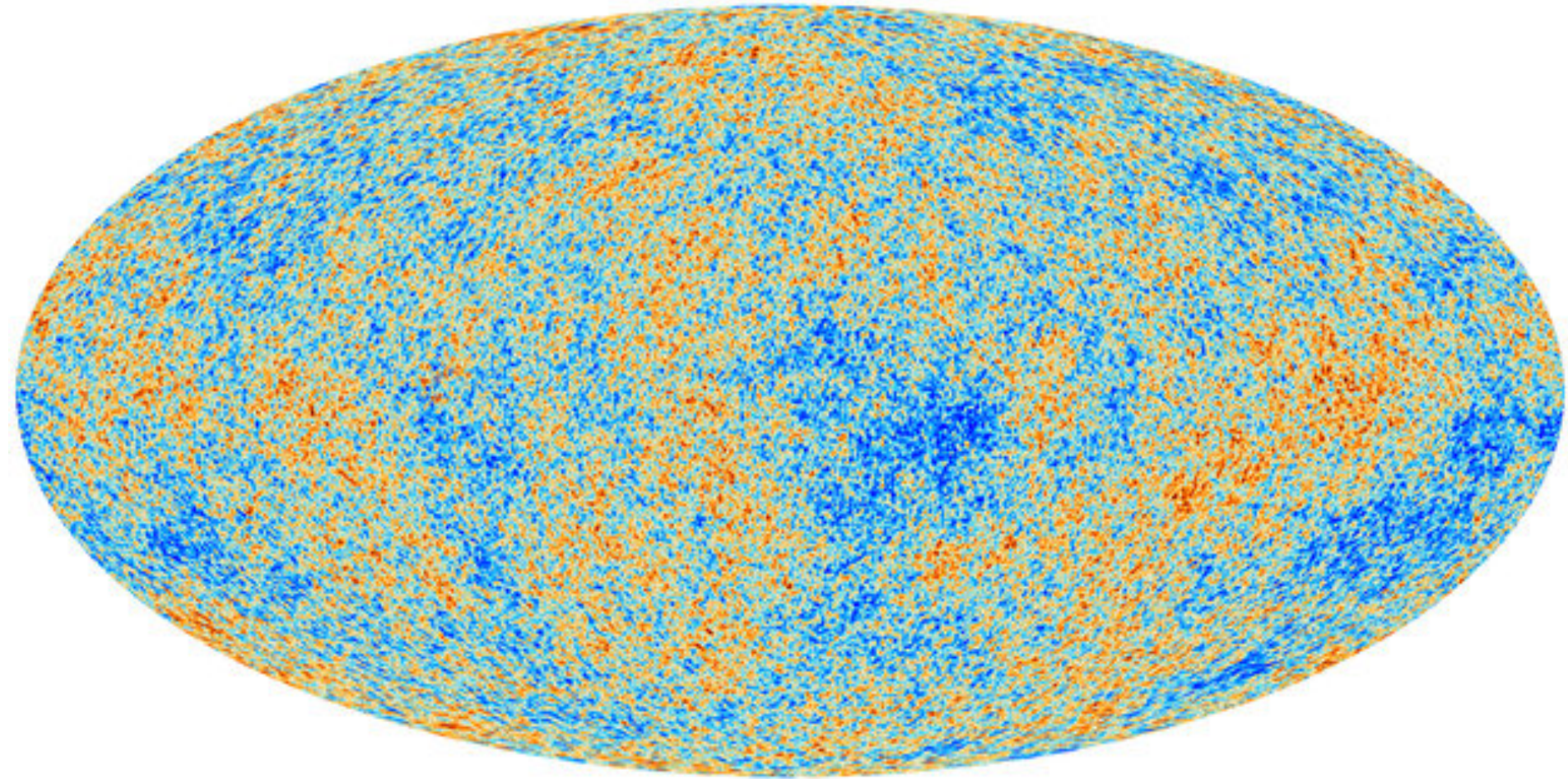


Nobel Prize in Physics in 2006 "the COBE-project can be regarded as the starting point for cosmology as a precision science".

CMB map from WMAP satellite 2001

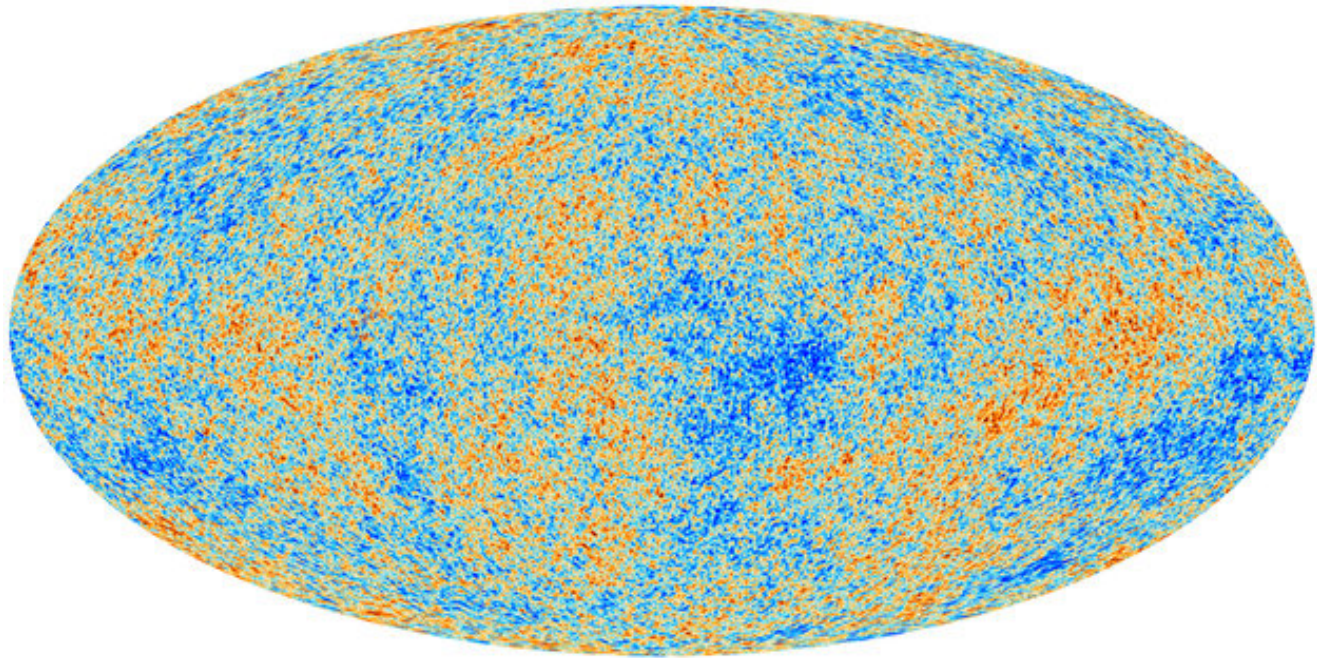


CMB map from PLANCK satellite March 2013



What is CMB? It is “snapshot” of early universe!

when it cooled enough after the Big Bang to allow protons and electrons to combine to make (long-lived) atoms for the first time, making the universe transparent to cosmic photons



at $t_{\text{ABB}}=380,000$ yrs

like “baby picture” ...

380,000 yr/13.8 Byr is like 1 day/80 years

Although CMB is pretty isotropic (uniform to 99.9%), there are 2 small but important anisotropies

b. small scale fluctuations (smaller, more irregular variations)

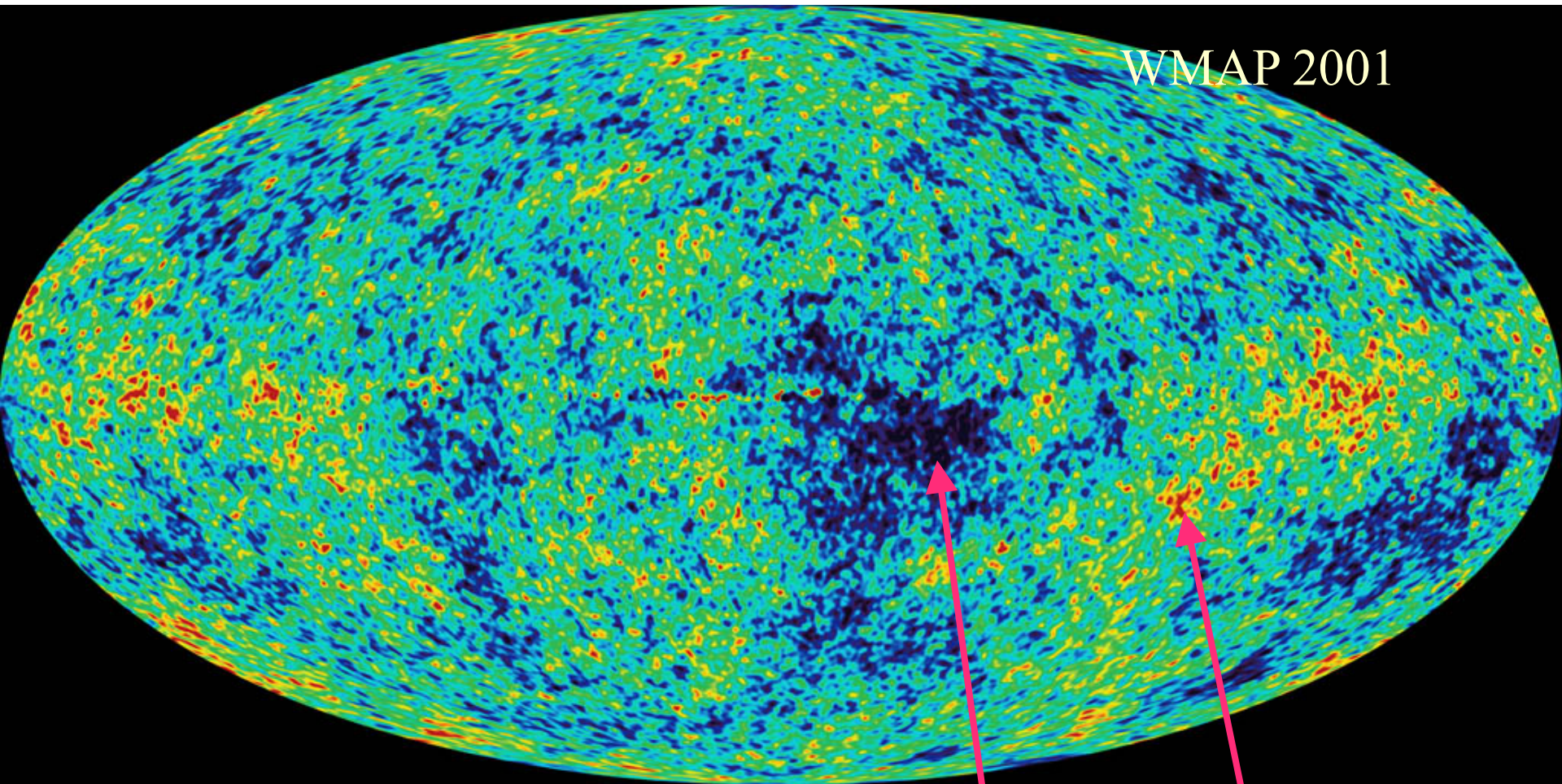
small shifts in peaks of CMB spectra from one spot to another, corresponding to temperature differences of $\Delta T/T_{av} = 6 \times 10^{-6}$

these are true temperature differences, not Doppler shifts

The dipole anisotropy tells us about our motion wrt the universe, but not much about the universe itself!

These fluctuations tell us about the early universe. They are a way to directly study the “primordial fireball” which was the universe 380,000 years ABB.

WMAP 2001



$$\Delta T = (T_1 - T_2)/2$$

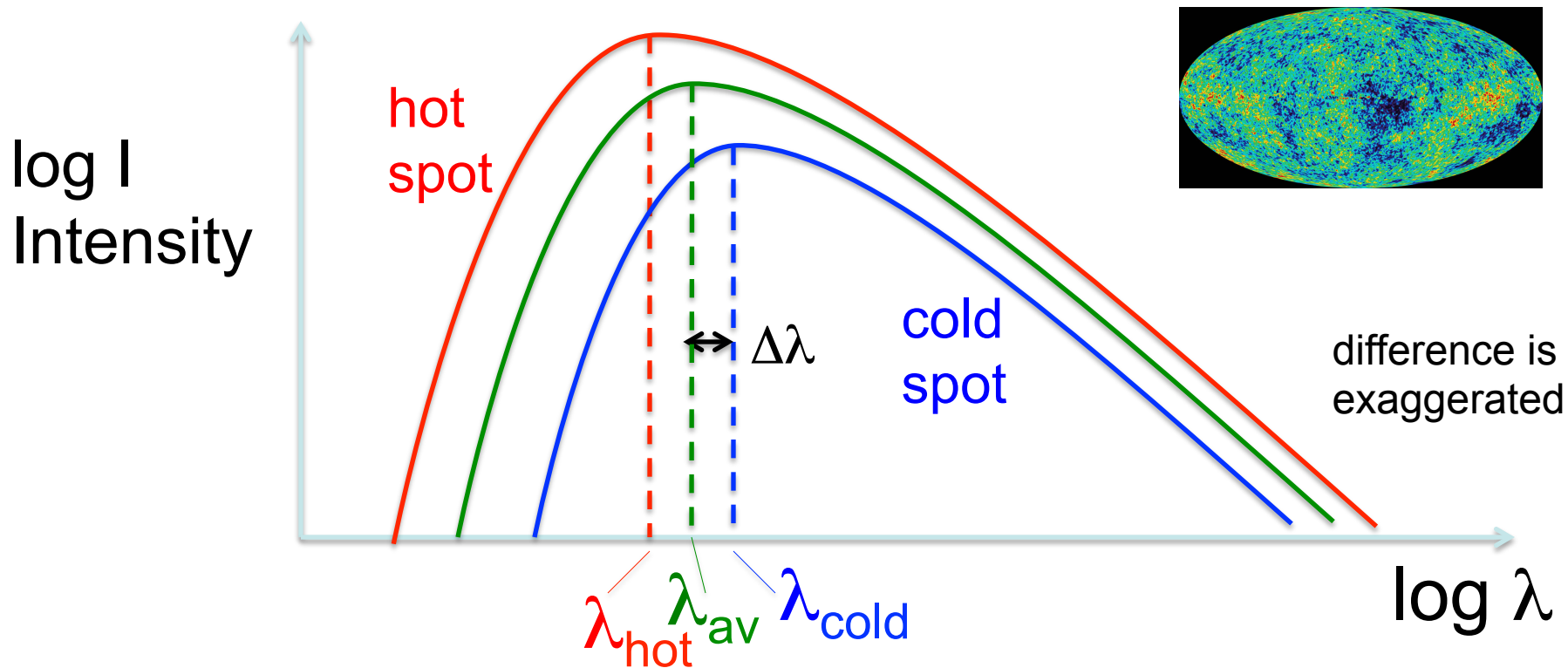
$$T_{\text{av}} = 2.725\text{K}$$

$$\Delta T/T_{\text{av}} = 6 \times 10^{-6}$$

Cold spot T_2

Hot spot T_1

CMB has hot spots and cold spots



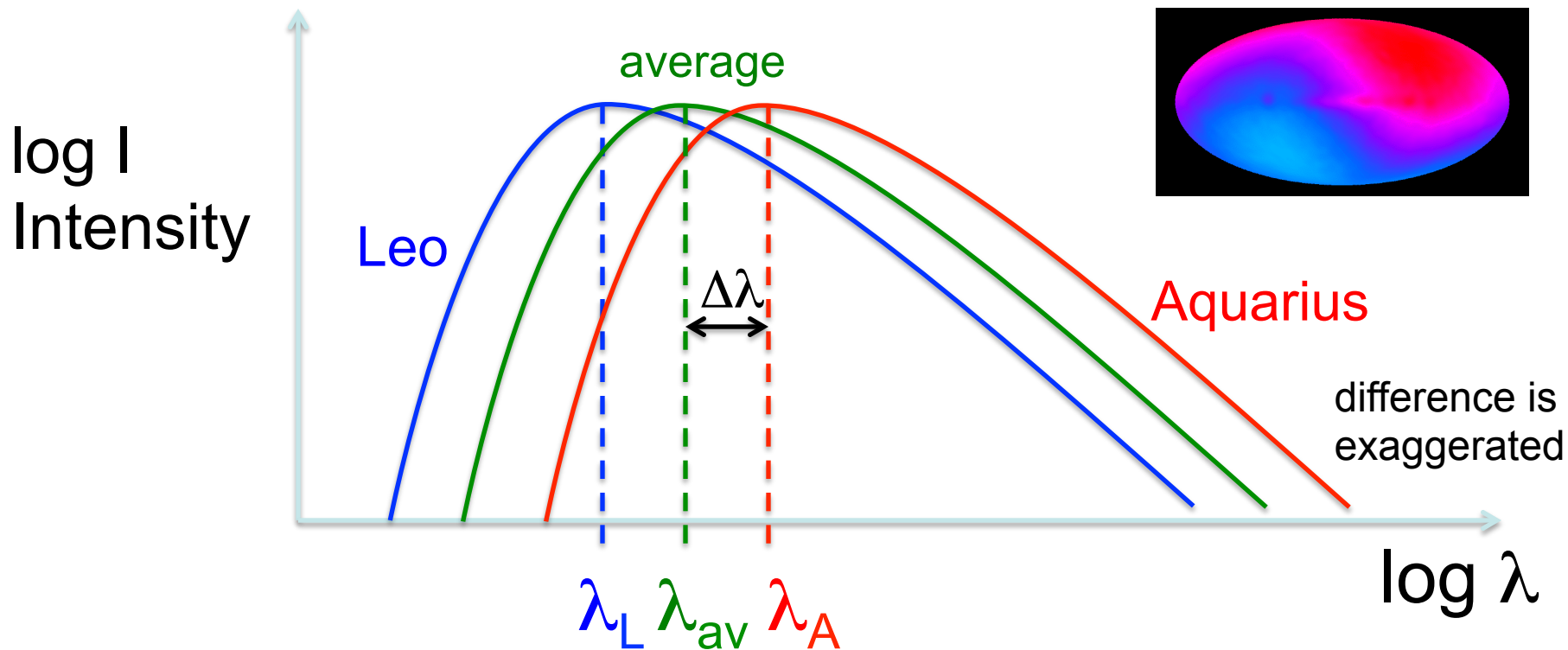
these are temperature variations

(curves don't cross)

$$\frac{\Delta\lambda}{\lambda_{\text{avg}}} = \frac{\Delta T}{T_{\text{avg}}} = 6 \times 10^{-6}$$

i.e. few parts per million

CMB spectrum slightly **blueshifted toward Leo**
 CMB spectrum slightly **redshifted toward Aquarius**



this is Doppler shift caused by motion of earth wrt CMB
 (curves cross)

$$\frac{\Delta\lambda}{\lambda_{avg}} = v / c = 0.0012 = 1.2 \times 10^{-3}$$

$$V_{earth,CMB} = 0.0012c = 370 \text{ km/sec}$$

A Mollweide projection map of the Cosmic Microwave Background (CMB) from the Wilkinson Microwave Anisotropy Probe (WMAP) in 2001. The map shows a complex pattern of temperature fluctuations across the sky, with colors ranging from dark blue (cooler) to red and yellow (warmer). The fluctuations are most prominent at larger angular scales, showing a clear dipole and quadrupole moment. The text "WMAP 2001" is visible in the upper right corner of the map.

WMAP 2001

Small fluctuations in cosmic background radiation trace the

1. Seeds of large-scale structure in universe and tell us
2. How space in the Universe is curved &
3. Contents of Universe (how much matter & energy)!

1.seeds of structure

Gravity acts to make things collapse and make universe lumpier

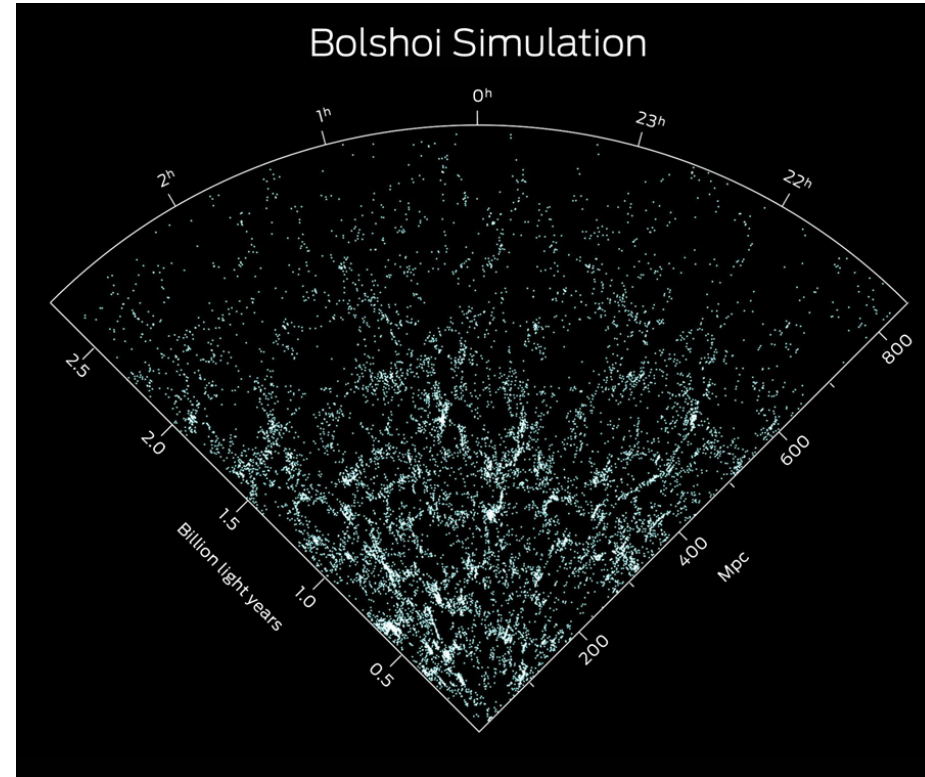
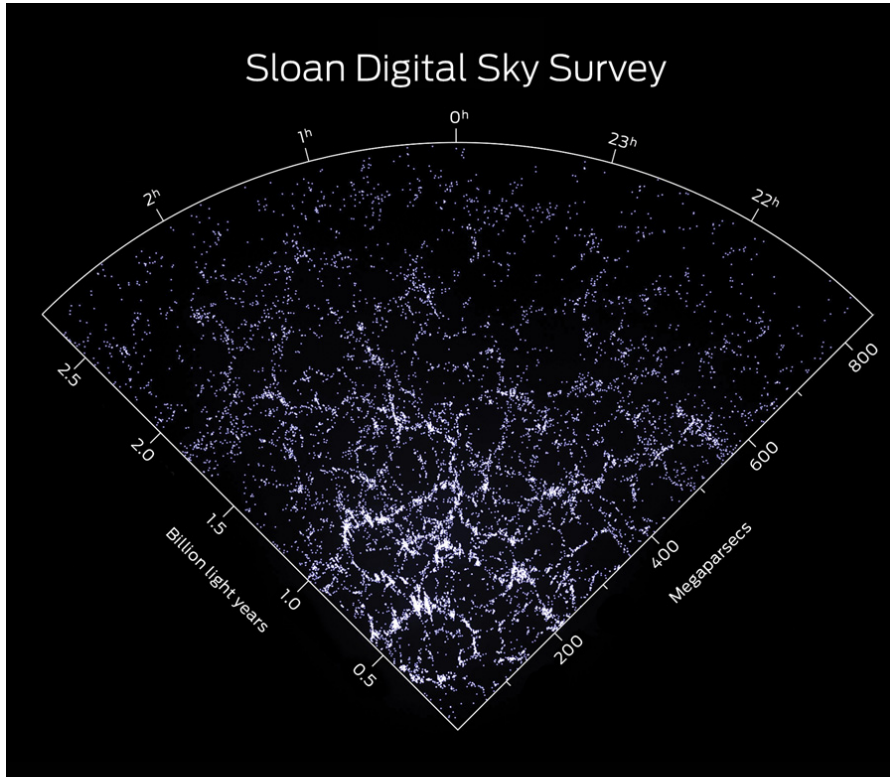
Now the matter distribution is very lumpy ..

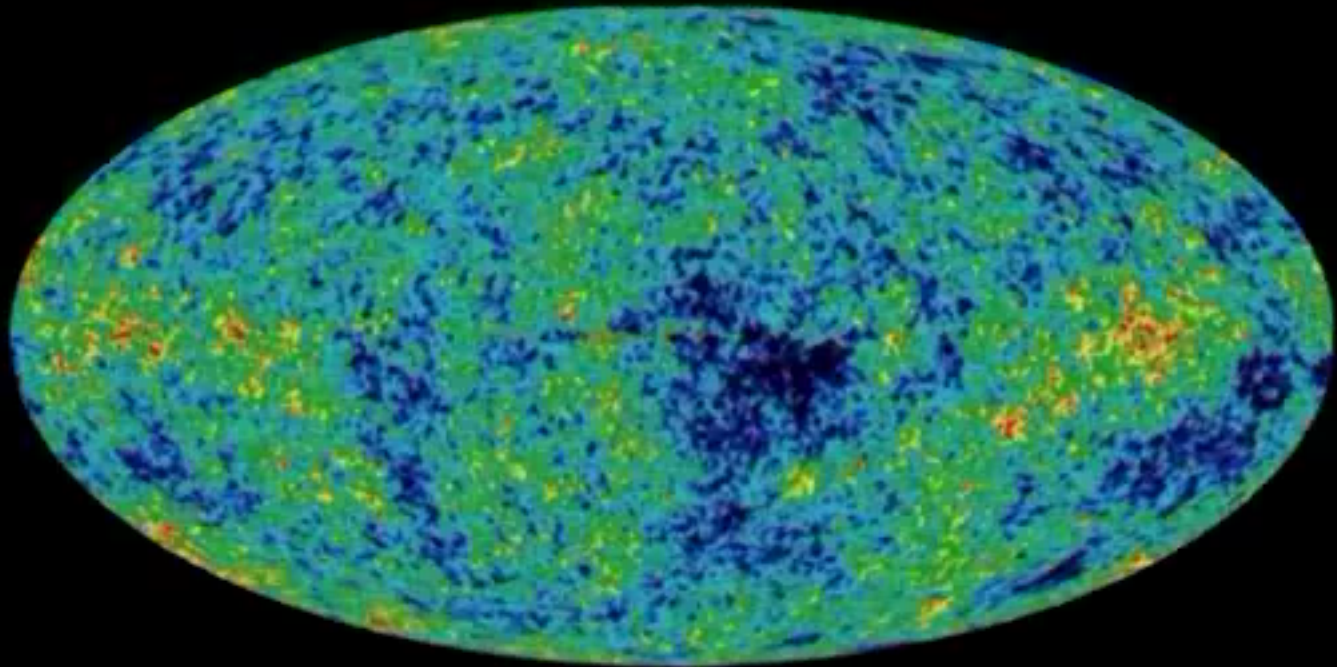
But how & when did “structure” in the universe form?

structure = concentrations of matter like superclusters, clusters, galaxies, stars

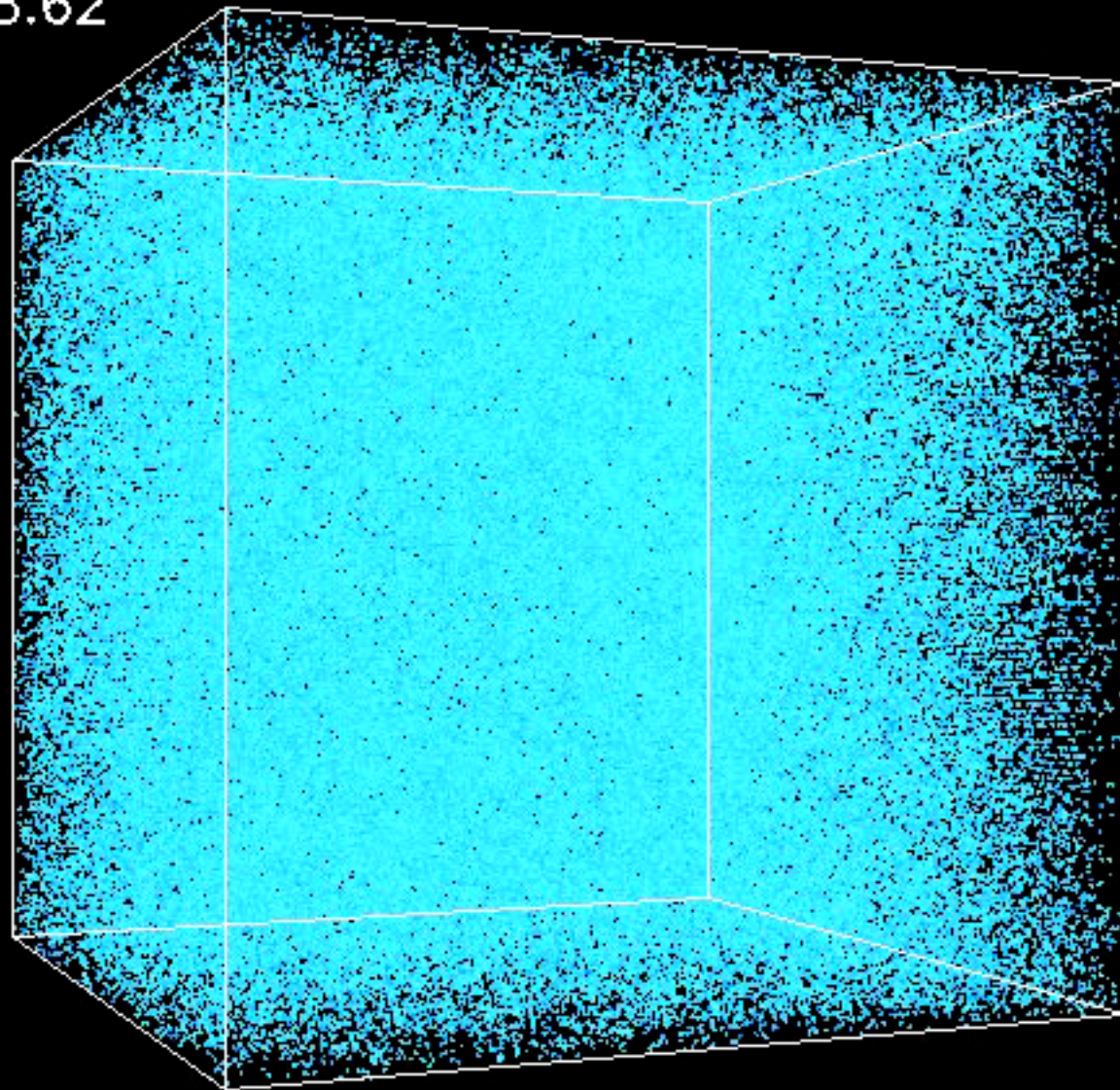
Large-scale structure in universe **TODAY**

Data vs. Simulation





$Z=28.62$

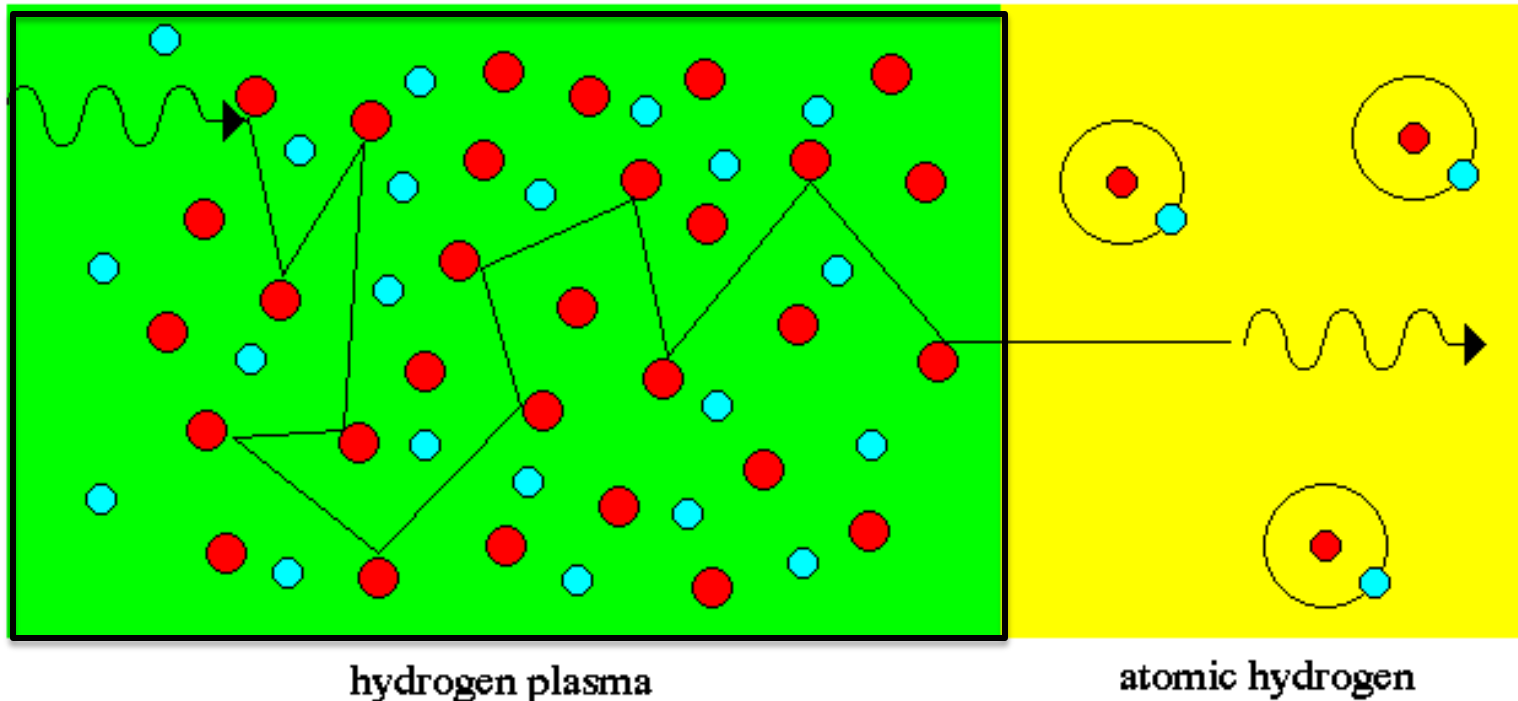


Why didn't lumps of matter form before recombination?

- A. The matter was too hot for gravity to form lumps
- B. Gravity was too weak compared to dark energy
- C. Radiation was coupled to matter, preventing lumps from cooling
- D. Radiation was the main source of mass-energy and gravity until recombination
- E. Not enough time for gravity to form lumps
- F. Just hard to get going so early in the morning

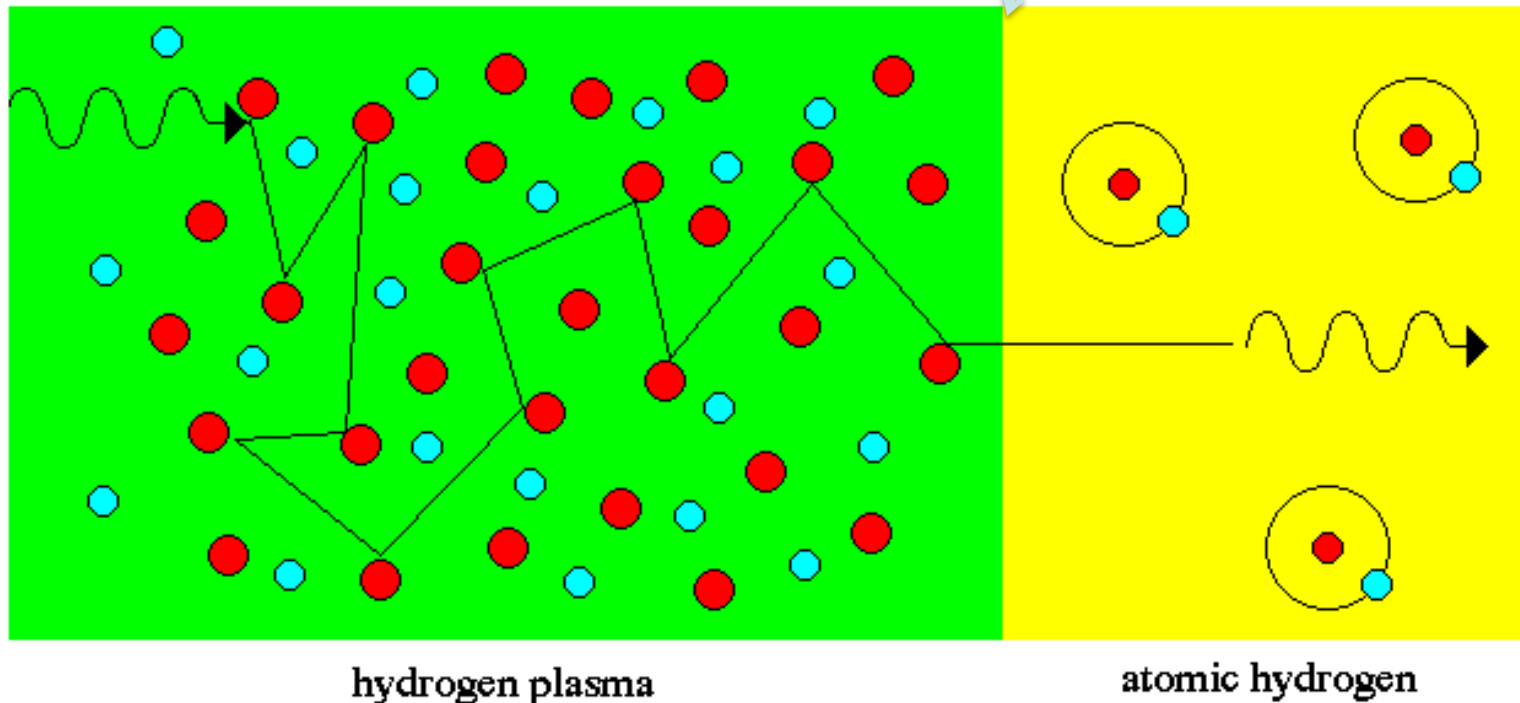
Before recombination

- Matter is in the form of plasma (p' s & e' s)
- Cosmic photons collide with p' s and e' s, scattering them – changing energy & direction
- Atoms can form but are quickly destroyed (ionized) by cosmic photons
- Cosmic photons had enough energy to ionize atoms
- Universe opaque to cosmic photons
- ***Matter & energy (cosmic photons) tightly coupled***



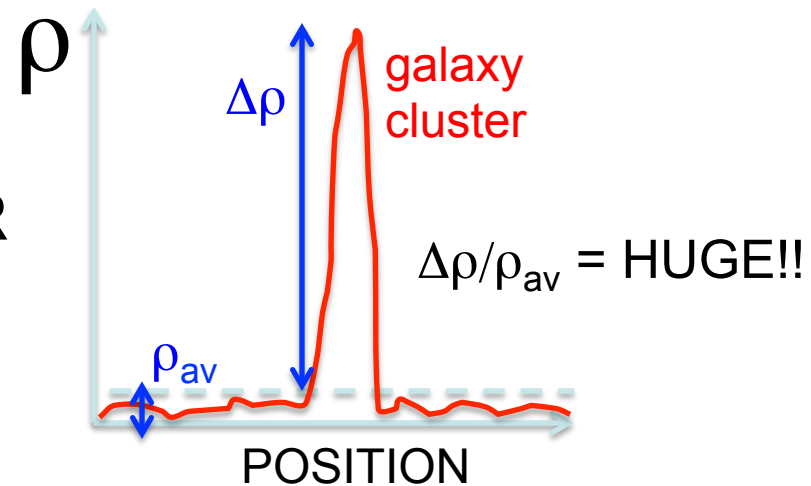
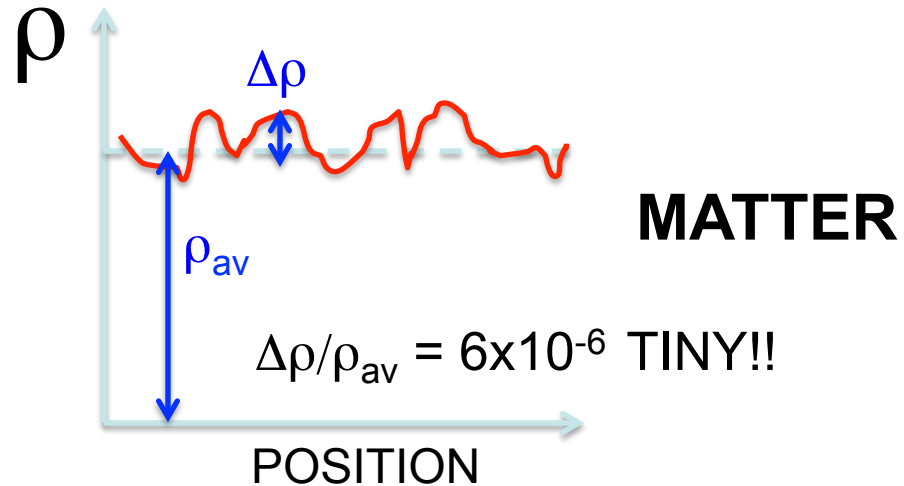
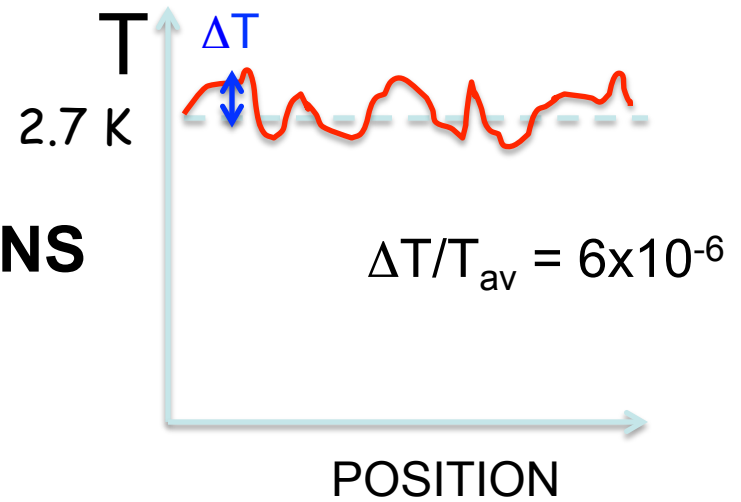
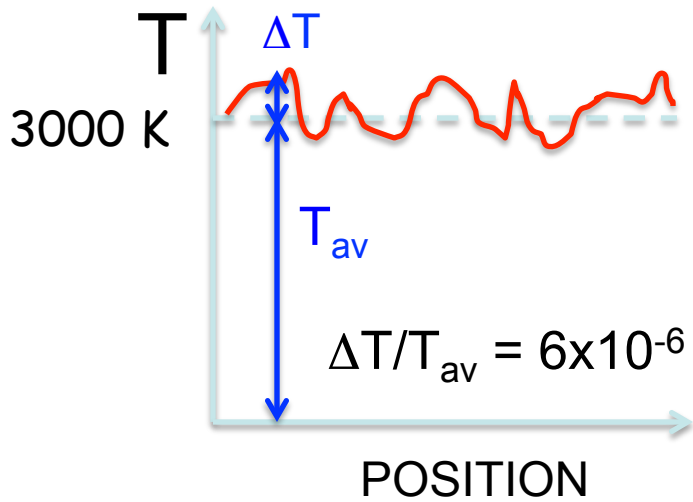
Universe AT $z=1100$, $T=3000\text{K}$, $t_{\text{ABB}}=380,000$ yr

- Cosmic photons suddenly no longer have enough energy to ionize atoms (due to expansion)
- p 's & e 's combine to form atoms (not ionized)
- “era of recombination” (combination?)
- **“era of decoupling” (of matter & cosmic photons)**
- Moment when universe changed from being opaque to transparent (for cosmic photons)
- all cosmic photons we see now were created or last scattered (direction or energy changed) at this time



THEN $t = 380,000$ yr ABB

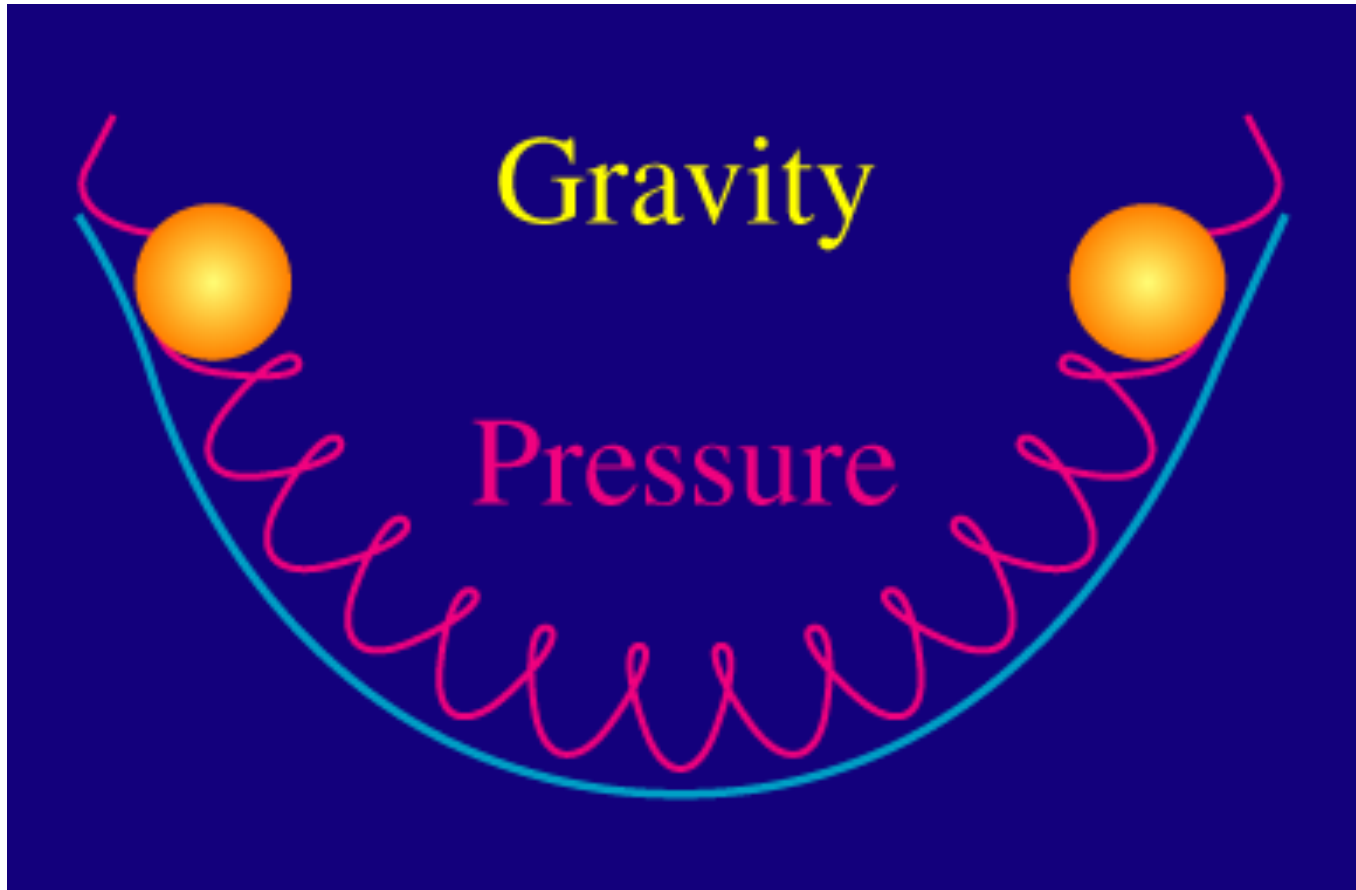
NOW $t = 13.8$ Byr ABB



before recombination, matter & photons coupled so structure can't form

structure really grows after recombination, once matter decoupled from cosmic photons

Why gravitational collapse doesn't happen before “recombination”



The pressure exerted by cosmic photons resists gravitational collapse

Dense lumps form from gravity if photons can escape & thereby release energy from the lump

Dense lumps form from gravity if photons can escape & thereby release energy from the lump

- If lump starts to collapse due to self-gravity, it can only continue to collapse if it can release “gravitational binding energy”, e.g. in the form of photons

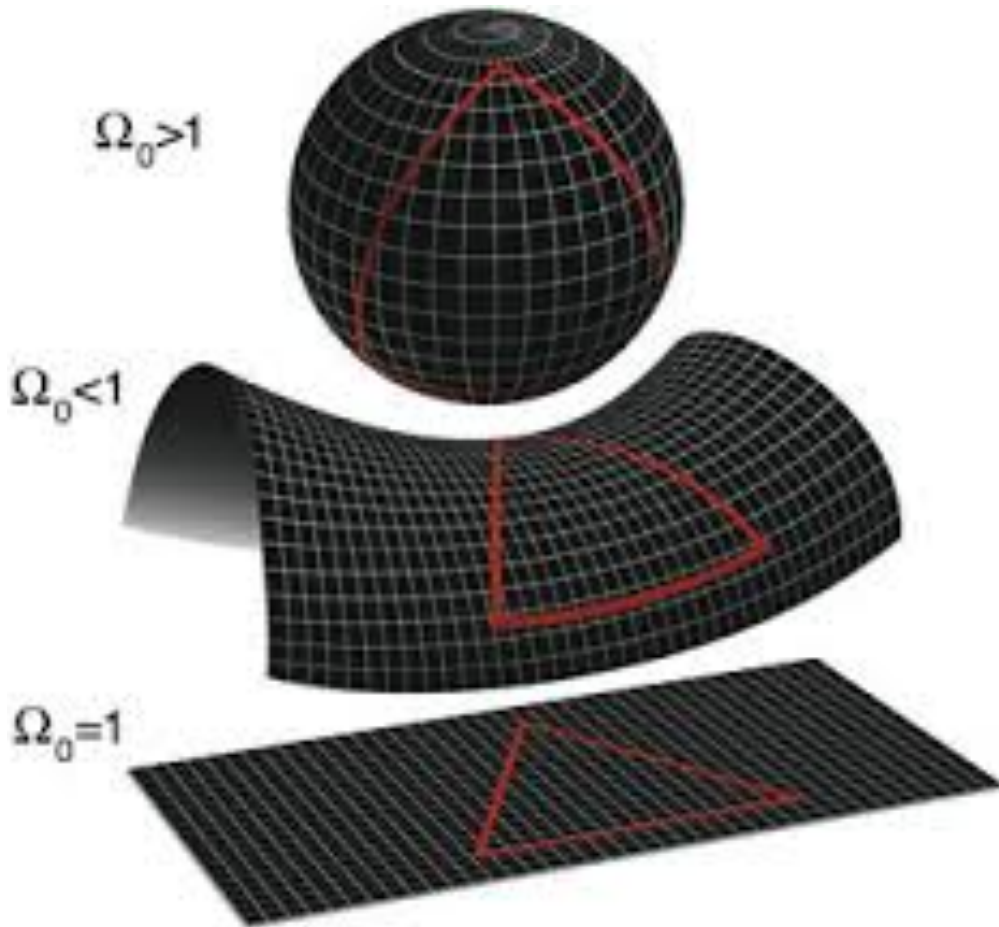
Dense lumps form from gravity if photons can escape & thereby release energy from the lump

- If lump starts to collapse due to self-gravity, it can only continue to collapse if it can release “gravitational binding energy”, e.g. in the form of photons
- If energy can't be released, lump will not collapse (before “decoupling”)

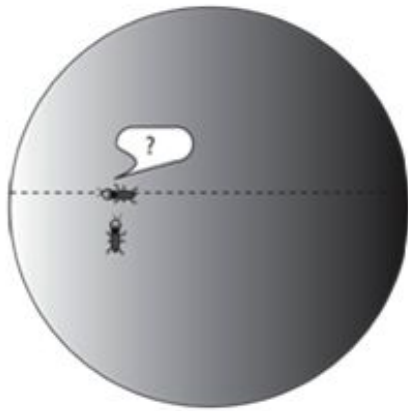
Dense lumps form from gravity if photons can escape & thereby release energy from the lump

- If lump starts to collapse due to self-gravity, it can only continue to collapse if it can release “gravitational binding energy”, e.g. in the form of photons
- If energy can't be released, lump will not collapse (before “decoupling”)
- If energy can be released, lump will collapse (after “decoupling”)

curvature of space in universe



The Ant Universe



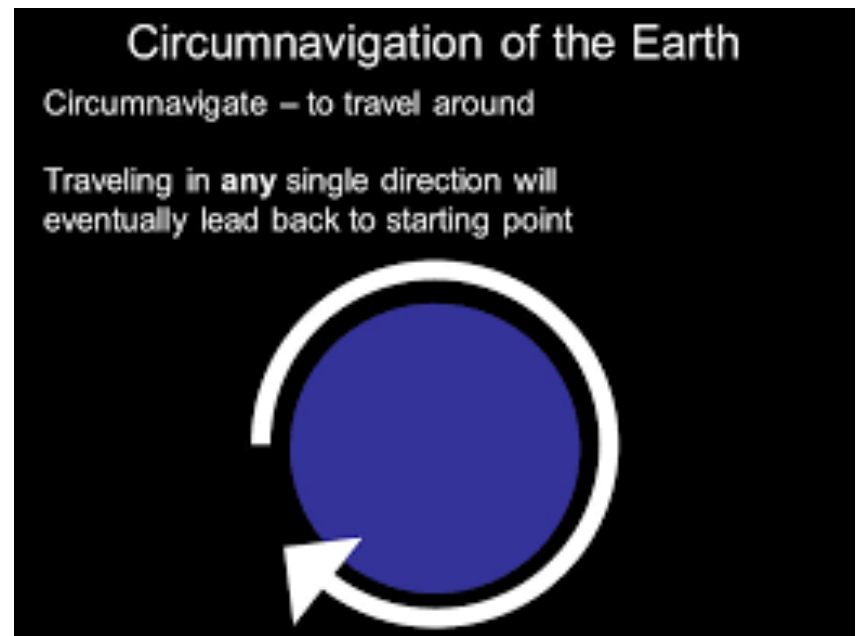
- Ants on surface of a balloon are a good model – the ants can “traverse” the surface of the balloon and never run into a boundary

What does it mean for space in universe to be curved?

- If space were positively curved (spherical geometry, closed) and you could travel infinitely fast, you could circumnavigate the universe!!



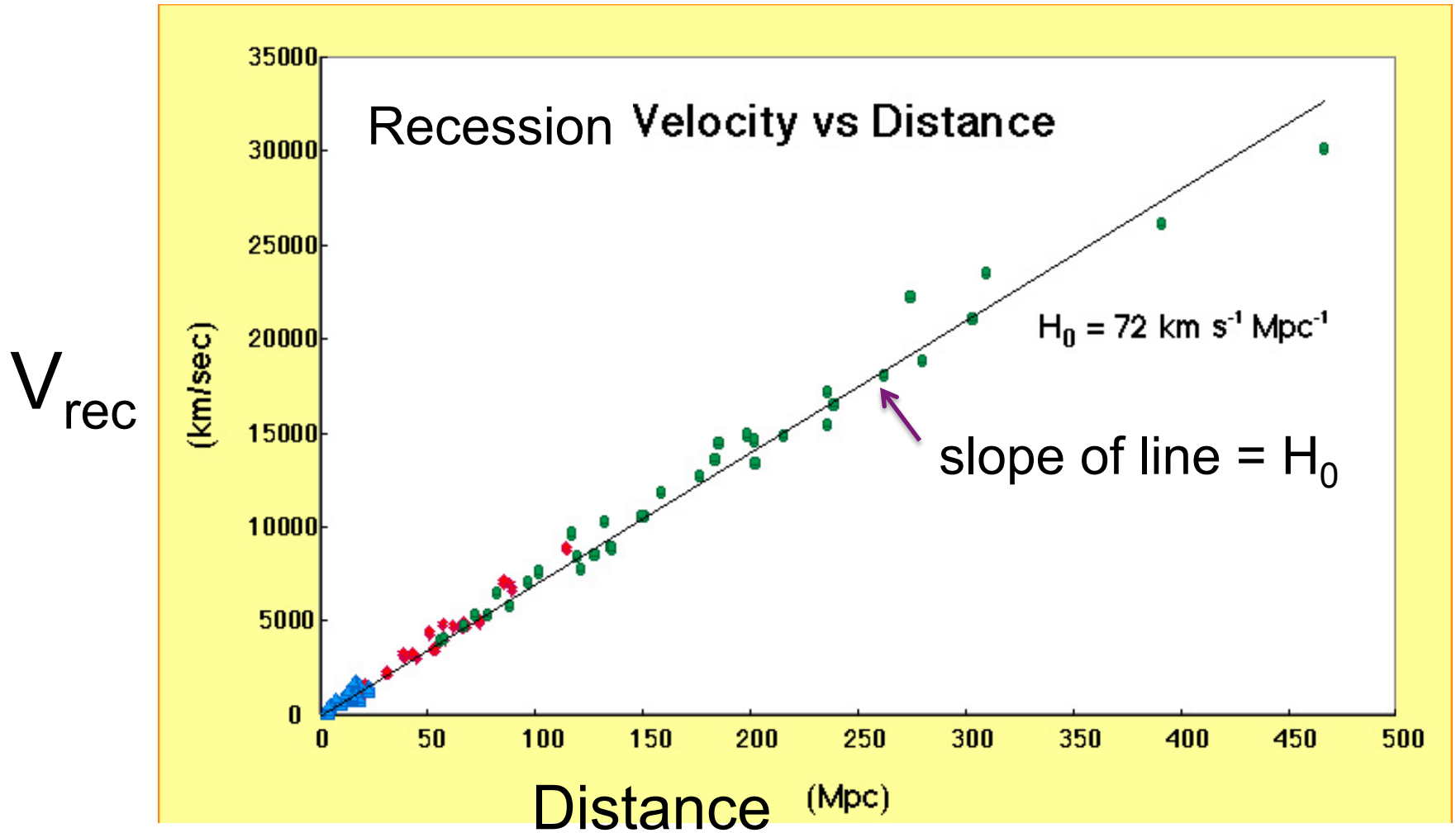
dreamstime.com



What does it mean for space in universe to be curved?

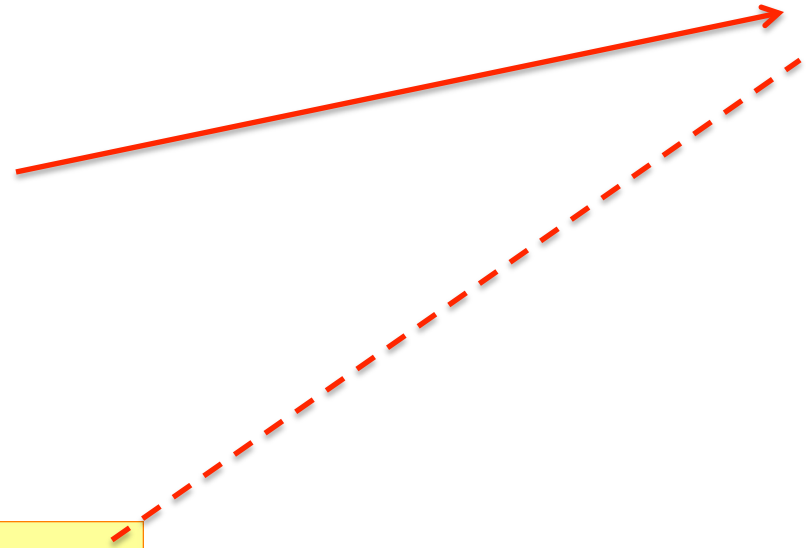
- If space were positively curved (spherical geometry, closed) and you could travel infinitely fast, you could circumnavigate the universe!!
- **But... since universe is expanding and fastest possible speed *through* space is c , this is not quite possible**

Hubble Law

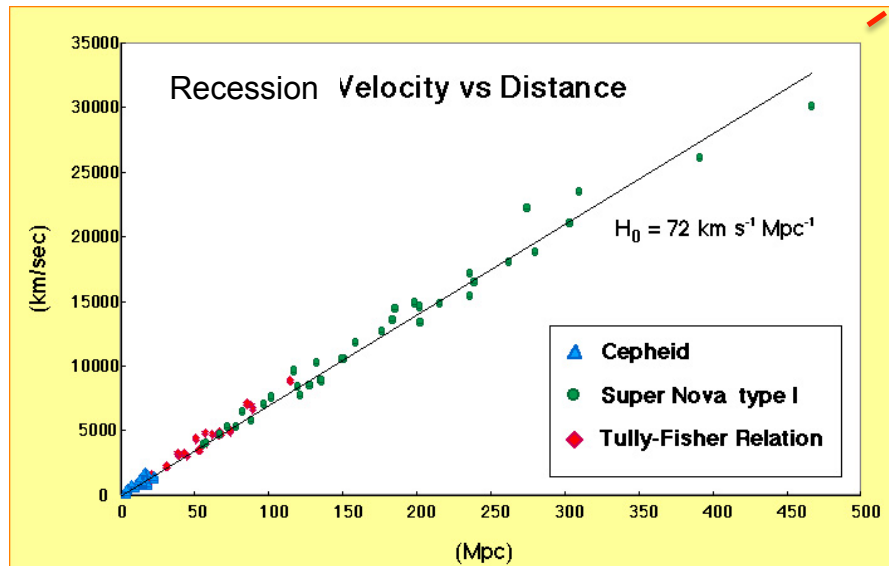


Hubble Law

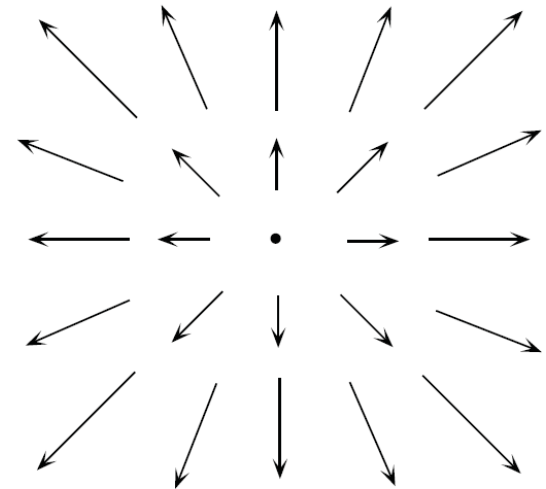
eventually at some distance the recession speed becomes $> c$



V_{rec}



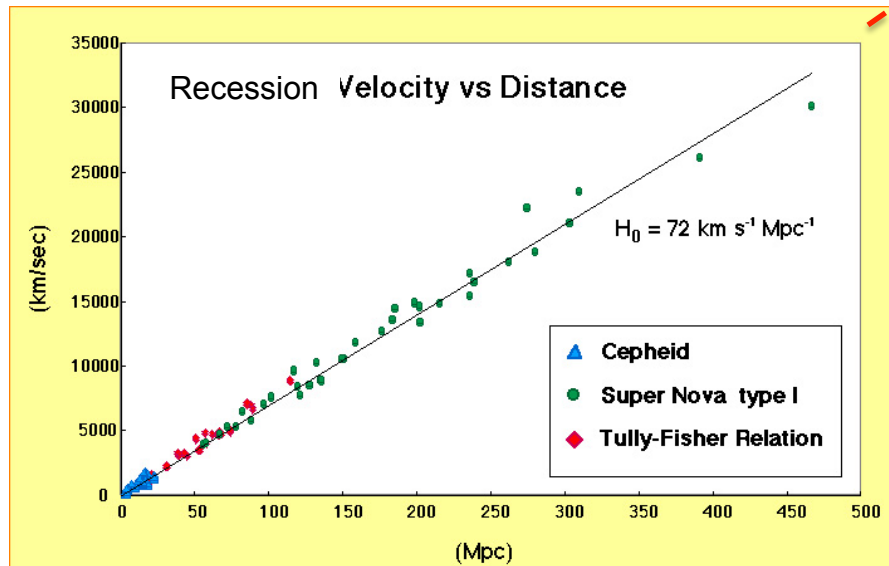
Distance



Hubble Law

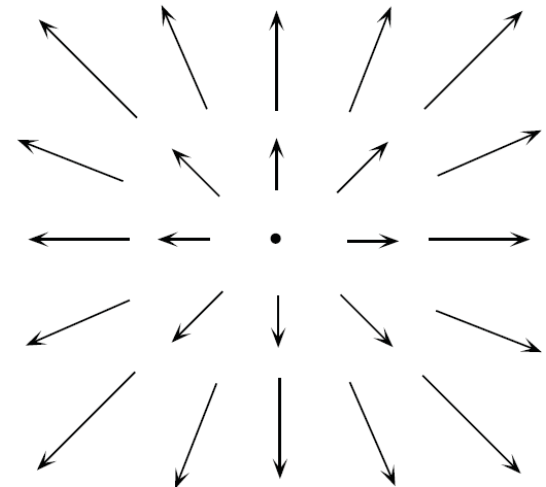
eventually at some distance the recession speed becomes $> c$

space can expand faster than the speed of light!



V_{rec}

Distance



Space can expand at $>c$

- General Relativity says: distant regions of space can separate from each other at speeds $> c$
- Special Relativity says: things cannot move *through* space at speeds $> c$

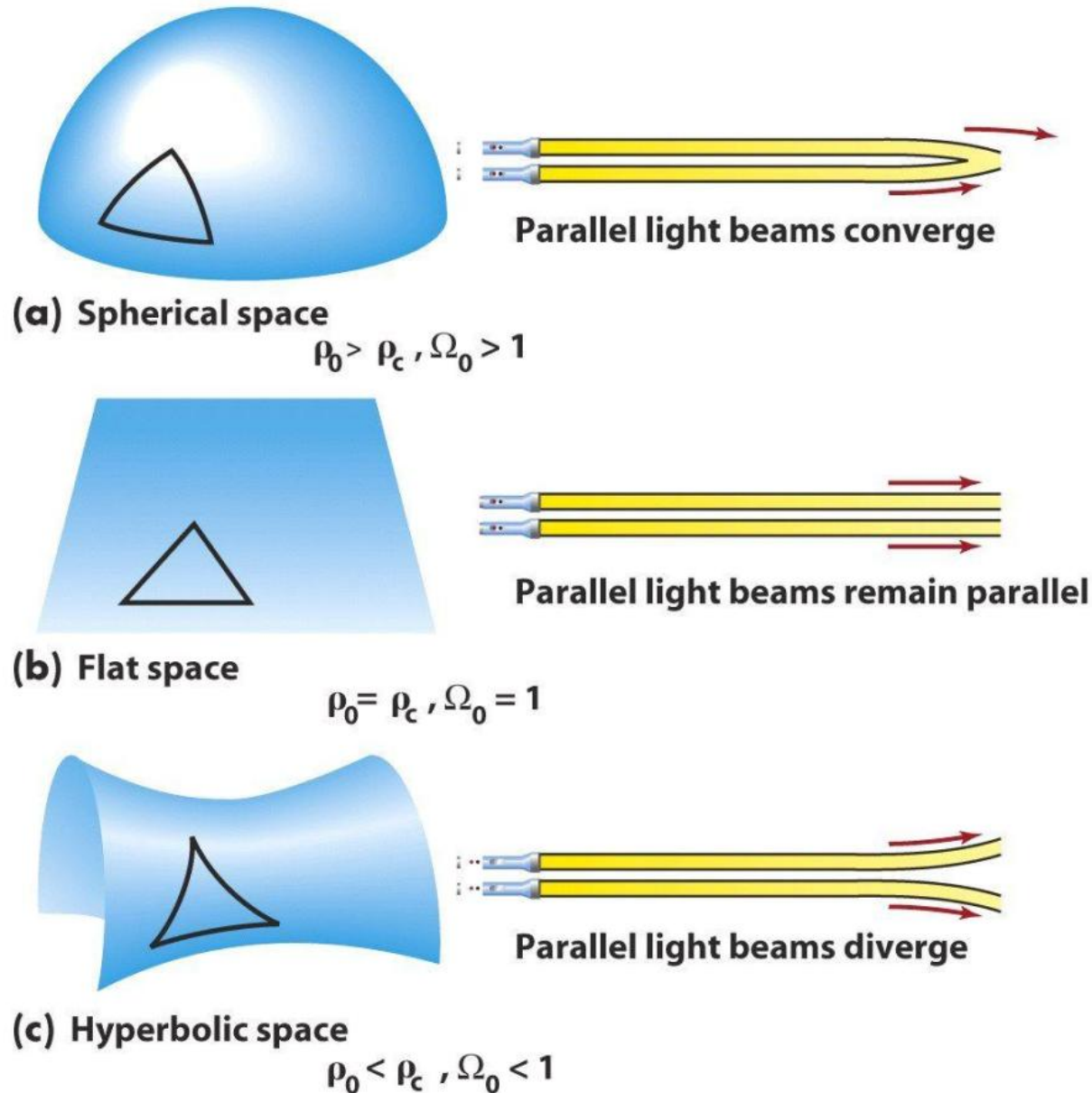
What does it mean for space in universe to be curved?

- If space were positively curved (spherical geometry, closed) and you could travel infinitely fast, you could circumnavigate the universe!!
- But... since universe is expanding and fastest possible speed *through* space is c , this is not quite possible
- **As universe expands, photons have further to travel – and distant regions of space are expanding away from us at faster than the speed of light (allowed by GR) – so photons can never catch up**

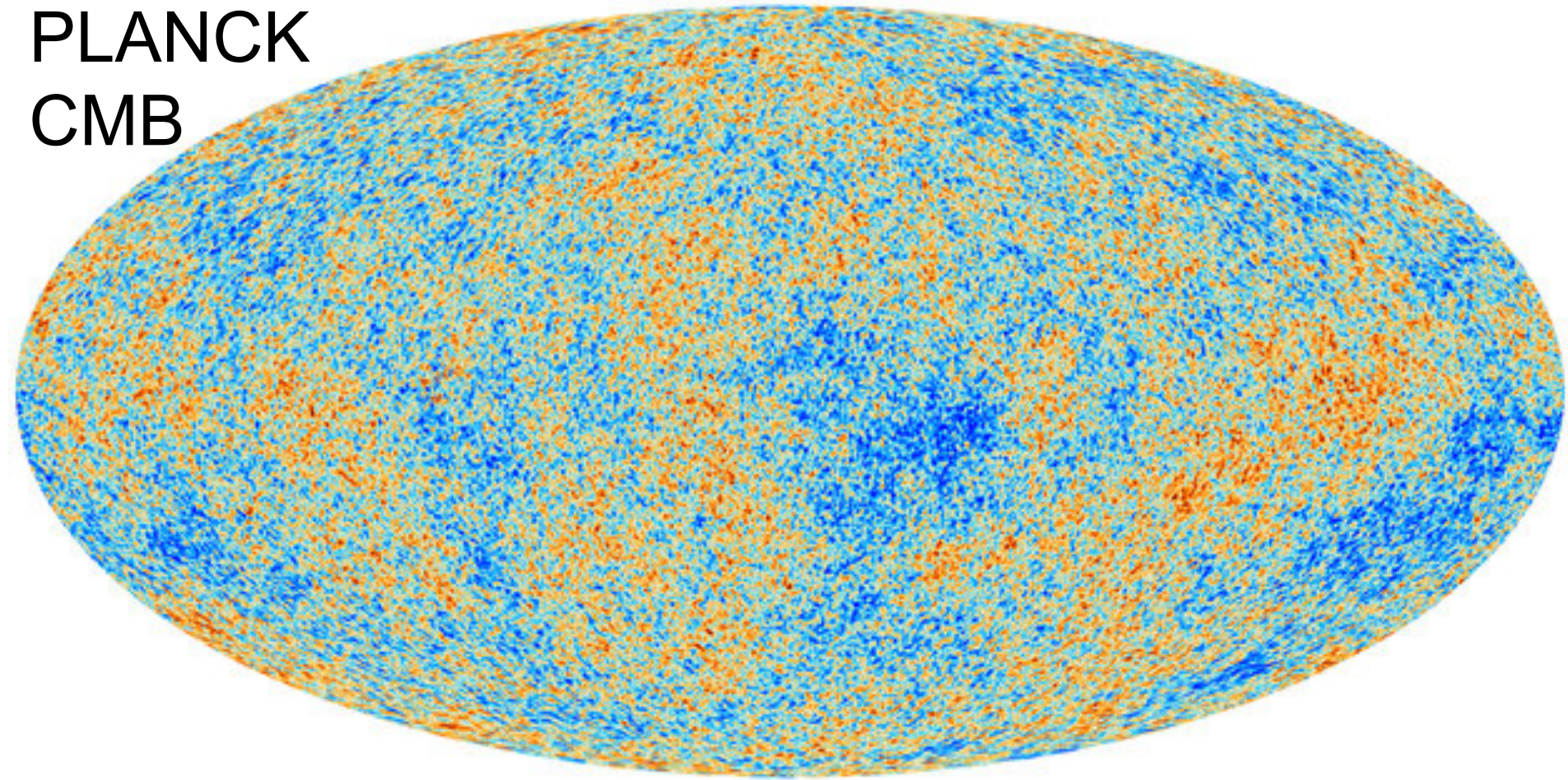
What does it mean for space in universe to be curved?

- If space were positively curved (spherical geometry, closed) and you could travel infinitely fast, you could circumnavigate the universe!!
- But... since universe is expanding and fastest possible speed *through* space is c , this is not quite possible
- As universe expands, photons have further to travel – and distant regions of space are expanding away from us at faster than the speed of light (allowed by GR) – so photons can never catch up
- **Only in *closed and contracting* universe would photons have enough time to circumnavigate the universe** (and our universe is neither...)

Possible space curvatures



PLANCK CMB

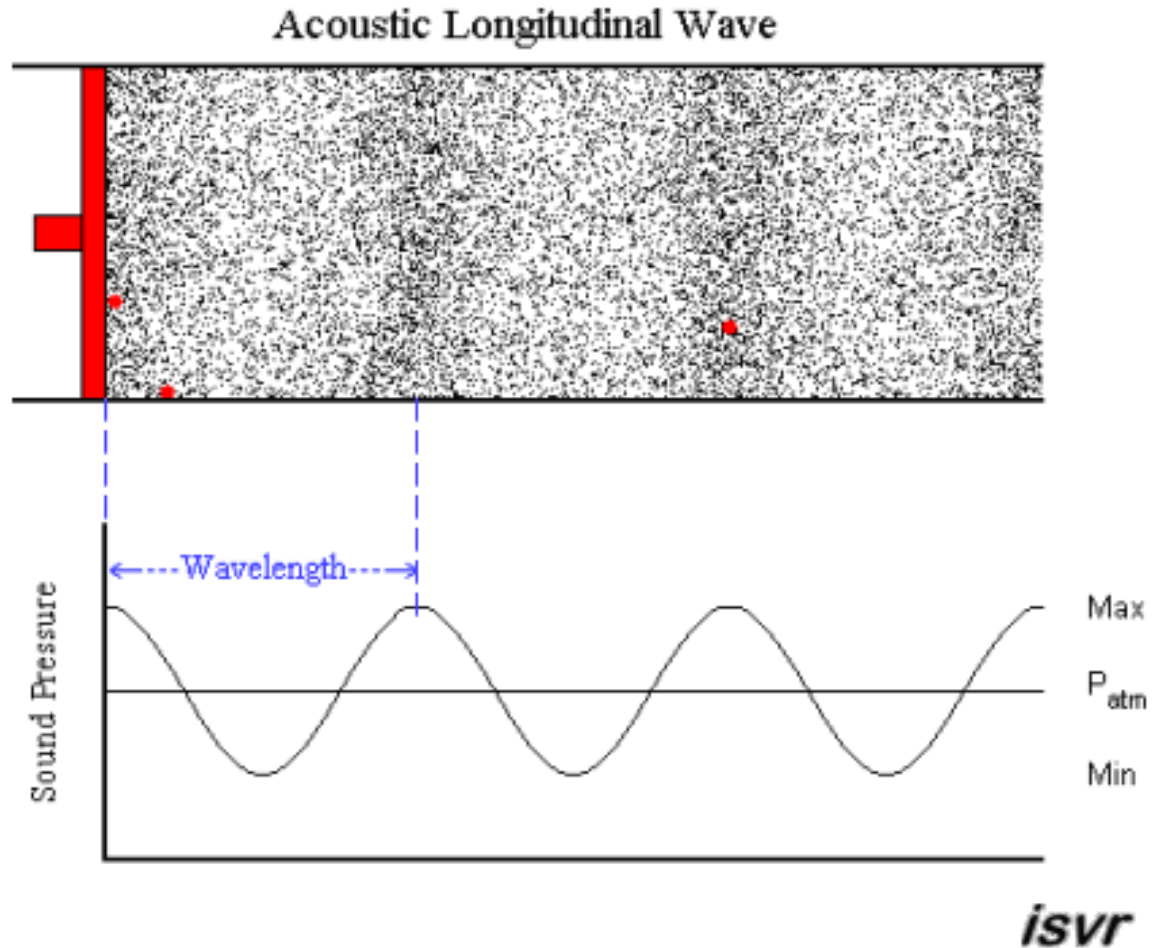


Small fluctuations in cosmic background radiation tell us
2. how space in the Universe is curved

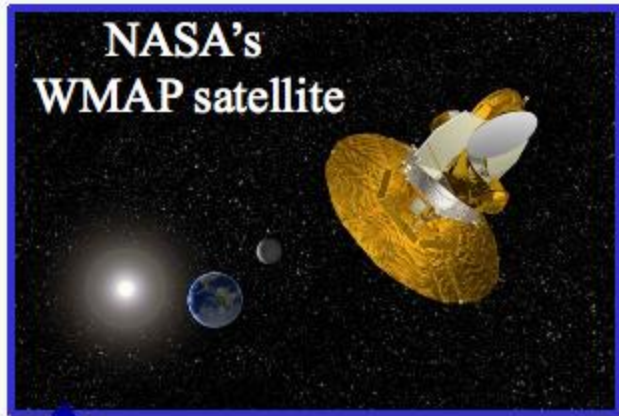
What are these fluctuations in CMB?

Fluctuations arise in very early universe ($t_{\text{ABB}} < 1$ sec) (as quantum fluctuations) – small non-uniformities which disturb the universe, causing sound waves

Most CMB fluctuations are *sound waves*

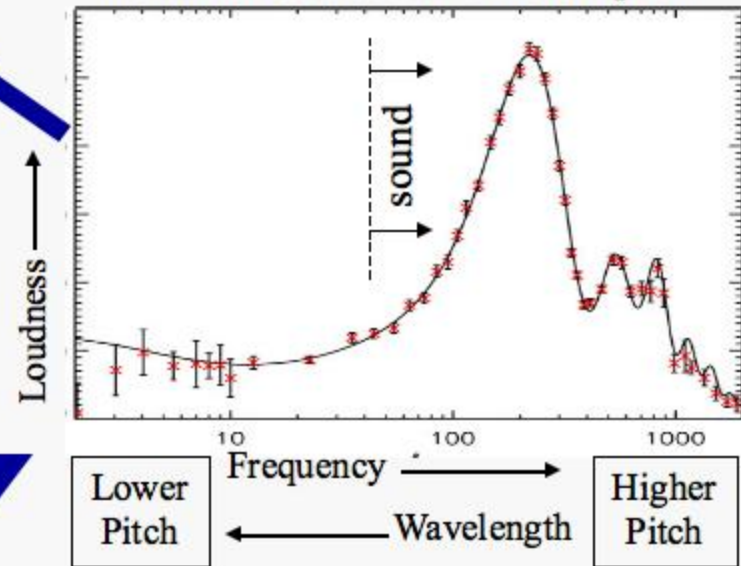


Sound Waves in the Sky

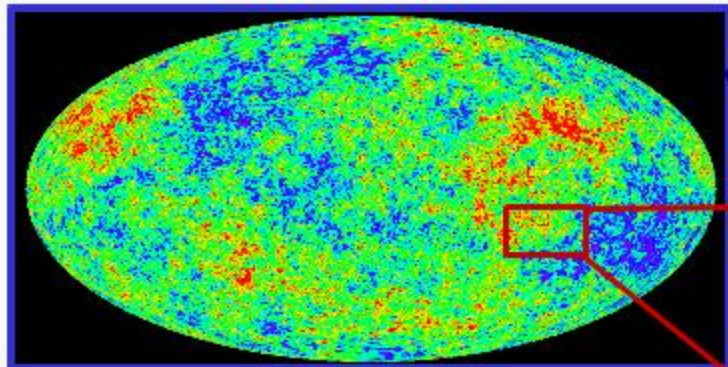


Loudspeaker

The CMB Power Spectrum
Relative loudness at different pitch



The Full Microwave Sky



Microwave brightness, greatly contrast stretched.
Brightness differences are also pressure differences
Patches smaller than 2° are sound waves

Water waves on the ocean surface illustrate
sound waves on the CMB "surface"



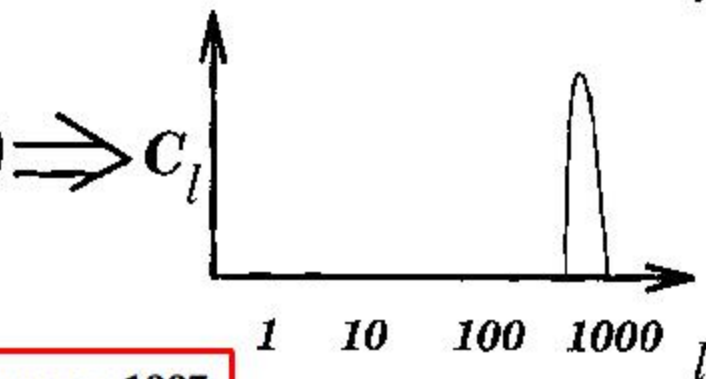
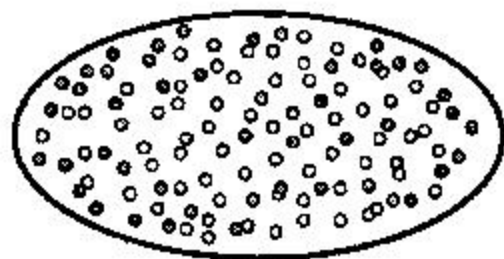
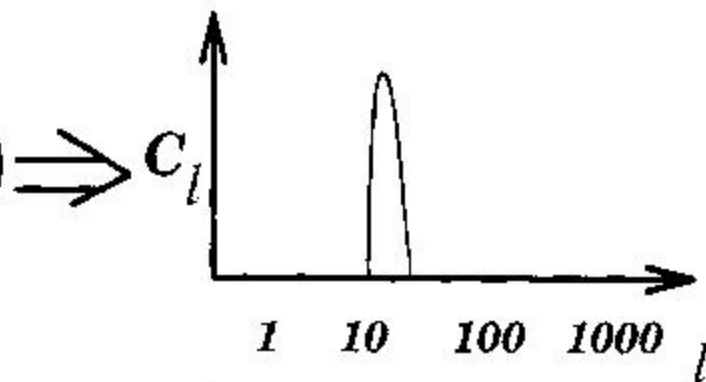
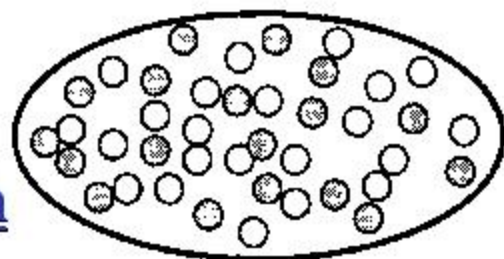
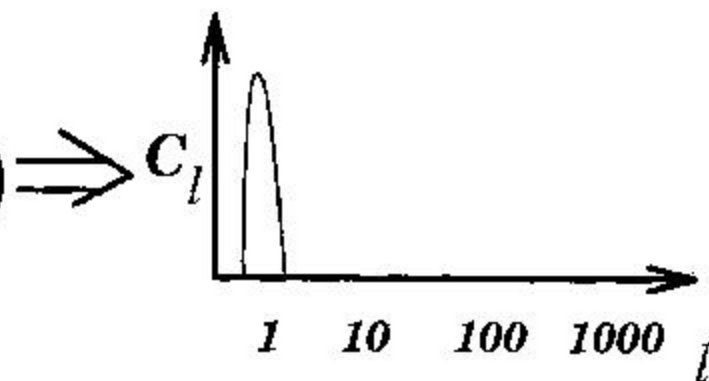
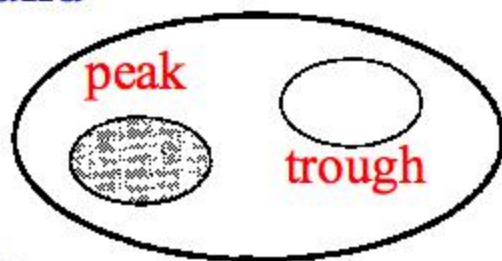
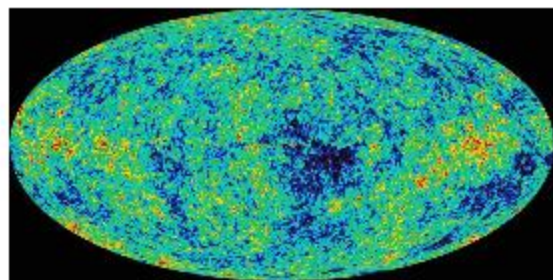
short
plus
medium
plus
long
all
mixed
together

Sky Maps \rightarrow Power Spectra

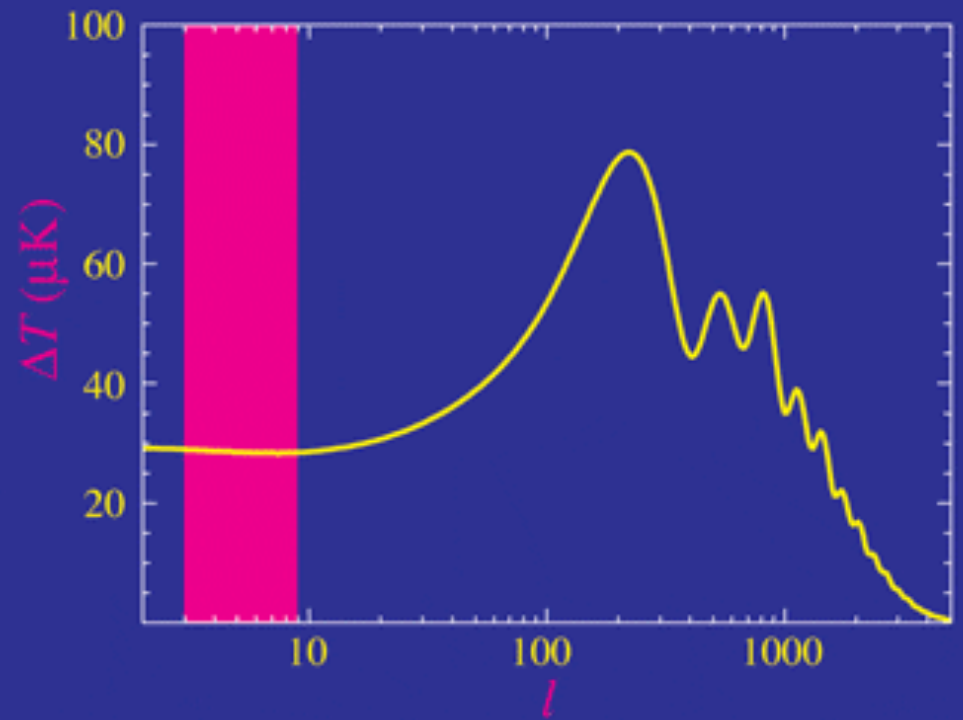
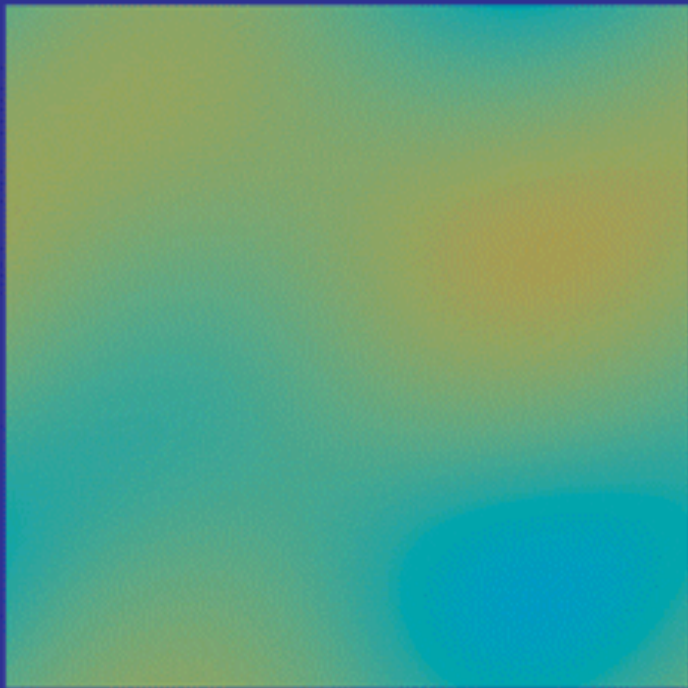
We “see” the CMB sound as waves on the sky.

Shorter wavelengths are smaller frequencies are higher pitches

Use special methods to measure the strength of each wavelength.



Lineweaver 1997



What are these fluctuations in CMB?

Fluctuations arise in very early universe ($t_{\text{ABB}} < 1$ sec) (as quantum fluctuations) – small non-uniformities which disturb the universe, causing sound waves

These sound waves survive and grow in size (linear scale) due to expansion. But they **do not grow in amplitude for first 380,000 yrs**, since photons were coupled to matter, preventing matter from collapsing

What is the furthest distance a signal could have traveled in the universe at the time when the CMB photons were produced?

- A. Infinite
- B. 13.7 BLY
- C. 380,000 LY
- D. 0 LY
- E. It depends on how the space in the universe is curved
- F. It depends on speed of CMB photons

The largest blobs in CMB are the largest causally connected regions

- How far could the fastest signal go through space during the entire history of the universe?

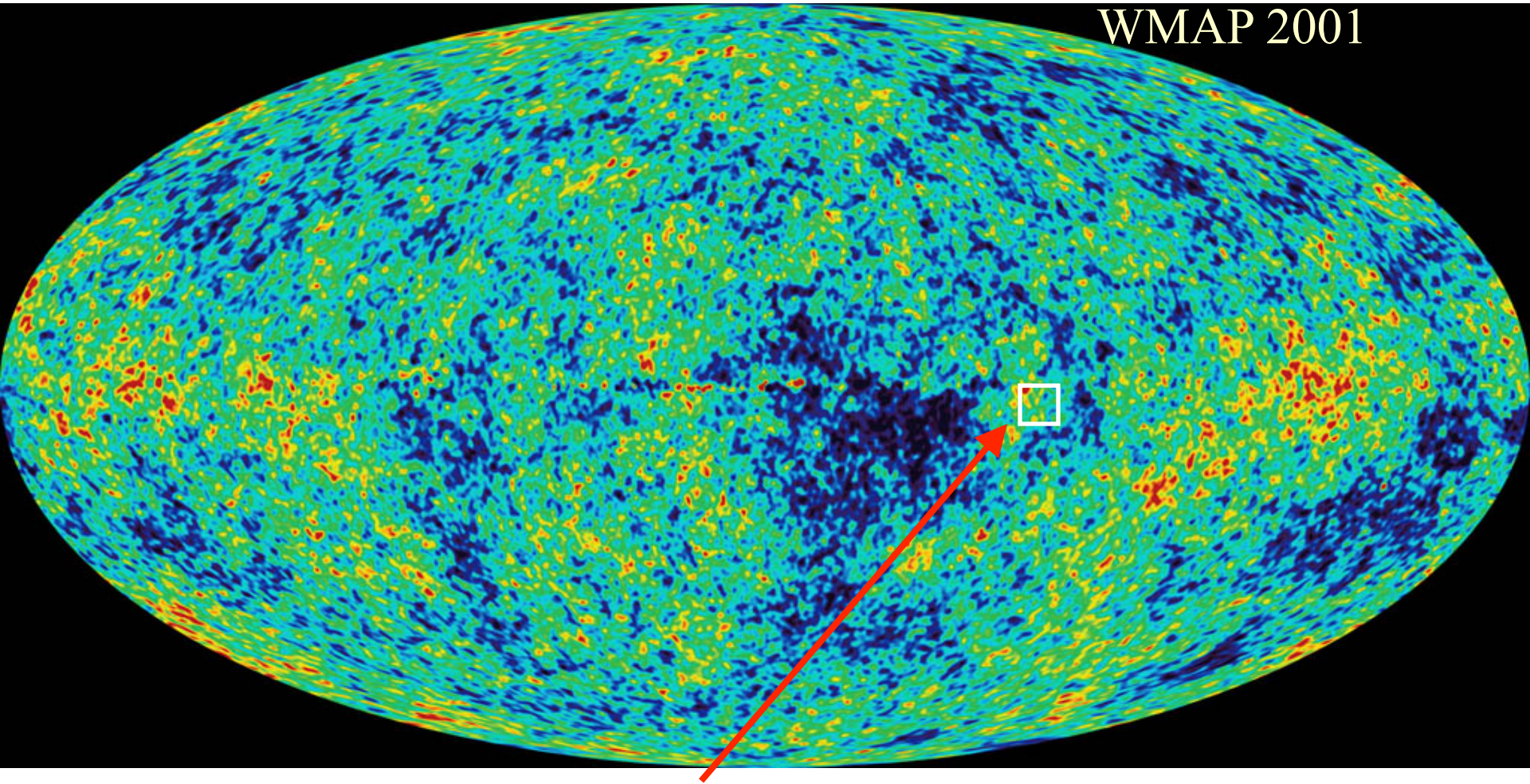
- This is the *Cosmic Light Horizon*

$$d_{\text{CLH}} = c t_{\text{ABB}}$$

- At age of $t_{\text{ABB}} = 380,000$ yrs
the largest causally connected region is

$$d_{\text{CLH}} = 380,000 \text{ LY in size}$$

WMAP 2001



Examine small patch of CMB

13.3 BLY (distance to CMB)

380,000 LY
(size of biggest
blobs in CMB)



Use “cosmological version” of small angle formula
(diagram shows case of *flat space*)

If space in the universe is:

Spherical

Flat

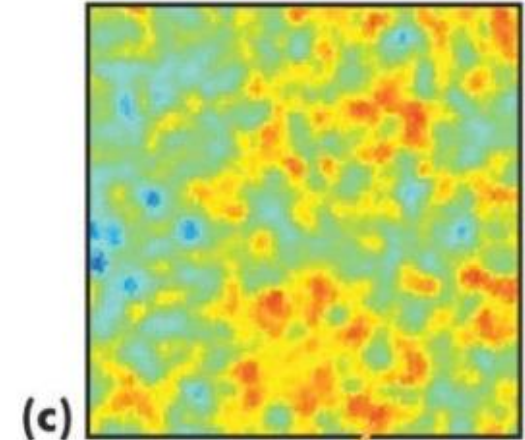
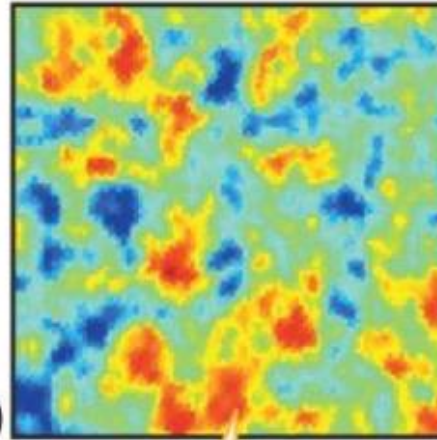
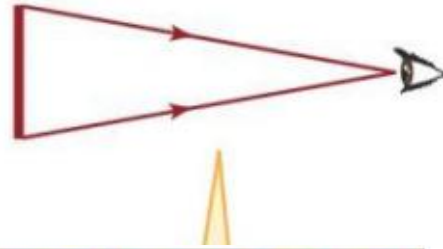
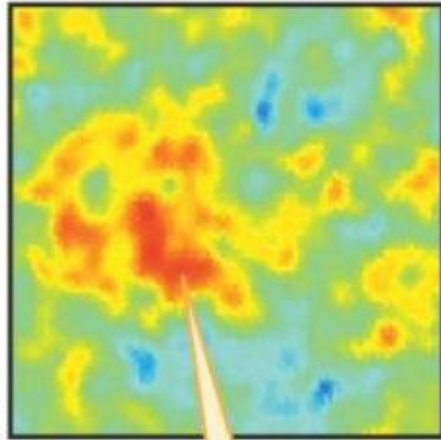
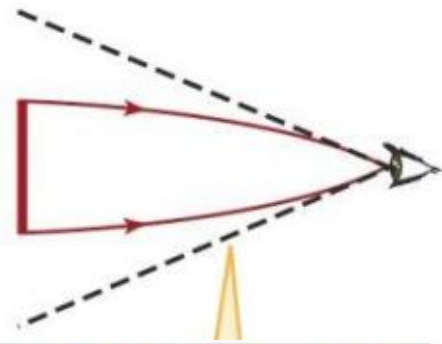
Hyperbolic

Then the biggest blobs in the CMB appear to be:

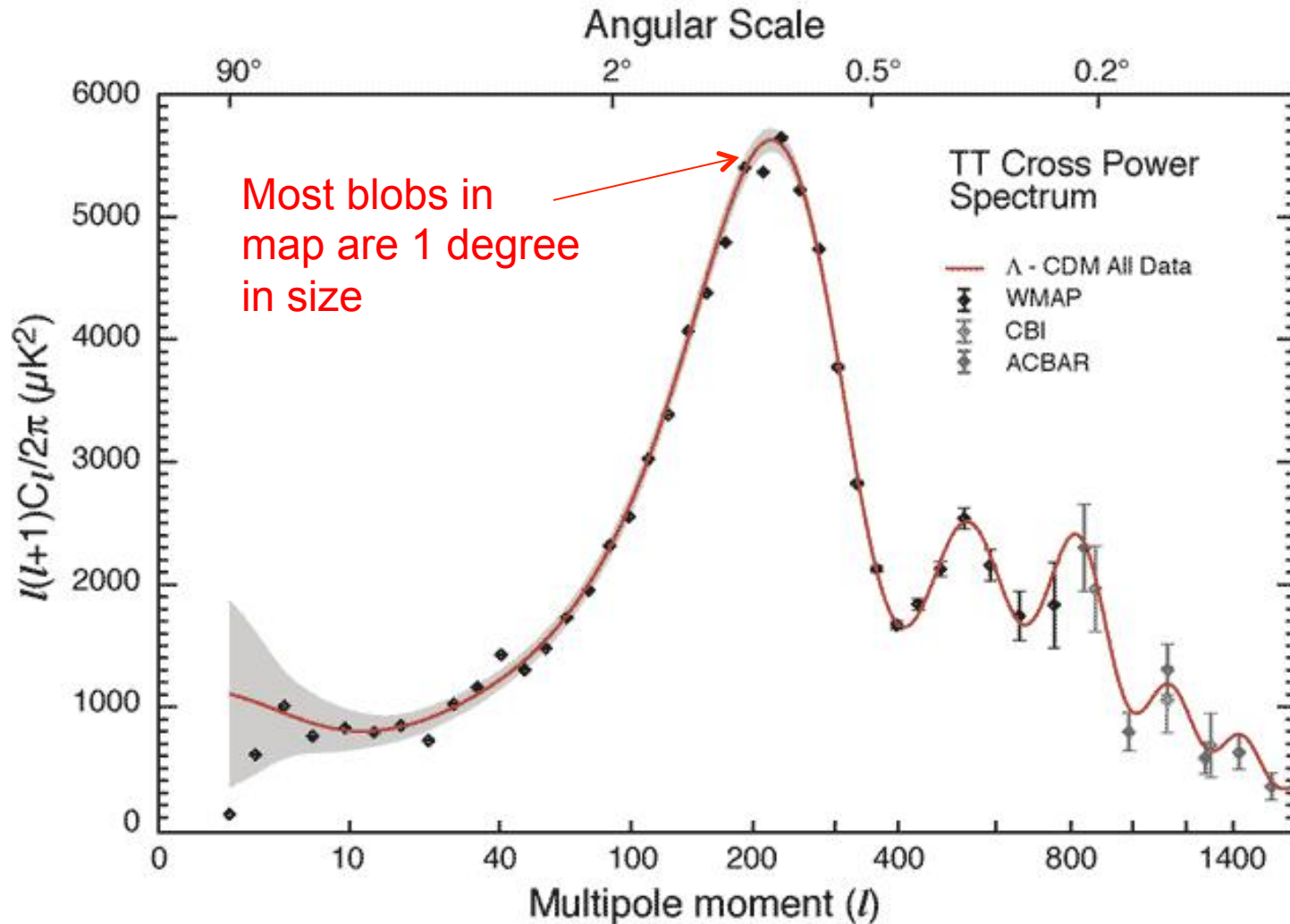
More than 1 deg

1 degree

Less than 1 deg



The structure in CMB map is not random!



13.3 BLY (distance to CMB)

380,000 LY
(size of biggest
blobs in CMB)

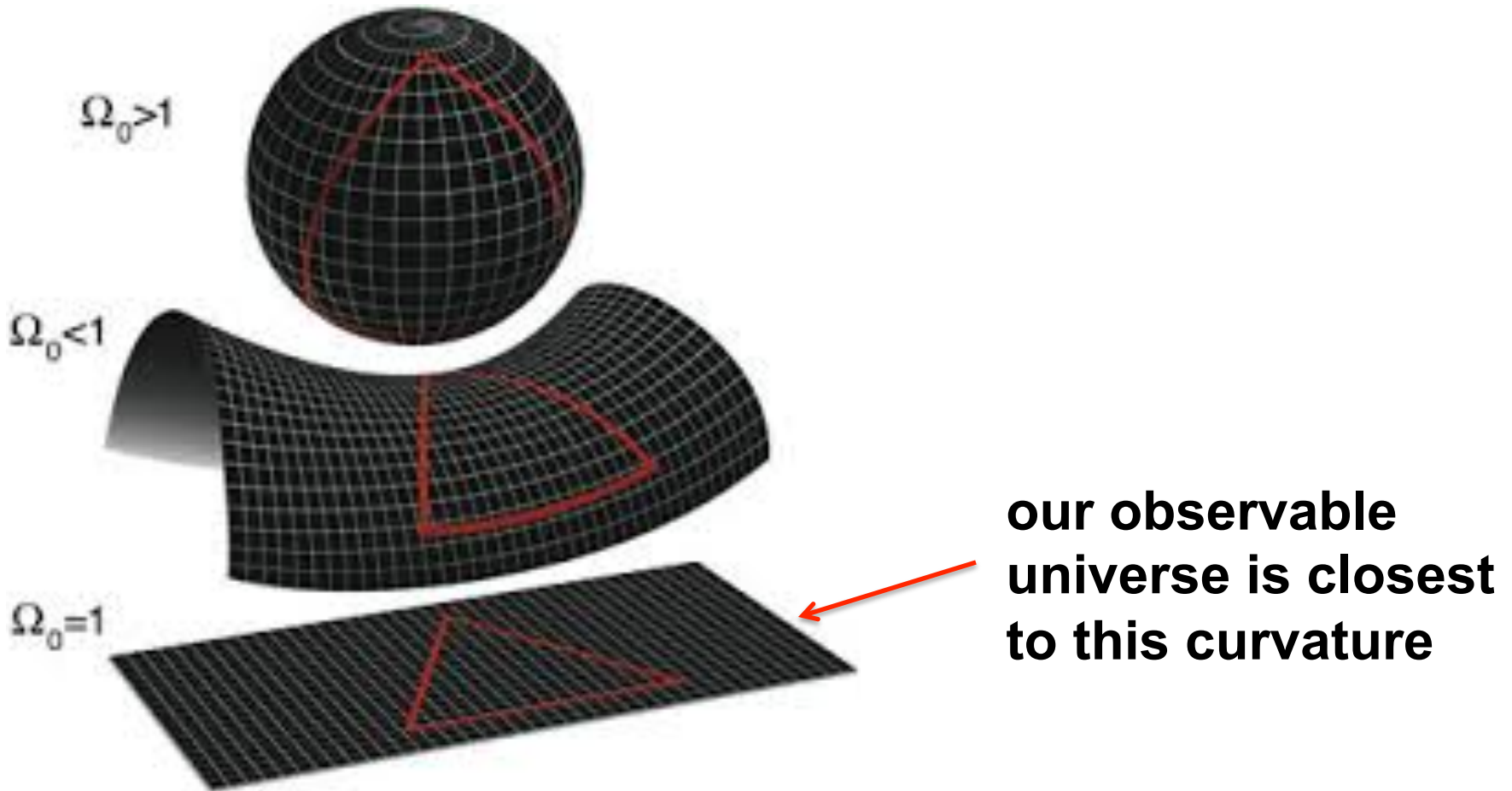


Use “cosmological version” of small angle formula
(diagram shows case of *flat space*)

What do we find?

- Biggest blobs are 1 degree in size
→ *space in universe appears flat !*

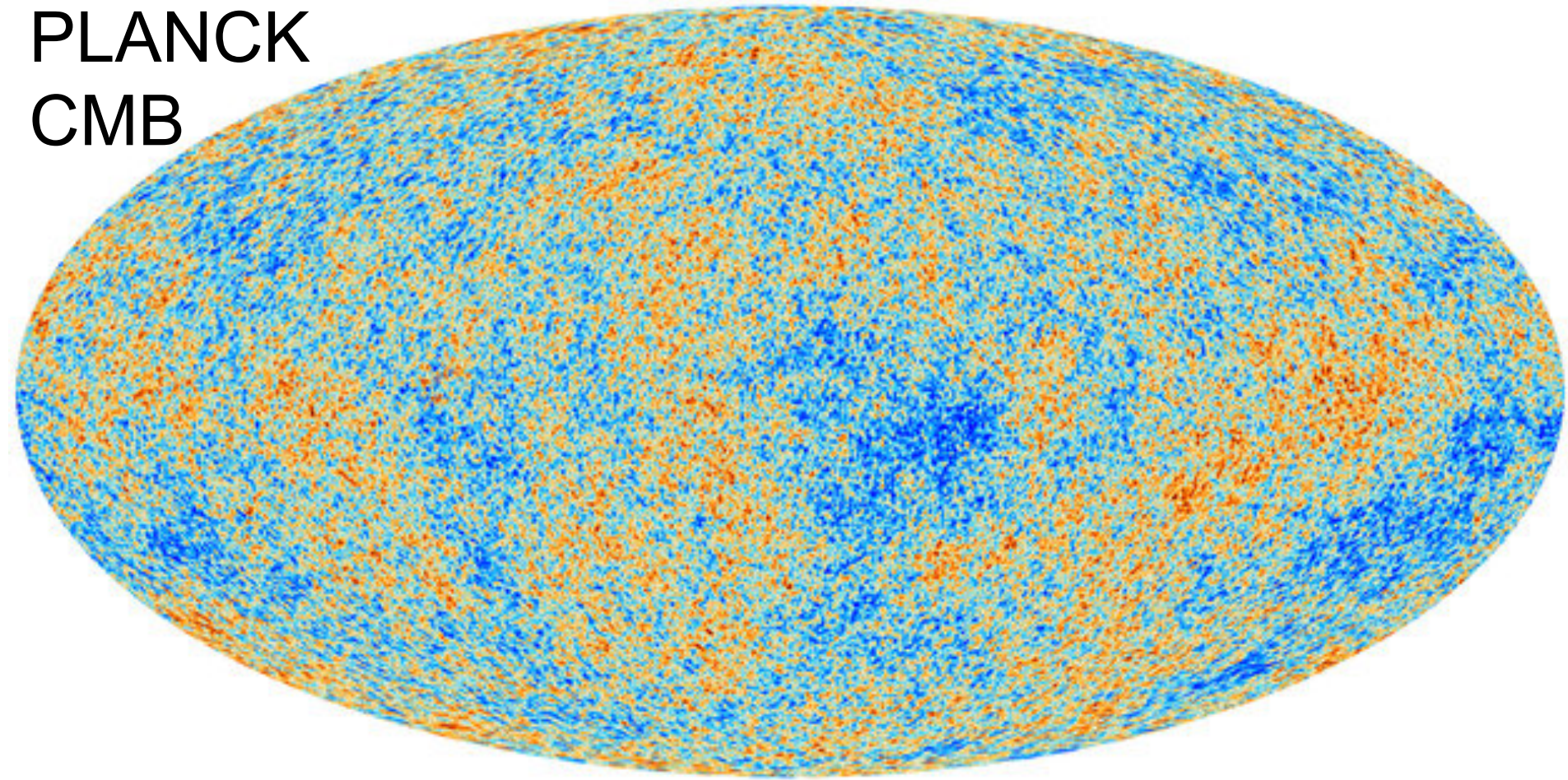
curvature of space



What do we find?

- Biggest blobs are 1 degree in size
→ *space in universe appears flat !*
- This has implications for
mass & energy content of universe
including evidence for **Dark Energy**

PLANCK CMB



Small fluctuations in cosmic background radiation tell us

2. how space in the Universe is curved &
3. contents of Universe!

Curvature of space & dark energy

Total amount (density) of matter, radiation & dark energy

$$\rho_0 = \rho_m + \rho_{\text{rad}} + \rho_\Lambda \quad \text{total density}$$

$$\Omega_m = \rho_m / \rho_{\text{crit}} \quad \text{matter (baryonic and dark matter)}$$

$$\Omega_{\text{rad}} = \rho_{\text{rad}} / \rho_{\text{crit}} \quad \text{radiation (cosmic background \& other photons)}$$

$$\Omega_\Lambda = \rho_\Lambda / \rho_{\text{crit}} \quad \text{dark energy}$$

$$\Omega_o = \Omega_m + \Omega_{\text{rad}} + \Omega_\Lambda \quad \text{total density parameter}$$

$$\Omega_o = \rho_0 / \rho_{\text{crit}} \quad ; \quad \rho_{\text{crit}} = 3 H_o^2 / 8 \pi G$$

Curvature of space & dark energy

$$\Omega_o = \Omega_m + \Omega_{\text{rad}} + \Omega_{\Lambda} = \rho_o / \rho_{\text{crit}} \quad \text{total density parameter}$$

$$\rho_{\text{crit}} = 3 H_o^2 / 8 \pi G$$

introduced previously in discussing FATE of universe

but in general $\rho_o / \rho_{\text{crit}}$ gives ***curvature of space***

Contents of universe determine its curvature!

Curvature of space & dark energy

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Contents of universe determine its curvature!

CMB fluctuations indicate:

$$\Omega_o = 1 \quad \text{i.e., flat universe}$$

We know $\Omega_m = 0.27$

$$\Omega_{\text{rad}} = 0.00005 \quad (\text{nearly zero!})$$

Curvature of space & dark energy

$$\Omega_o = \Omega_m + \Omega_{\text{rad}} + \Omega_\Lambda = \rho_o / \rho_{\text{crit}} \quad \text{total density parameter}$$

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$$\rightarrow \Omega_\Lambda = 0.73$$

i.e. dark energy must exist and is important component of universe!

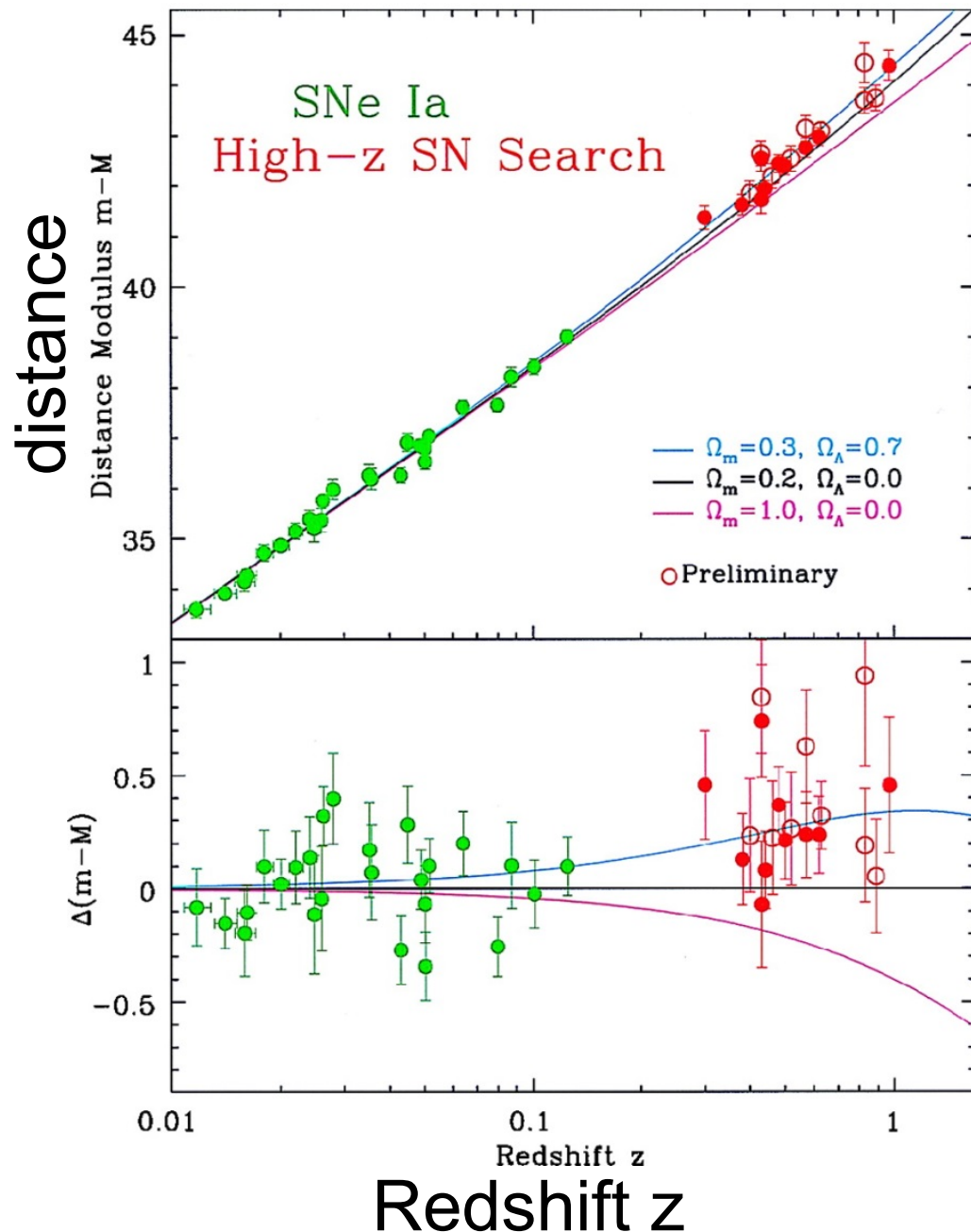
Type Ia supernova in nearby spiral galaxy



HST image of NGC 4526 in Virgo Cluster,
distance ~ 50 MLY



Type Ia supernovae
are
standard candles!

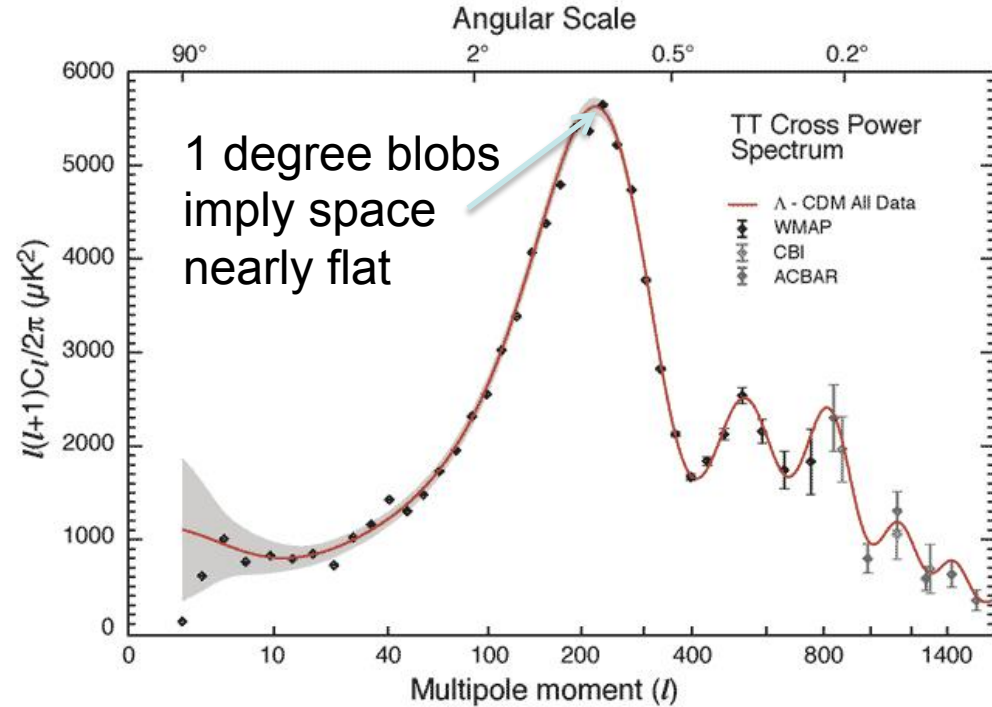
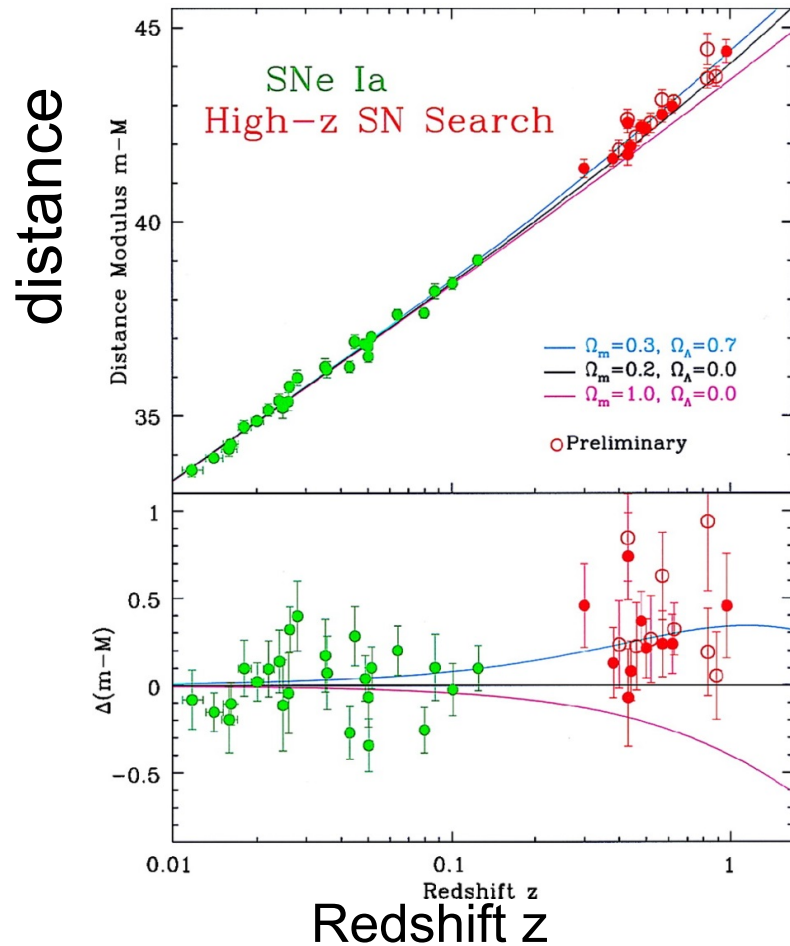


Evidence for *acceleration* in expansion of universe

Distant supernovae at a given distance have *smaller* redshifts than they would if expansion was constant or slowing down (decelerating)

This wins Nobel Prize in Physics in 2011 !!

Two forms of evidence for Dark Energy

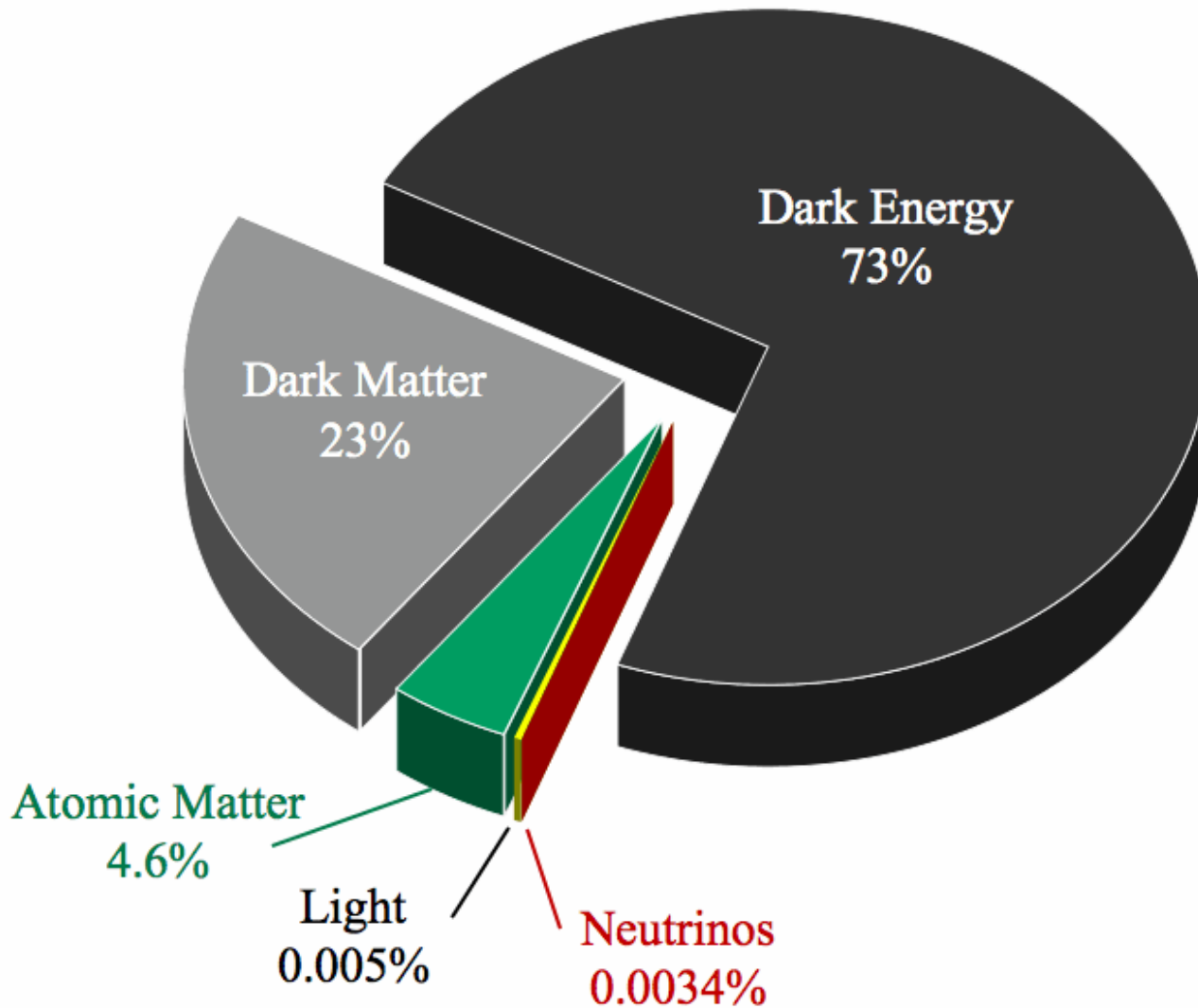


amount of Dark Energy needed to account for acceleration of expansion ($\Omega_\Lambda = 0.73$) is same amount needed to account for nearly flat space ($\Omega_o = 1 \rightarrow \Omega_\Lambda = 0.73$) in observable universe

Evidence for Dark Energy from distant standard candles (Type Ia SN)

1. For SN at given (large & known) distance, **redshift is smaller** than in case of constant expansion
2. Thus photons from large distances have been **stretched less** than constant expansion case
3. Which implies **less rapid expansion in past**
4. Which implies **expansion rate has accelerated**
5. Something must have caused acceleration; that something given name “Dark Energy”

Mass-energy budget of present universe



What is Dark Energy?

- A. the energy associated with dark matter
 $E_{\text{DARK}} = M_{\text{DARK}} c^2$
- B. the mass-energy needed to balance the effect that gravity has on the expansion of the universe
- C. the mass-energy needed to bridge the gap between the mass we know exists and what is needed to make the universe flat
- D. the mass-energy which is causing the expansion to decelerate
- E. Putin's REAL secret plan